

Solid State Physics			
(Ch. 2)		Lecture	3
Last week:			
 Crystals, Crystals, Cry	tal Lattice, Recipr n crystals	ocal Lattice,	
• Today:			
 Scattering factors and selection rules for diffraction 			
HW2 discussion			
Lecture 3	Andrei Sirenko, NJIT		2















Diffraction process: 1) Scattering by individual atoms 2) Mutual interference between scattered rays **Scattering from atom** Consider single electron. Plane wave $u = Ae^{i(\mathbf{k}\cdot\mathbf{r}-\omega t)}$ $k = |\mathbf{k}| = \frac{2\pi}{\lambda}$ Scattered field: $u' = f_e \frac{A}{R} e^{i(kR-\omega t)}$ $f_e - scattering length of electron$ R - radial distanceTwo electrons: $u' = f_e \frac{A}{R} e^{ikR} [1 + e^{i\Delta \mathbf{k}\cdot\mathbf{r}}]$ or, more generally $u' = f_e \frac{A}{R} e^{ikR} [e^{i\Delta \mathbf{k}\cdot\mathbf{r}_1} + e^{i\Delta \mathbf{k}\cdot\mathbf{r}_2}]$ many electrons: $u' = f_e \frac{A}{R} e^{ikR} \sum_{l} e^{i\Delta \mathbf{k}\cdot\mathbf{r}_l}$ similar to single electron with $f = f_e \sum_{l} e^{i\Delta \mathbf{k}\cdot\mathbf{r}_l}$

intensity:
$$I \sim |f| = f_e^{2} \left| \sum_{l} e^{i\Delta \mathbf{k}\cdot\mathbf{r}_l} \right|^2$$

this is for coherent scatterers. If random then $I \sim N f_e^{2}$
Scattering length of electron: $f_e = \left[\left(1 + \cos^2 2\theta \right) / 2 \right]^{1/2} r_e$
classical electron radius $r_e = \frac{1}{4\pi\varepsilon_0} \frac{e^2}{mc^2} \approx 2.8 \times 10^{-15} \text{ m}$
In atom, $f_e \sum_{l} e^{i\Delta \mathbf{k}\cdot\mathbf{r}_l} \rightarrow f_e \int n(\mathbf{r}) e^{i\Delta \mathbf{k}\cdot\mathbf{r}_l} d^3 r$
 $f_a = \int n(\mathbf{r}) e^{i\Delta \mathbf{k}\cdot\mathbf{r}_l} d^3 r$ - atomic scattering factor (form factor)
Lecture 3 Andrei Sirenko, NJIT 11

































