

## Naïve Bayes algorithm

### Input:

1. Data matrix of dimension  $n$  by  $m$  ( $n$  rows and  $m$  columns)
2. Training labels  $L$ . Each label  $l_i$  is an integer indicating the class that row  $i$  belongs to.

### Algorithm:

1. Training:
  - a. Initialize the mean  $m_j$  of each class to the vector of all 1's (not 0's). These are pseudocounts to avoid zero variance.
  - b. Compute mean  $m_j$  of each class by adding each datapoint to  $m_j$  and dividing by number of datapoints
2. Prediction: Assign point  $x'_i$  to class  $j$  if  $x'_i$  is closest to the mean of class  $j$  normalized by standard deviation. In other words

$$class(x'_i) = \underset{j}{\operatorname{argmin}} \sum_{k=1}^m \left( \frac{x'_{ik} - m_{jk}}{s_{jk}} \right)^2$$

where  $s_{jk}$  is the standard deviation of the  $k^{\text{th}}$  feature (dimension) of class  $j$  and  $m_{jk}$  and  $x'_{ik}$  are the  $k^{\text{th}}$  entry (dimension) of the vectors  $x'_i$  and  $m_j$  respectively.