

Lecture 2

Motion along a straight line

(HR&W, Chapter 2)

Physics 105; Summer 2007

Lecture 2

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Motion along a straight line

- Motion
- Position and Displacement
- Average velocity and average speed
- Instantaneous velocity and speed
- Acceleration
- Constant acceleration: A special case
- Free fall acceleration

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Motion

- Everything moves!
- Classification and comparison of motion
⇒ **kinematics**
- Simplification
 - Motion along straight line
 - Forces cause changes in motion
 - Moving object is a particle or moves like a particle



LA

Newark



particle

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Motion along a straight line

- this is the simplest type of motion
- it lays the groundwork for more complex motion

Kinematic variables in one dimension

Position	$x(t)$ meters
Velocity	$v(t)$ meters/second
Acceleration	$a(t)$ meters/second ²

All depend on time

All are vectors: have direction and magnitude.

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One Dimensional Position: $x(t)$

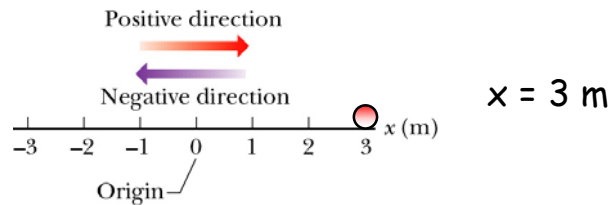
Position is a **vector** quantity.

Position has both a **direction** and **magnitude**.

Position has units of [Length]: *meters*.

Must define:

- > $x = 0$ some position (Origin)
- > positive direction for x

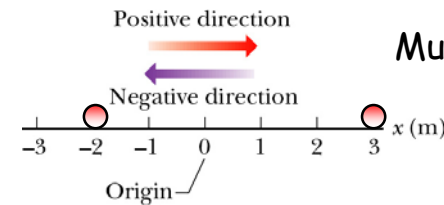


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Displacement Along a Straight Line



Must define: $t = 0$



Displacement:

$$\Delta x = x_2 - x_1$$

$$x_1 = 3 \text{ m}$$

$$x_2 = -2 \text{ m}$$

$$\Delta x = -5 \text{ m}$$

Displacement is a change of position in time.

It is a **vector** quantity.

It has both a **direction** and **magnitude**.

It has units of [Length]: *meters*.

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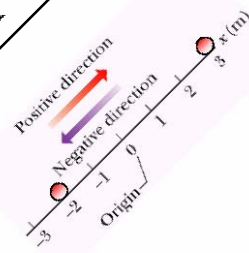
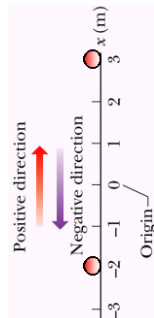
Displacement Along a Straight Line

$t=0$; (start the clock) $x = 0$; (origin)

$x(t=0)$ does not have to be 0

Straight line can be oriented

Horizontal, vertical, or at some angle

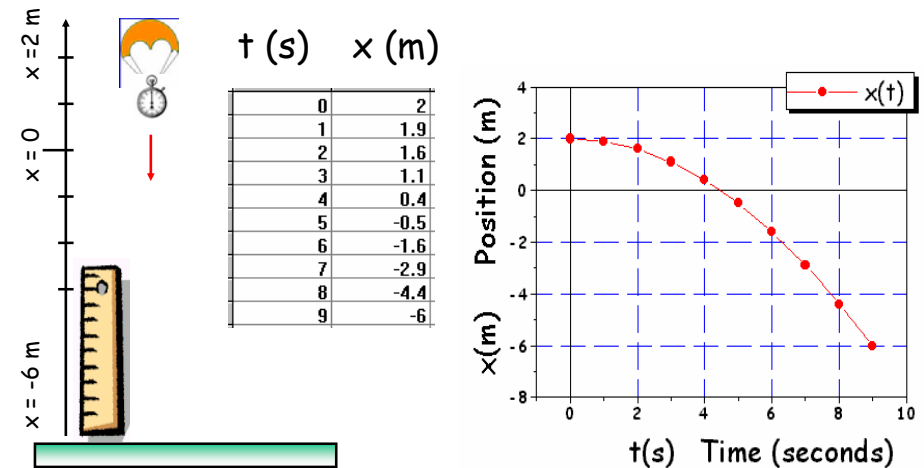


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Displacement Along a Straight Line



Motion with respect to the origin !

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Displacement

Displacement in time:

$$\Delta t = t_2 - t_1$$

Displacement in Space:

$$\Delta x = x(t_2) - x(t_1)$$

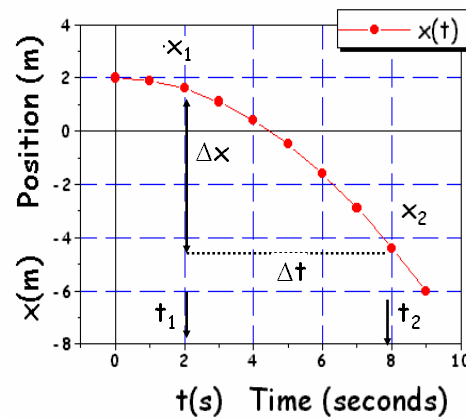
or

$$\Delta x = x_2 - x_1$$

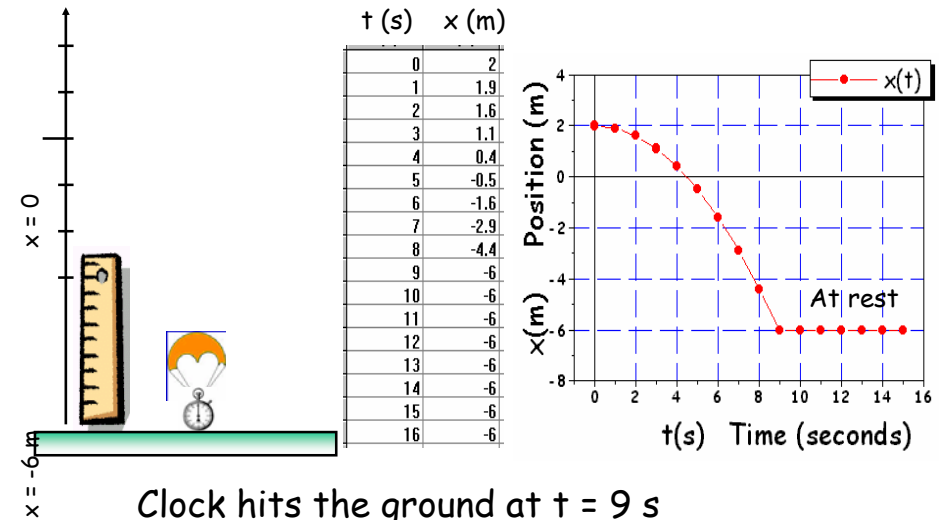
Avg:

$$x(t_2) - x(t_1)$$

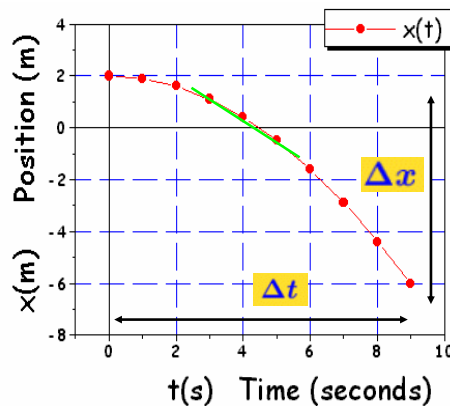
is negative



Displacement Along a Straight Line



Velocity



Average velocity

$$v_{\text{avg}} = \frac{\Delta x}{\Delta t} = \frac{x_2 - x_1}{t_2 - t_1} = -8/9 \text{ m/s} \approx -0.9 \text{ m/s}$$

Average speed

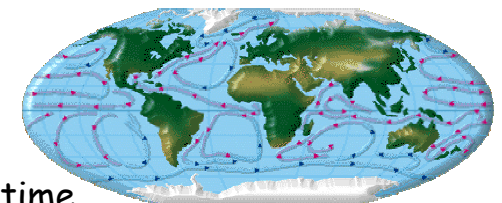
$$s_{\text{avg}} = \frac{\text{total distance}}{\Delta t} = 8/9 \text{ m/s} \approx 0.9 \text{ m/s}$$

Instantaneous velocity

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \frac{dx}{dt}$$

Velocity is the rate of change of position

Velocity is a vector !

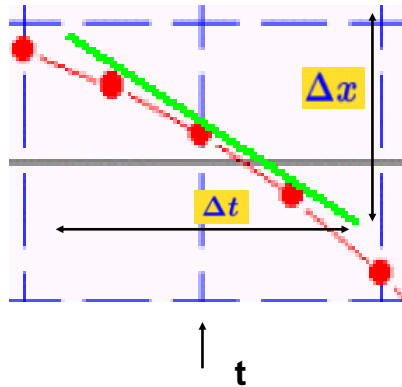


Velocity has direction !

Velocity can change with time

Instantaneous Velocity

Consider smaller time intervals:



Instantaneous velocity $v(t)$ is the slope of the tangent line to $x(t)$

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \frac{dx}{dt}$$

changes with time !

$v(t)$ is a function of time !

Velocity

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \frac{dx}{dt}$$

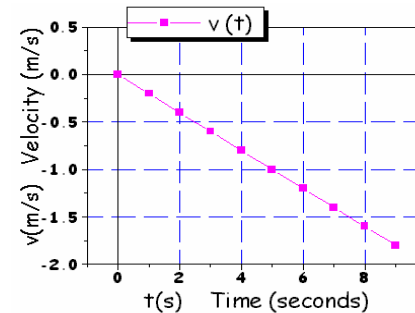
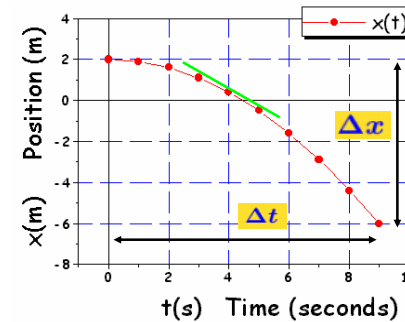
Example of negative v

Velocity is positive in the same direction as x is positive

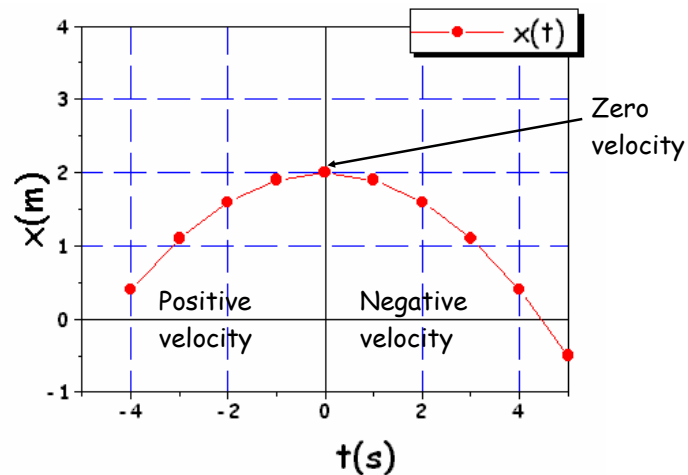
Example of a constant acceleration:

$$v(t) = at$$

$v(t)$ is a straight line

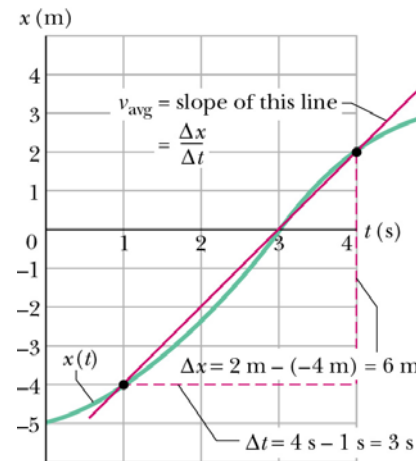


Sign of velocity



$v(t)$ is a function of time !

Velocity



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"moving armadillo"

- Average velocity

$$v_{avg} = \frac{\Delta x}{\Delta t} = \frac{x_2 - x_1}{t_2 - t_1} = 6/3 \text{ m/s}$$

- Average speed

$$s_{avg} = \frac{\text{total distance}}{\Delta t} = 6/3 \text{ m/s}$$

- Instantaneous velocity

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \frac{dx}{dt}$$

Acceleration

- Average acceleration

$$a_{\text{avg}} = \frac{v_2 - v_1}{t_2 - t_1} = \frac{\Delta v}{\Delta t}$$

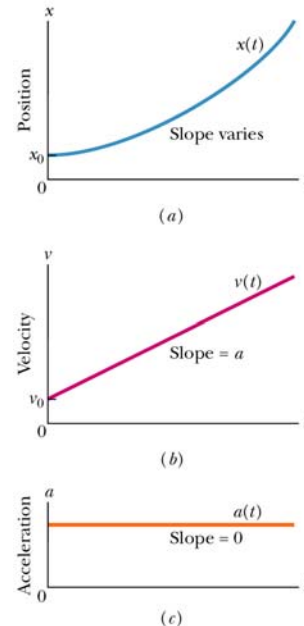
- Instantaneous acceleration

$$a = \frac{dv}{dt}$$

- Constant acceleration

$$v = v_0 + at$$

$$x - x_0 = v_0 t + \frac{1}{2} at^2$$



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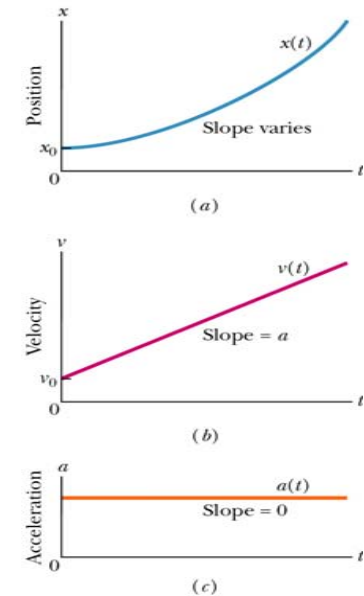
Constant Acceleration

$$(a > 0)$$

$$v(t) = v_0 + at;$$

$$x(t) - x_0 = v_0 t + at^2/2$$

$$x(t) - x_0 = (v(t)^2 - v_0^2)/2a$$



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Kinematic Variables

Position is a function of time: $x = x(t)$

Velocity is the rate of change of the position

Acceleration is the rate of change of the velocity

$$v(t) = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \frac{dx}{dt}$$

$$a(t) = \lim_{\Delta t \rightarrow 0} \frac{\Delta v}{\Delta t} = \frac{dv}{dt}$$

Position $\xrightarrow{\frac{d}{dt}}$ Velocity $\xrightarrow{\frac{d}{dt}}$ Acceleration

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What does zero mean ?

- $t = 0$ beginning of the process
- $x = 0$ is arbitrary; can set where you want it
- $x_0 = x(t=0)$; position at $t=0$; do not mix with the origin

- $v(t) = 0$ x does not change $x(t) - x_0 = 0$
- $v_0 = 0$ $v(t) = at$; $x(t) - x_0 = at^2/2$
- $a = 0$ $v(t) = v_0$; $x(t) - x_0 = v_0 t$

- $a \neq 0$ $v(t) = v_0 + at$; $x(t) - x_0 = v_0 t + at^2/2$
- help: $t = (v - v_0)/a$ $x - x_0 = \frac{1}{2}(v^2 - v_0^2)/a$
- $a = (v - v_0)/t$ $x - x_0 = \frac{1}{2}(v + v_0)t$

- Acceleration and velocity are positive in the same direction as displacement is positive

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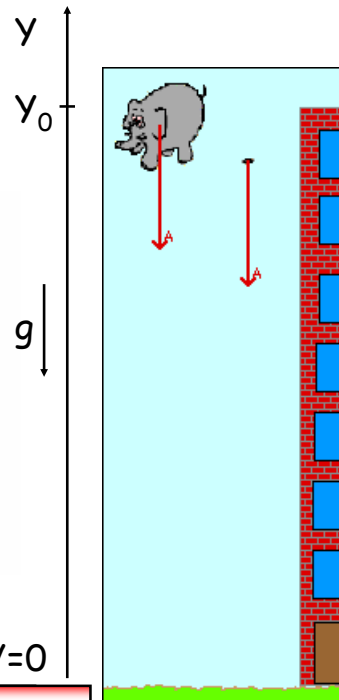
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Free Fall

Most important case of constant acceleration: Free fall

$$a = -g \quad \text{where } g = 9.8 \text{ m/s}^2$$

(defining "up" as the positive direction)



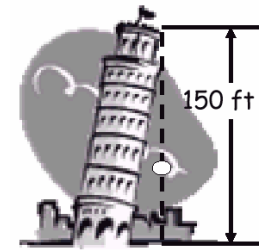
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$y=0$

Gravitation is universal

Gravitational acceleration does not depend on the nature of the material or the mass of the object.



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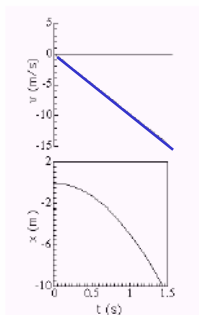
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Three cases of free fall

$$x(t) = x_0 + v_0 t + \frac{1}{2}(-g)t^2$$

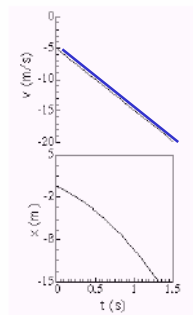
$$v(t) = v_0 + (-g)t$$

$v_0 = 0$



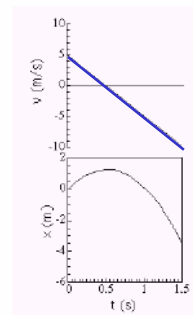
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$v_0 < 0$



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$v_0 > 0$



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Sample Problem II-2

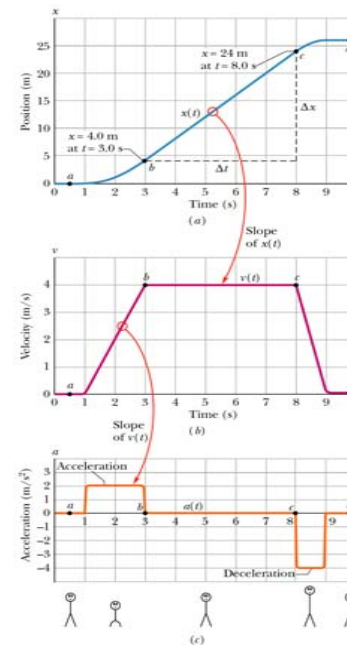
p. 18

An elevator is initially stationary, then moves upward (which we take the positive direction of x), and then stops. Plot V as a function of time.

(a) $x(t)$ curve for an upward moving elevator cab

(b) $v(t)$ curve for the cab. Note $v = dx/dt$!

(c) $a(t)$ curve for the cab. Note $a = dv/dt$!



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<http://webphysics.ph.msstate.edu/>

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Conclusions: Motion along a straight line

- the simplest type of motion
- the groundwork for more complex motion

Kinematical variables in one dimension

Position: $x(t)$ meters

Velocity: $v(t)$ meters/second

Acceleration: $a(t)$ meters/second²

All depend on time

All are **vectors**: have direction and magnitude.

TABLE 2-1 Equations for Motion with Constant Acceleration^a

Equation Number	Equation	Missing Quantity
2-11	$v = v_0 + at$	$x - x_0$
2-15	$x - x_0 = v_0 t + \frac{1}{2}at^2$	v
2-16	$v^2 = v_0^2 + 2a(x - x_0)$	t
2-17	$x - x_0 = \frac{1}{2}(v_0 + v)t$	a
2-18	$x - x_0 = vt - \frac{1}{2}at^2$	v_0

^a Make sure that the **acceleration** is indeed constant before using the equations in this table.

Next Lecture: Motion in 2D and 3D + Vectors

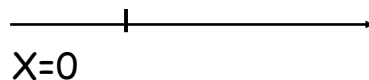
One dimension (1D)

Position: $x(t)$ m

Velocity: $v(t)$ m/s

Acceleration: $a(t)$ m/s²

All are **vectors**: have direction and magnitude.

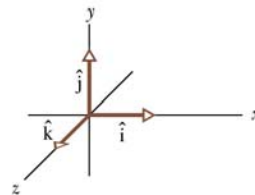


Three dimension (2D)

Position: $\vec{r}(t)$ m

Velocity: $\vec{v}(t)$ m/s

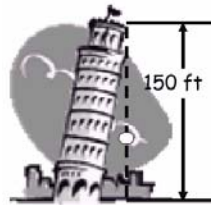
Acceleration: $\vec{a}(t)$ m/s²



Lecture QZ2

A rock is dropped from the height of 150 ft with no initial velocity. What is the rock's **speed** after the first 2 seconds. (Neglect the air resistance).

Hint: The free fall acceleration $g = 9.8 \text{ m/s}^2$
(150 ft \rightarrow ? meters)



Homework:

- Utexas