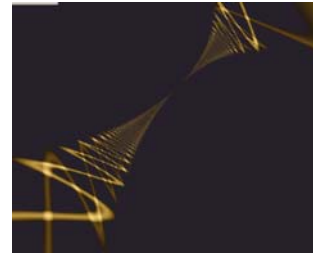


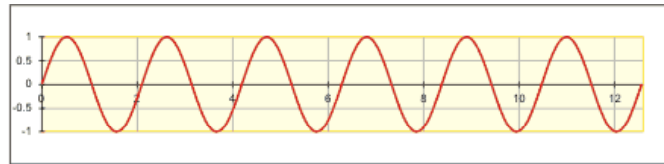
Lecture 9

Sound and Waves



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Physics 103 Spring 2012



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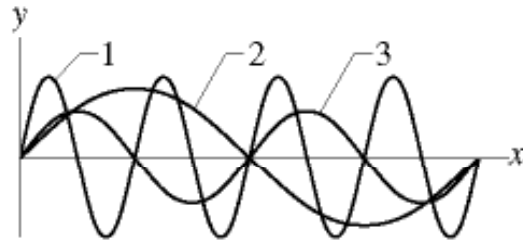
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WAVES: QZ2

The figure is a composite of three snapshots, each of a wave traveling along a particular string. The phases for the waves are given by

- (a) $2x - 4t$,
- (b) $4x - 8t$, and
- (c) $8x - 16t$.



Which phase corresponds to which wave in the figure?

$$y(x, t) = y_m \sin(kx - \omega t).$$

$$k = \frac{2\pi}{\lambda} \quad (\text{angular wave number}).$$

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Summary

Transverse and Longitudinal Waves

Mechanical waves can exist only in material media and are governed by Newton's laws. **Transverse** mechanical waves, like those on a stretched string, are waves in which the particles of the medium oscillate perpendicular to the wave's direction of travel. Waves in which the particles of the medium oscillate parallel to the wave's direction of travel are **longitudinal** waves.

Sinusoidal Waves

A sinusoidal **wave** moving in the positive x direction has the mathematical form

$$y(x,t) = y_m \sin(kx - \omega t), \quad (17-2)$$

where y_m is the **amplitude** of the wave, k is the **angular wave number**, ω is the **angular frequency**, and $kx - \omega t$ is the **phase**. The **wavelength** λ is related to k by

$$k = \frac{2\pi}{\lambda}. \quad (17-5)$$

The **period** T and **frequency** f of the wave are related to ω by

$$\frac{\omega}{2\pi} = f = \frac{1}{T}. \quad (17-9)$$

Finally, the **wave speed** v is related to these other parameters by

$$v = \frac{\omega}{k} = \frac{\lambda}{T} = \lambda f. \quad (17-12)$$

Summary

Equation of a Traveling Wave

Any function of the form

$$y(x,t) = h(kx \pm \omega t) \quad (17-16)$$

can represent a **traveling wave** with a **wave** speed given by Eq. 17-12 and a wave shape given by the mathematical form of h . The plus sign denotes a wave traveling in the negative x direction, and the minus sign a wave traveling in the positive x direction.

Wave Speed on Stretched String

The speed of a **wave** on a stretched string is set by properties of the string. The speed on a string with **tension** τ and linear **density** μ is

$$v = \sqrt{\frac{\tau}{\mu}}. \quad (17-25)$$

Power

The **average power**, or average rate at which energy is transmitted by a sinusoidal **wave** on a stretched string, is given by

$$P_{\text{avg}} = \frac{1}{2} \mu v \omega^2 y_m^2. \quad (17-32)$$

Summary

Superposition of Waves

When two or more waves traverse the same medium, the displacement of any particle of the medium is the sum of the displacements that the individual waves would give it.

Interference of Waves

Two sinusoidal waves on the same string exhibit **interference**, adding or canceling according to the principle of **superposition**. If the two are traveling in the same direction and have the same **amplitude** y_m and **frequency** (hence the same wavelength) but differ in **phase** by a **phase**

constant ϕ , the result is a single **wave** with this same frequency:

$$y'(x, t) = [2y_m \cos \frac{1}{2} \phi] \sin(kx - \omega t + \frac{1}{2} \phi). \quad (17-38)$$

If $\phi = 0$, the waves are exactly in phase and their **interference** is fully constructive; if $\phi = \pi$ rad, they are exactly out of phase and their interference is fully **destructive**.

Summary

Standing Waves

The **interference** of two identical sinusoidal waves moving in opposite directions produces **standing waves**. For a string with fixed ends, the **standing wave** is given by

$$y'(x, t) = [2y_m \sin kx] \cos \omega t. \quad (17-47)$$

Standing waves are characterized by fixed locations of zero displacement called **nodes** and fixed locations of maximum displacement called **antinodes**.

Resonance

Standing waves on a string can be set up by reflection of traveling waves from the ends of the string. If an end is fixed, it must be the position of a node. This limits the frequencies at which standing waves will occur on a given string. Each possible **frequency** is a **resonant frequency**, and the corresponding **standing wave** pattern is an **oscillation mode**. For a stretched string of length L with fixed ends, the **resonant** frequencies are

$$f = \frac{v}{\lambda} = n \frac{v}{2L}, \quad \text{for } n = 1, 2, 3, \dots \quad (17-53)$$

The oscillation mode corresponding to $n = 1$ is called the *fundamental mode* or the *first harmonic*; the mode corresponding to $n = 2$ is the *second harmonic*; and so on.

SOUND WAVES:

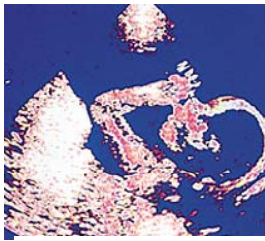
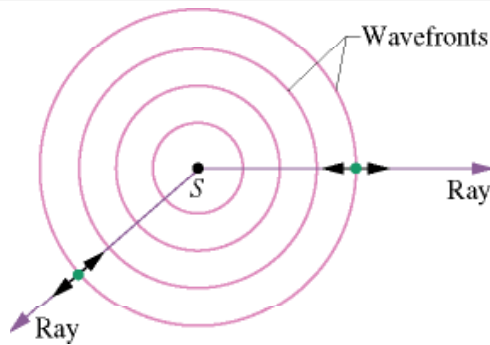


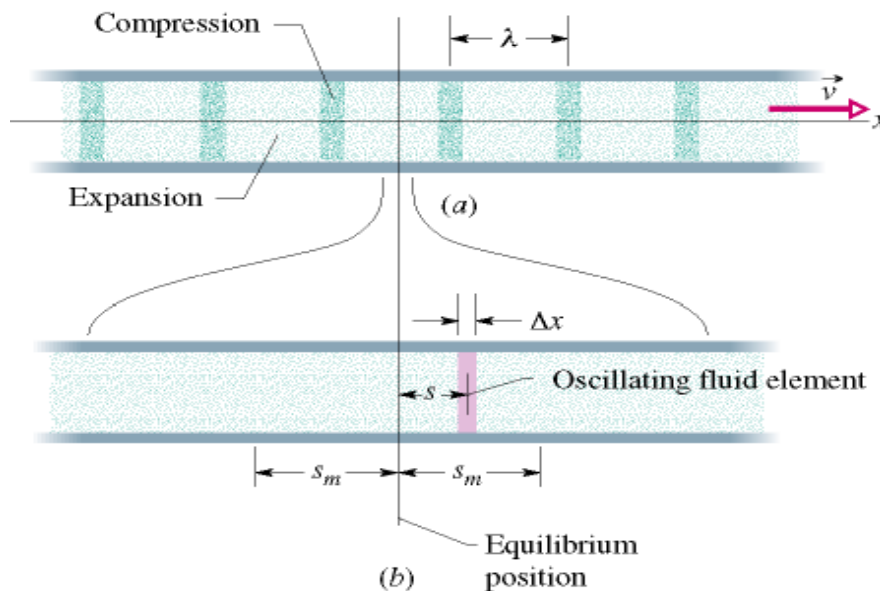
TABLE 18-1 The Speed of Sound^a

Medium	Speed (m/s)
<i>Gases</i>	
Air (0°C)	331
Air (20°C)	343
Helium	965
Hydrogen	1284
<i>Liquids</i>	
Water (0°C)	1402
Water (20°C)	1482
Seawater ^b	1522
<i>Solids</i>	
Aluminum	6420
Steel	5941
Granite	6000



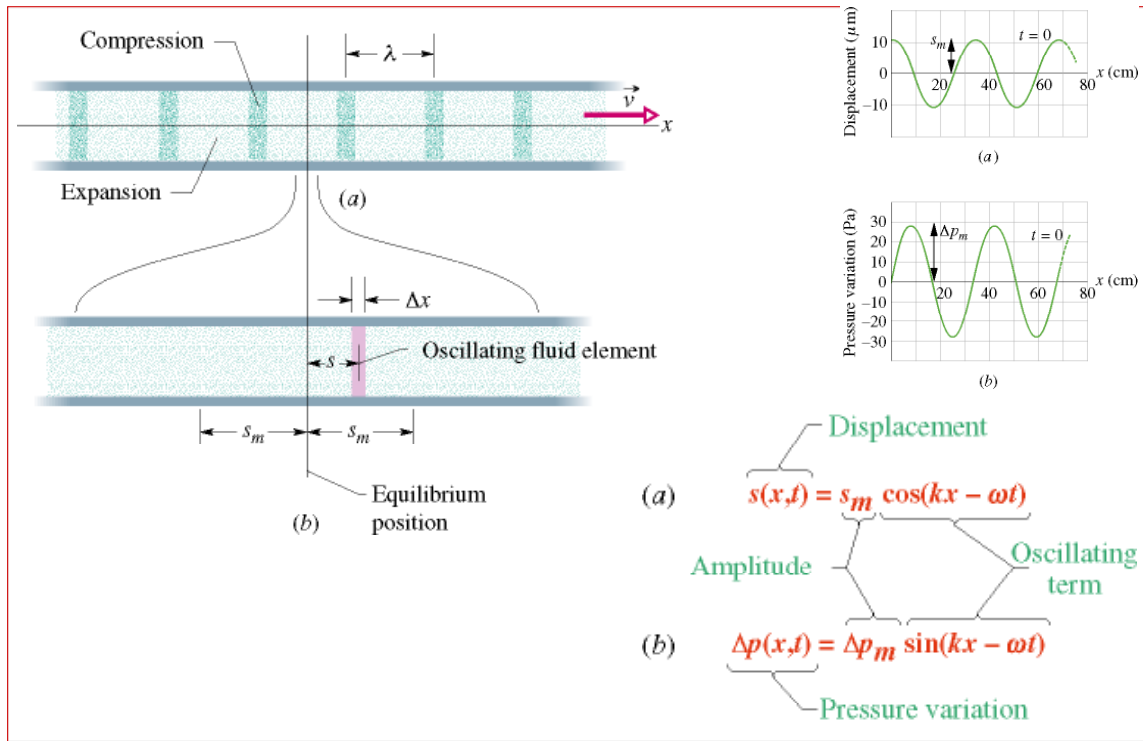
$$v = \sqrt{\frac{\tau}{\mu}} = \sqrt{\frac{\text{elastic property}}{\text{inertial property}}}$$

TRAVELLING SOUND WAVES:

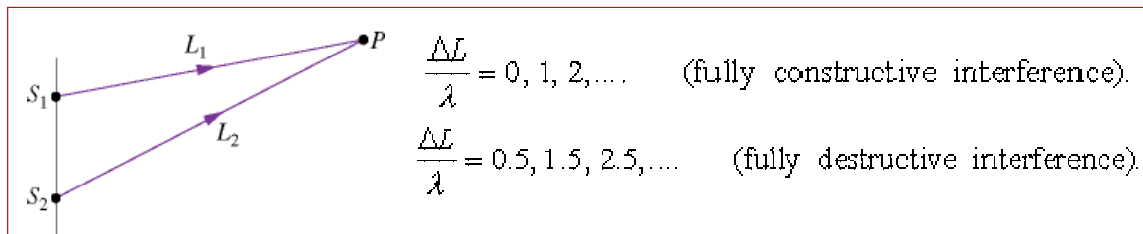


A **sound** wave, traveling through a long air-filled tube with speed v , consists of a moving, periodic pattern of expansions and compressions of the air.

TRAVELLING SOUND WAVES:



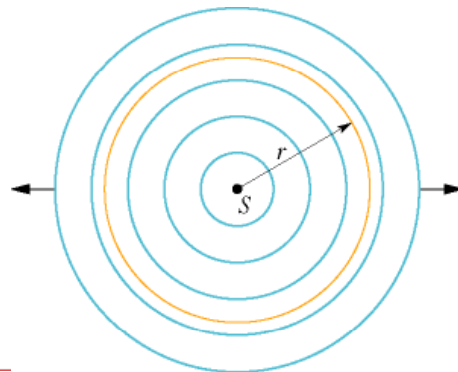
INTERFERENCE of the SOUND WAVES:



INTENSITY of the SOUND WAVES:

$$I = \frac{P_s}{4\pi r^2},$$

$$I = \frac{1}{2} \rho v \omega^2 s_m^2.$$



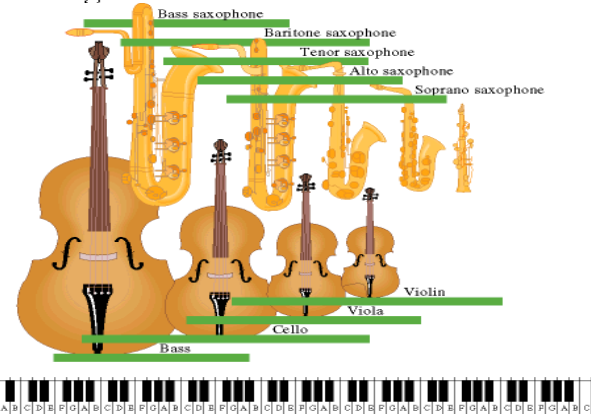
The Decibel Scale:

$$\beta = (10 \text{ dB}) \log \frac{I}{I_0}$$



TABLE 18-2 Some Sound Levels (dB)

Hearing threshold	0
Rustle of leaves	10
Conversation	60
Rock concert	110
Pain threshold	120
Jet engine	130



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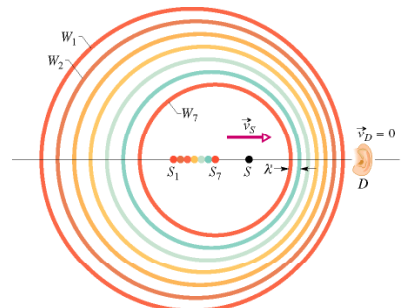
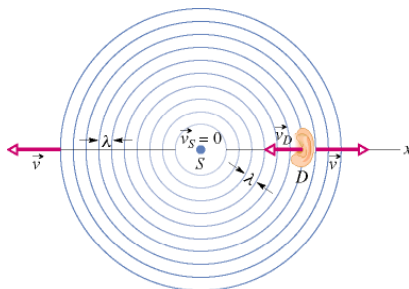
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The Doppler Effect

For speeds v less than

$$f' = f \frac{v \pm v_D}{v \pm v_S}$$

the **speed of sound**
(general Doppler effect),



When the motion of detector or source is toward the other, the sign on its speed must give an upward shift in **frequency**. When the motion of detector or source is away from the other, the sign on its speed must give a downward shift in frequency

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Supersonic Speeds; Shock Waves

(a) (b)

$$\sin \theta = \frac{v_f}{v_s t} = \frac{v}{v_s} \quad (\text{Mach cone angle}).$$

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Summary

Sound Waves

Sound waves are longitudinal mechanical waves that can travel through solids, liquids, or gases. The speed v of a sound wave in a medium having bulk modulus B and density ρ is

$$v = \sqrt{\frac{B}{\rho}} \quad (\text{speed of sound}). \quad (18-3)$$

In air at 20°C, the speed of sound is 343 m/s.

A sound wave causes a longitudinal displacement s of a mass element in a medium as given by

$$s = s_m \cos(kx - \omega t), \quad (18-13)$$

where s_m is the displacement amplitude (maximum displacement) from equilibrium, $k = 2\pi/\lambda$, and $\omega = 2\pi f$, λ and f being the wavelength and frequency, respectively, of the sound wave. The sound wave also causes a pressure change Δp of the medium from the equilibrium pressure:

$$\Delta p = \Delta p_m \sin(kx - \omega t), \quad (18-14)$$

where the pressure amplitude is

$$\Delta p_m = (v\rho\omega)s_m. \quad (18-15)$$

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Summary

Interference

The **interference** of two **sound** waves with identical wavelengths passing through a common point depends on their **phase** difference ϕ there. If the sound waves were emitted in phase and are traveling in approximately the same direction, ϕ is given by

$$\phi = \frac{\Delta L}{\lambda} 2\pi, \quad (18-21)$$

where ΔL is their **path length difference** (the difference in the distances traveled by the waves to reach the common point). Fully constructive interference occurs when ϕ is an integer multiple of 2π ,

$$\phi = m(2\pi), \quad \text{for } m = 0, 1, 2, \dots, \quad (18-22)$$

and, equivalently, when ΔL is related to **wavelength** λ by

$$\frac{\Delta L}{\lambda} = 0, 1, 2, \dots \quad (18-23)$$

Fully destructive interference occurs when ϕ is an odd multiple of π ,

$$\phi = (2m+1)\pi, \quad \text{for } m = 0, 1, 2, \dots, \quad (18-24)$$

and, equivalently, when ΔL is related to λ by

$$\frac{\Delta L}{\lambda} = 0.5, 1.5, 2.5, \dots \quad (18-25)$$

Summary

Sound Intensity

The **intensity** I of a **sound wave** at a surface is the average rate per unit area at which energy is transferred by the wave through or onto the surface:

$$I = \frac{P}{A}, \quad (18-26)$$

where P is the time rate of energy transfer (power) of the sound wave and A is the area of the surface intercepting the sound. The **intensity** I is related to the displacement **amplitude** s_m of the sound wave by

$$I = \frac{1}{2} \rho v \omega^2 s_m^2. \quad (18-27)$$

The intensity at a distance r from a point source that emits sound waves of power P_s is

$$I = \frac{P_s}{4\pi r^2}. \quad (18-28)$$

Sound Level in Decibels

The **sound level** β in **decibels** (dB) is defined as

$$\beta = (10 \text{ dB}) \log \frac{I}{I_0}, \quad (18-29)$$

where I_0 ($= 10^{-12} \text{ W/m}^2$) is a reference **intensity** level to which all intensities are compared. For every factor-of-10 increase in intensity, 10 dB is added to the **sound** level.

Summary

The Doppler Effect

The *Doppler effect* is a change in the observed **frequency** of a **wave** when the source or the detector moves relative to the transmitting medium (such as air). For **sound** the observed frequency f' is given in terms of the source frequency f by

$$f' = f \frac{v \pm v_D}{v \pm v_S} \quad (\text{general Doppler effect}), \quad (18-47)$$

where v_D is the speed of the detector relative to the medium, v_S is that of the source, and v is the **speed of sound** in the medium. The signs are chosen such that f' tends to be *greater* for motion (of detector or source) “toward” and *less* for motion “away.”

Shock Wave

If the speed of a source relative to the medium exceeds the **speed of sound** in the medium, the **Doppler** equation no longer applies. In such a case, shock waves result. The half angle θ of the Mach cone is given by

$$\sin \theta = \frac{v}{v_S} \quad (\text{Mach cone angle}). \quad (18-57)$$