



Conditions for Equilibrium

An object at equilibrium has no net influences to cause it to move, either in translation (linear motion) or rotation. The basic conditions for equilibrium are:



Equilibrium

Balance of Forces:





 $\vec{P}=0$

- 1. The vector sum of all the external forces that act on the body must be zero.
- 2. The vector sum of all the external torques that act on the body, measured about any possible point, must be zero.
- 3. The linear momentum \underline{P} of the body must be zero.
- 4. The gravitational force \underline{F}_g on a body effectively acts on a single point, called the center of gravity (cog) of the body. If g is the same for all elements of the body, then the body's cog is coincident with the body's center of mass.

Equilibrium inside a Star



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8

Equilibrium of the tower of Piza Static Equilibrium $\vec{P}=0$ Balance of Forces: Balance of Torques: Is it really stable? The Leaning Tower of Piza $ec{F}_{ m net} = rac{dec{P}}{dt} = 0$ $ec{ au_{ m net}}=rac{dec{L}}{dt}=0$ Back to Eq. Stable vs. Unstable $ec{F}_{ m net} = rac{dec{P}}{dt} = 0$ Static Equilibrium N An equilibrium point is stable if small changes in the position lead to mg restoring forces back to equilibrium. mg Away from Eq. If it moves away from the equilibrium $ec{ au_{ m net}}=rac{dec{L}}{dt}=0$ point when displaced slightly, it is unstable. mg \mathbf{mg}_{10} Andrei Sirenko, NJIT Andrei Sirenko, NJIT 10/24/2006 9 10/24/2006

Equilibrium for fun





Unstable Equil.



Stable Equil.

11

Equilibrium for fun







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Sample Problem XIII – 1



A uniform beam of length L and mass m = 1.8 kg is at rest with its ends on two scales. A uniform block with mass M = 2.7 kg is at rest on the beam, with its center a distance L/4 from the beam's left end. What do the scales read?

15

10/24/2006



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16



Sample Problem XIII – 2



Cabl

(a)

10/24/2006

A ladder of length L = 12 m and mass m = 45 kg leans against a slick (frictionless) wall. Its upper end is at height h = 9.3 m above the pavement on which the lower end rests (the pavement is not frictionless). The ladder's center of mass is L/3 from the lower end. A firefighter of mass M = 72 kg climbs the ladder until her center of mass is L/2 from the lower end. What the are the magnitudes of the forces of the ladder from the wall and the pavement? Andrei Sirenko, NJIT 18



Sample Problem XIII – 3

A safe of mass M = 430 kg is hanging by a rope from a boom with dimensions a = 1.9 m and b = 2.5 m. The boom consists of a hinged beam and a horizontal cable that connects the beam to a wall. The uniform beam has a mass m = 85 kg. The masses of the cable and the rope are negligible.

- a) What are the tension T_c in the cable? In other words, what is the magnitude of the force \underline{T}_c on the beam from the cable?
- b) Find the magnitude *F* of the net force on the beam from the hinge.

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QZ#8 m=5kg d=2m

•Show all forces acting on the beam. Mass of the beam is zero

•Write the force and torque balances

•Calculate M to keep the whole system in equilibrium





Sample Problem XIII – 4

A rock climber with mass m = 55kg rests during a "chimney climb", pressing only with her shoulders and feet against the walls of a fissure of width w = 1.0 m. Her center of mass is is a horizontal distance d = 0.2 m from the wall against which her shoulders are pressed. The coefficient of static friction between her shoes and the wall is $\mu_1 = 1.1$, and between her shoulders and the wall it is $\mu_2 = 0.7$. To rest, the climber wants to minimize her horizontal push on the walls. The minimum occurs when her feet and her shoulders are on the verge of sliding. 10/24/2006



- a) What is the minimum horizontal push on the walls?
- b) For that push, what must be the vertical distance h between her feet and her shoulders if she is to be stable?

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23