

Biol698/Math635/Math430
Fall 2018

Homework 2

Answer the following questions. Justify your answers, explain your results, and provide the necessary calculations in a clear way.

Question 1

Calculate the equilibrium (reversal) potentials for the following ions at a temperature of 20° C.

- (a) K^+ , $[K^+]_{out} = 5 \text{ mmol/L}$, $[K^+]_{in} = 150 \text{ mmol/L}$.
- (b) Na^+ , $[Na^+]_{out} = 150 \text{ mmol/L}$, $[Na^+]_{in} = 15 \text{ mmol/L}$.
- (c) Cl^- , $[Cl^-]_{out} = 125 \text{ mmol/L}$, $[Cl^-]_{in} = 10 \text{ mmol/L}$.
- (d) Ca^{2+} , $[Ca^{2+}]_{out} = 2 \text{ mmol/L}$, $[Ca^{2+}]_{in} = 0.0002 \text{ mmol/L}$.

What is the effect of increasing the temperature to 25° C (room temperature) on these equilibrium potentials.

Question 2

Consider an ion X^+ at room temperature (20° C). What is the concentration relation $[X^+]_{out}/[X^+]_{in}$ necessary to maintain a resting membrane potential $V = -60 \text{ mV}$?

How is this value affected when the temperature is increased to 25° C?

Question 3

Consider the following passive membrane equation

$$\tau \frac{dV}{dt} = -(V - E_L) + R I_{app} \quad (1)$$

with $V(0) = E_L$, $R = 100 \text{ M}\Omega$, $C = 100 \text{ pF}$, $I_{app} = 0.25 \text{ nA}$ and $E_L = -60 \text{ mV}$.

- (a) Calculate the value of τ .
- (b) Calculate the value of the term $R I_{app}$.
- (c) Calculate, if possible, the time it takes the voltage to reach $V = -50 \text{ mV}$.
- (d) Calculate, if possible, the time it takes the voltage to reach $V = -30 \text{ mV}$.

Question 4

Write a code to solve numerically eq. (1) or adapt the template code provided in the course website. Simulate eq. (1) for the parameter provided in Question 3.

Note: The axis should be labeled correctly and the fonts should be large enough (suggested: “fontsize” = 24).