

Math 335-002 * Spring 2015

Homework #2

Due date: Thursday, February 5, 2015

Please show all work in detail to receive full credit

1. Simplify the following expression. Hint: use the BAC-CAB rule (see exercise 23 on page 50), and multiply the result by **a**. Bold letters indicate vectors.

$$((\mathbf{a} \times \mathbf{b}) \times \mathbf{b}) \times \mathbf{a}$$

2. Problem 24(b), page 50:

$$\text{Show that } (\mathbf{u} \times \mathbf{v}) \cdot (\mathbf{u}' \times \mathbf{v}') = (\mathbf{u} \cdot \mathbf{u}') (\mathbf{v} \cdot \mathbf{v}') - (\mathbf{u} \cdot \mathbf{v}') (\mathbf{u}' \cdot \mathbf{v})$$

Hint: you have to transform this expression twice: first, note that this can be viewed as a scalar triple product of three vectors, so you can use the cyclical property of the scalar triple product; then, use the BAC-CAB rule of triple vector product (see exercise 23 on page 50)

3. Problem 2, p. 58: Find the spherical coordinates of the Cartesian point $(\sqrt{6}, -\sqrt{2}, -2\sqrt{2})$
4. Problem 7, page 59: describe and sketch the following surfaces, which are given in cylindrical or polar coordinates:
 - (a) $z = r^2$
 - (b) $\rho = 4 \csc \phi \sec \theta$
 - (c) $r = 4 \sin \theta$
 - (d) $\rho \sin \phi = 2$

Hint: this is much easier than this looks. In (b) and (d), convert each equation to Cartesian coordinates (x, y, z) to identify these very simple surfaces.