

2.34) $x(n) = \cos(\Omega_0 n T)$. If $x(n)$ is periodic with a period N , then

$$x(n+N) = \cos(\Omega_0 n T + \Omega_0 N T) = x(n) = \cos(\Omega_0 n T)$$

This implies $\Omega_0 N T = 2\pi r$ with r any nonzero positive integer. Hence, the sampling rate must satisfy the relation $T = 2\pi r / \Omega_0 N$. If $\Omega_0 = 20$, i.e., $T = \pi/8$, then we must have $20N \frac{\pi}{8} = 2\pi r$. The smallest value of N and r satisfying this relation are $N=4$ and $r=5$.

The fundamental period is thus $N=4$.

2.49) Make use of the identity $\delta(n-m) \otimes \delta(n-r) = \delta(n-m-r)$

$$a) y_1(n) = x_1(n) \otimes h_1(n) = [3\delta[n-2] - 2\delta[n+1]] \otimes [-\delta(n+2) + 4\delta(n) + 2\delta(n-1)]$$

$$= -3\delta(n-2) \otimes \delta(n+2) + 12\delta(n-2) \otimes \delta(n) - 6\delta(n-2) \otimes \delta(n-1) + 2\delta(n+1) \otimes \delta(n+2) - 8\delta(n+1) \otimes \delta(n) + 4\delta(n+1) \otimes \delta(n-1). \text{ Hence,}$$

$$y_1(n) = -3\delta(n) + 12\delta(n-2) - 6\delta(n-3) + 2\delta(n+3) - 8\delta(n+1) + 4\delta(n) \\ = 2\delta(n+3) - 8\delta(n+1) + \delta(n) + 12\delta(n-2) - 6\delta(n-3).$$

$$b) y_2(n) = x_2(n) \otimes h_2(n) = 15\delta(n-7) + 7.5\delta(n-5) - 5\delta(n-2) + 6\delta(n-3) + 3\delta(n-1) - 2\delta(n+2)$$

$$c) y_3(n) = x_1(n) \otimes h_2(n) = 2\delta(n+2) - 6\delta(n-1) - 6\delta(n-3) + 4.5\delta(n-4) + 9\delta(n-6)$$

$$d) y_4(n) = x_2(n) \otimes h_1(n) = -2\delta(n+3) + 8\delta(n+1) - 4\delta(n) - 5\delta(n-1) + 20\delta(n-3) - 10\delta(n-4)$$