# Distance based phylogeny reconstruction 

Usman Roshan

## Neighbor joining

1. Additive and $O\left(n^{\wedge} 3\right)$ time
2. Initialization: same as UPGMA
3. For each species compute

$$
u_{i}=\frac{\sum_{k=1, k \neq i}^{n} d_{i k}}{n-2}
$$

4. Select $i$ and $j$ for which $d_{i j}-\left(u_{i}+u_{j}\right)$ is minimum
5. Make them neighbors in the tree by adding new node (ij), and set tree distance from (ij) to $i$ and $j$ as

$$
d_{i,(i j)}=\frac{1}{2} d_{i, j}+\frac{1}{2}\left(u_{i}-u_{j}\right) \quad d_{j,(i j)}=\frac{1}{2} d_{i, j}+\frac{1}{2}\left(u_{j}-u_{i}\right)
$$

## Neighbor joining

6. Update distance matrix $d$ : for all clusters $k$ do the following

$$
d_{(i j), k}=\frac{d_{i k}+d_{j k}-d_{i j}}{2}
$$

7. Delete columns and rows for $i$ and $j$ in $d$ and add new ones corresponding to cluster (ij) with distances as computed above
8. Go to 3 until two nodes/clusters are left

## NJ

NJ constructs the correct tree for additive matrices


## Neighbor joining implementation in Python

- Instead of -1 to denote unusable entries of d we will use ' $X$ '. For this we make changes to
- Find_closest_pair
- Update_distance_matrix
- Make_little_d


# Neighbor joining implementation in Python 

- We also need to modify the functions below to reflect neighbor joining updates
- Find_closest_pair
- Update_distance_matrix
- Distance

