

GOOGLE SEARCH ENGINE ARCHITECTURE

1998@Stanford

Paper L1 (pdf is long article, html shorter version) and 4.2.1 (Heaps' Law)

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Google in 1998

General Statistics

The main statistics of the Google Search Engine Architecture in its original incarnation at Stanford can be summarized in the stats available in Figure 1. Google's view of the Web was a paltry 25M pages of total size 147GiB uncompressed (zlib compressed down to 53GiB), index size was approximately 60GiB. Thus the index is slightly larger than the compressed Corpus. Of those 60GiB of the index roughly two-thirds or 41GiB was the size of the inverted index and the remainder the size of other index-related data structures. As a point of reference in 2015, approximately 1T URLs are crawled, around 30G pages indexed, and roughly 6G queries are satisfied daily (two-thirds of them just by Google).

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A. Google's Search Engine Performance in 1998@Stanford
  Active crawlers      : 3-4 typically with 300 open connections/crawler
  Web-page read        : 100/sec concurrently, 600KiB/sec
B. Google@Stanford size statistics
  # of Web pages       : 25M                                     25M Web-pages
  # Crawling (New)     : 9 days per crawl for 25M pages, 50pages/sec
  # Crawling (Existing) : 63hrs for 11M preexisting pages
  # of URLs/WebServers : 76M URLs and 500,000 Web Servers
  # of Email addresses : 1.7M Email addresses and 1.6M 404 messages
C. Google Indexer Performance
  Indexer Speed        : 54 pages/second, 2-4weeks total
  Sorter Speed         : 24 hours on 4 PCs
  PageRank             : < 1 day
D. Google Query Speed  : 1-10 seconds/query, 1K/day
E. Data Collected from Web-pages
  Link Data            : fromURL, toURL, anchor-text
                       : [25M URLs, 260M anchors, 322M links]
  Short Barrel (4GiB)  : [title and anchor text only]
  Long Barrel (37GiB)  : [all]
F. Google Index Data
  Fetched Information   : 147GiB                                  ~150GB or 150GiB size/Corpus
  Compressed           : 53GiB (3 to 1)                          [or ~ 6000B /Web-page]
  Inverted Index Full   : 41GiB                                   [or ~ 1000 words/Web-page]
    Short Barrel       : 4GiB
    Long Barrel        : 37GiB
  Anchors              : 6.6GiB [260M]
  Links                : 3.9GiB
  Lexicon              : .3GiB [14M words]
  DocIndex             : 9.7GiB
G. Source: Brin & Page [ http://www-db.stanford.edu/~backrub/google.html ]
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Figure 1: Google Search Engine 1998

Gentler Reminder. Note that B stands for byte, bit for bit, b for nothing/nonsense. 1MB may be 1,000,000B if it denotes hard-disk drive capacity and 1,048,576B of main memory. Use SI's 1MiB for 1,048,576B i.e 2^{20} B or 1GiB, 1TiB, 1PiB instead!

1.1 Corpus size (Google@1998) and URLs. In Google@1998, the corpus was 25M web-pages and approximately 80M URLs. The cumulative size of the web-pages was 150GiB uncompressed, roughly 50GiB compressed; overall index size (all data structures) was 64GiB.

1.2. Performance (Google@1998). Google's crawler used to crawl on the average 50pages/sec and fetch all 25 million pages in roughly 9 days. The indexer and sorter used to index 54pages/sec sustained over a 24 hour period using only 4 workstations. The PageRank computation could be completed in less than a day.

1.3. Link information (Google@1998). The 25 million pages included more than 260M anchors that were indexed, and close to 520M hyperlinks (some might point to inside a given page) with a total of 322M links stored in the Links structures of Google (to be explained).

Google@1998: Search, sort, and select.

1.4.1 Search. Google's first action was to **search** i.e. **crawl** the web, locate 500K web-servers containing 25M pages and fetch those pages at rates ranging from 50pages/sec, to 100pages/sec for the 3-4 instances of a crawler running at any time. Such a task could be completed in less than 2 weeks (9 days) from scratch or in less than 3 days if preexisting (known) pages were to be refetched.

1.4.2 Sort. The **indexing process** in Google is realized by the **indexer** and the **sorter**. The indexer deals with parsing pages and generating the forward index at a speed of 54pages/sec in 1998 completing its task in roughly 2-4 weeks. The sorter then inverts the forward index using **sorting** to generate the inverted index i.e. the **index** in 24 hours using 4PCs.

1.4.3 Select. The **selection** procedure requires the actions of the **query engine** or what is known in Google terminology (see bottom right of Figure 2) as the **searcher**.

The crawler was implemented in Python but the indexer mainly in C and C++.

Search Engines

Google System Architecture Components

The original Google System Architecture is depicted in Figure 2 and its major components are highlighted below. A component is a program (oval) or data structure (rectangle).

- 2.1 URL server. Provides a list of URLs to be sent to and retrieved by the crawler.
- 2.2 Crawler. A distributed crawler is used with 3-4 instances running at any time (in 1998-2000).
- 2.3 StoreServer. Compresses Web-pages (using zlib) and then stores them into the
- 2.4 Repository, that holds all retrieved pages. The indexer can use the Repository and the error log of the Crawler to restore the index.
- 2.5 Indexer. Parses documents and generates Google's index.
- 2.6 Anchors. Contains a list of (possibly relative) URLs retrieved by the Indexer.
- 2.7 URLresolver. Converts Anchors-related data into absolute URLs and uses this information to generate the
- 2.8 Links, data that show how URLs reference each other (i.e. depict the link structure of the Web).
- 2.9 Lexicon. Contains a list of unique words found (14million, 256MBytes of data in 2000). Resides in main memory (and the size of the main memory determines its size).
- 2.10 DocIndex. Contains information about documents. Every document has a docID which is a hash of its contents, a pointer to its location to the Repository along with other useful information (eg. URL and title).
- 2.11 Barrels. Contain all hitlists generated by the indexer from the Repository. Google originally used 64 Barrels, one barrel for a group of consecutive words. It contains information about hits i.e. is an inverted index of all words in all documents (every word records also positional, font and TITLE/ANCHOR relative indexing information).
- 2.12 Sorter. It's the program that sorts the Barrels based on word (actually wordID) to generate the hitlists.
- 2.13 PageRank. It's the ranking method used by Google to rank documents based on "popularity". Such information is based solely on the graph structure available in Links.
- 2.14 Searcher. It's the search interface for Google. It parses queries, converts them into a form google understands (e.g. converts words into wordIDs using the Lexicon), accesses the Barrels to determine the documents. The ranking of the output documents is a combination of PageRank and an evaluation of the results of the hits according to the query.

Search Engines Google System Architecture

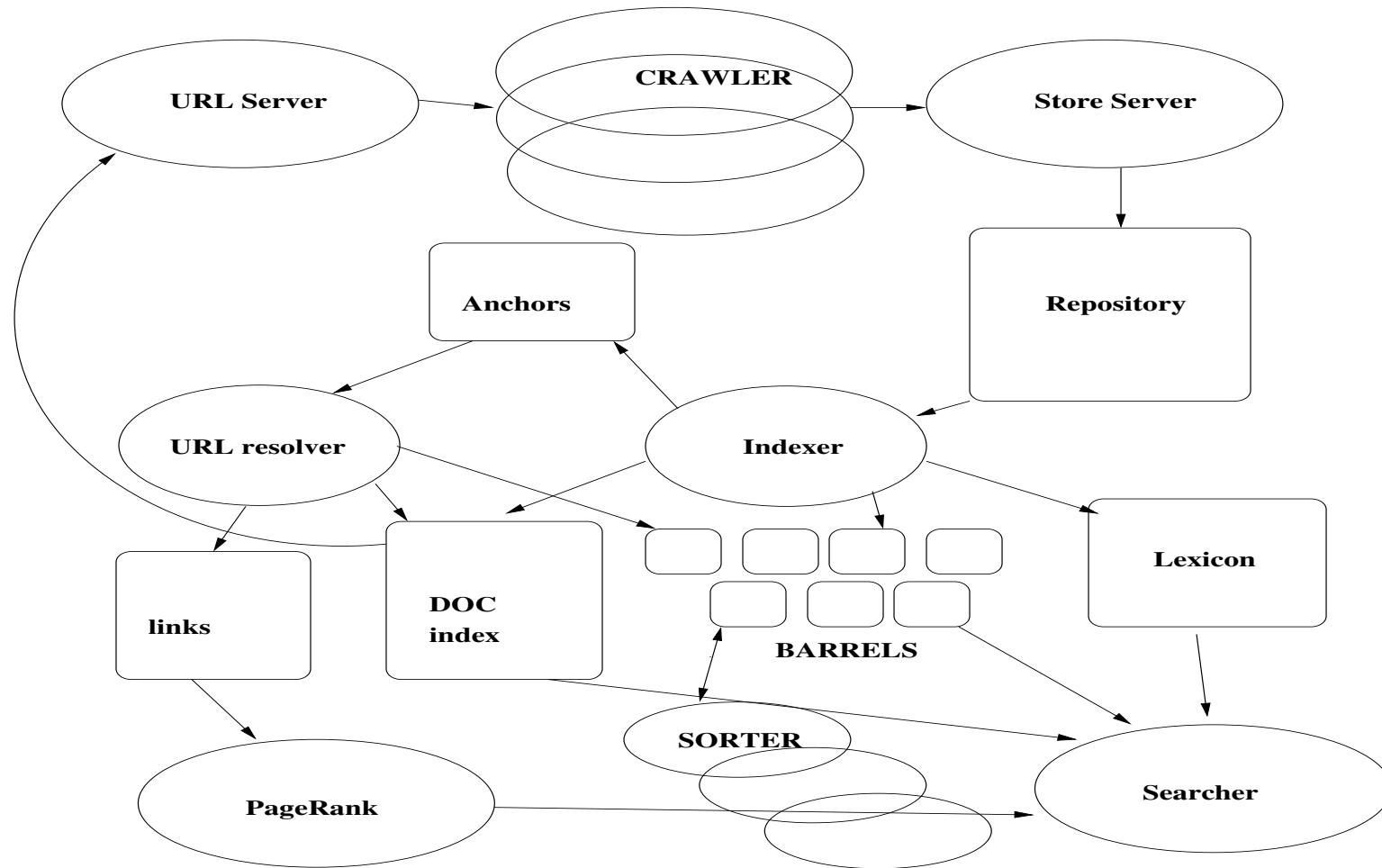


Figure 2: Google System Architecture.

2.1-2.4: URL Server, Crawler, StoreServer, Repository

2.1. URLserver. The URL server maintains lists of URLs in a data structure known as DOC Index, that were obtained in previous runs of the crawler. In subsequent runs, it is the URLserver that schedules what a crawler is going to crawl: it sends lists of URLs to the active instances of the crawler (3-4 active ones at a time in 1997/1998). The URLserver is implemented in Python. The URLserver maintains metadata (data on the "data"/URLs) on these URLs (eg. last time fetched, etc).

ACTION 2.1 (URLserver). The URL server supplies lists of URLs to the crawler(s).

2.2. Crawler. Google's crawler (1998 edition) is a distributed one written mainly in Python, with 3-4 instances of it running at any time, maintaining 300 connections and using a visit policy based on Depth First Search (DFS). In 9 days it could crawl and visit roughly 26M arbitrary pages though it could visit and fetch 11M preexisting pages in 63 hours at a rate of 100pages/sec for the 3-4 instances. The 25M pages indexed at the time included 76M URLs, and 1.7M email addresses. All 4 instances of a crawler could work on 100pages/sec, fetching roughly 600KiB/sec.

ACTION 2.2 (Crawler) The crawler receives lists of URLs from the URLserver and then goes to the Web to visit those pages, fetch its contents, and then sends these pages to the StoreServer. Metadata or other info may be transmitted to the URLserver and subsequently stored by the Storeserver into the Repository.

2.3. StoreServer. The storeserver received pages from the crawler, compresses them using zlib, and stores them into the Repository; metadata (i.e. data on those data) related to them are also stored there. Google made the decision of using zlib (compression ratio of 3 to 1) over bzip (ratio of 4 to 1) based on speed considerations than compression performance.

ACTION 2.3 (Storeserver) The Storeserver receives pages from the crawler(s), compresses them and stores them into the Repository.

2.4. Repository. The Repository is a data structure that stores compressed pages received by the Storeserver from the Crawler who fetched them from the Web. They are stored in compressed zlib format in the form of packets that maintain a *docID*; *URL length*; *URL*; *compressed page size*; *raw compressed page*. Such pages are then made available to the Indexer. (**Action 2.4.**)

ACTION 2.4 (Repository) The Repository is only written by the Storeserver and read primarily by the Indexer during the indexing process. All of Google's index can be built from information stored in the Repository, without the Indexer accessing the Web or interacting with the crawler; the error log of the crawler is only used to discard incomplete pages that were not fetched due to errors.

Google Search Engine Architecture

Indexing Process: Indexer, Sorter and Barrels

INDEXING PROCESS: The **2.5 Indexer** and the **2.12 Sorter**. The indexing process in Google@1998 includes the indexing functions performed by the (a) the **Indexer**, and (b) the **Sorter**. Through ACTION 2.4 the Indexer first reads and decompresses pages from the Repository, and using the Error Log of the crawler to discard incomplete pages then generates the forward index. The forward index is a list of hits (i.e. a hitlist), with a hit being an occurrence of a word in a document. A partially sorted forward index is thus generated by the Indexer into a data structure known as Barrels (there are long and short Barrels). Subsequently the Sorter would read the Barrels and invert (i.e sort) the forward index to generate the (inverted) index also stored into the Barrels. Auxiliary functions are being performed by the URL resolver and PageRank, with the latter ranking links (aka resolved pairs of URLs); several other data structures are maintained.

2.5 Indexer. The indexer performs two actions:

- (a) **ACTION 2.5.1: forward-index generation** stored into the long and short BARRELS using as input the Error Log of the crawler, and the data in the Repository; these are the only two sources from which the Indexer accepts input and this action creates/populates a variety of other structures including the Lexicon and Doc Index, and
- (b) **ACTION 2.5.2: Anchor creation** using the text information parsed and extracted from inside web-pages.

Action 2.5.1:Forward Index. The indexer through ACTION 2.4

- i. reads a compressed web-page (document) and its metadata from the Repository,
- ii. uncompresses and parses it, and
- iii. generates the forward index that is a collection of hits (in hitlists) i.e. tuples that include **word-parsed**, **word-offset in doc**, **capitalization**, **fontsize**, **context/location**, and
- iv. then assigns those hits to the (a) the **short barrels** that deal with words appearing in the **title**, **meta** tags of an HTML document, or the URL, or the **anchor** text that points to another document (known as **fancy hits** of the short barrels), and (b) the **long/full barrels** that deal with words appearing everywhere (including the title and anchor related text).

The **Forward index** is partially ordered (by offset and maybe docID).

ACTION 2.5.1 continued: A **hitlist** consists of **hits**. A hit is a single **word occurrence** in a document; a document is thus converted into a sequence of word occurrences i.e. tuples $\langle \text{docID}, \text{wordID}, \text{offset}, \text{Info} \rangle$

In a hitlist a hit count precedes list of hits; a hit is 2B with an Info field for the fontsize of the word, its capitalization, context such as whether it is in the title of a document, in the anchor, it is emphasized, of higher font size, etc. **The hitlists form a partially sorted forward index**; for a given document (docID) its tuples are ordered by **offset**.

There are two types of hits: (a) **fancy hits** and (b) **plain hits**. A *fancy hit* is for words appearing in title, meta, and anchor tags or in the URL. 1 bit is used to indicate capitalization, 3 bits are set to the pattern 111 indicative of a fancy hit, 4 bits to indicate the type of a fancy hit, and 8 bits are being used to either indicate offset information (normal) or anchor-related information: in the latter case 4 bits are indicative of offset in the anchor text and the remaining 4 bits is a 4-bit hash of the docID containing the anchor/text. *Plain hits* use 1 bit for capitalization, 3 bits for fontsize encoding relative to the fontsize of the rest of the document (7 states are used; state 111 indicates a fancy hit), and 12 bits for a word offset (value 4095 is for offsets > 4095). *In a hit-list a hit count that precedes the list of hits is either 5 bits or 8 bits depending on whether it is available in the inverted index (combined with a docID) or the forward index (combined with a wordID) for a total of 32bits.*

ACTION 2.5.2: Anchors. The **second action** of the indexer is to parse out all links (anchors) of every page and store them into **Anchors**. If page p has a full or partial URL associated to page u , **Anchors** will include the full URL of p , the full or partial URL of u and the anchor text in p associated with u though! Thus a tuple of the form

$\langle \text{fromURLof_}p, \text{toURLof_}u, \text{AnchorTextin}p\text{Associatedwith_}u \rangle$ is stored in **Anchors**. Moreover the URL resolver will store into the short barrels for document $\text{toURLof_}u$ the $\text{AnchorTextin}p\text{AssociatedWith_}u$ as described in ACTION 2.7.2 later.

URL, URLsum, docID, word, wordID. Every URL has a checksum (hash) which is a fingerprint of the URL (a "shorter and simpler" identifier of it). A 0-1024 characters long URL has a 16-32B fixed length checksum: URLsum. An even shorter docID (4-8B) is associated with the URL and URLsum. A mapping of URL, URLsum, docID is maintained in the index. The docID is assigned to a URL by the URLresolver. Note that the Indexer stores full or partial URL in **Anchors**; the URL resolver resolves the full path of the URL stores that finalized information in the DOC index. Likewise for every word of arbitrary length a shorter wordID (say 3-4B) is maintained. The mapping between the two is available in the Lexicon.

2.12 Sorter: Inversion and (Inverted) Index.

The Sorter takes information from the barrels (short or long/full) in the form of a partially sorted **forward index** and sorts this information. The sorting is by **wordID**, first, then for a given **wordID** by **docID** and then for a given **wordID,docID** pair by **offset**. This sorting operation is known as **inversion**. The output of this inversion is stored back into the barrels in the form of an **(inverted) index**. The Sorter also generates a list of **wordIDs**. Thus both the input and the output of the sorter is available in the barrels. (Figure 2 shows the Sorter connected to the barrels only.)

ACTION 2.12.1 : Inversion. The sorter uses the forward index of the Barrels as input to invert it (sort it) and the output of this inversion is the (inverted) index also stored into the Barrels.

ACTION 2.12.2 : List of wordID. The sorter generates also a list of **wordIDs** as an output of the inversion process.

2.11 Barrels. There are 64 Barrels (short or long). Data associated with long barrels is 10 times larger than those of short barrels. The forward index is distributed over those 64 barrels. Each barrel stores a range of **wordIDs**. For **wordIDs** in a given barrel we don't need to store all the bits of the **wordID** but only an offset from the first **wordID** stored in that barrel (thus shaving off 6bits).

2.11.1 Forward Index in Barrels. For a given document, the forward index contains multiple variable-length tuples. A tuple will contain a **docID** to identify the current document, followed by multiple entries i.e. hitlists that consist of a **wordID** to identify the word whose hits will be recorded, an **nhits** record (8 bits) that will record the number of occurrences of the word in **docID** followed by a variable length array of **nhits** entries; since a hit is 2B long, the length of the hitlist is **nhits*2+4** bytes including the **wordID**. The last tuple for a given **docID** records a **NULL** for a **wordID** to indicate the end of the for the given **docID**. Information related to the next **docID** is then made available.

2.11.2 (Inverted) Index in Barrels. The same barrels that store the forward index store the (inverted) index except that in the latter the tuples are sorted by **wordID**. The Lexicon records for a given **wordID** the number of documents **ndocs** that contain it. A pointer to the barrel(s), long or short, is also available. This pointer points to an area of **ndocs** consecutive variable length records. Each such record is a tuple containing a **docID**, the document containing that word, an **nhits** field (5bits) that records the number of occurrences within **docID** of **wordID**, followed by a variable length record recording say **nhits**. The length of this record is **nhits*2+4** bytes (including the **docID**).

Google Search Engine Architecture

Indexing Process: Anchors, URL Resolver and Links

2.6 Anchors and

2.7. URL Resolver.

During the indexing process and ACTION 2.5.2 the **Indexer** creates and populates the **ANCHORS** data structure. This data structure is being read by the URL Resolver. The URL Resolver (i) converts a partial or relative URL into an absolute URL, and then (ii) absolute URLs into docIDs.

ACTION 2.7.1.: Absolute URL and docID conversion. The URL resolver reads **Anchors** and converts a partial or relative URL into an absolute URL. Absolute URL with no docID are assigned one. This information is maintained in the DOC index.

ACTION 2.7.2.: Short Barrel Update. As previously explained in ACTION 2.5.2 of the INDEXER, for a document p that has an anchor link to document u , the INDEXER extracts the text **AnchorTextinAssociatedwith_u** and forms tuple $\langle \text{fromURLof_p}, \text{toURLof_u}, \text{AnchorTextAssociatedwith_u} \rangle$ stored in **Anchors**. In this ACTION 2.7.2 the URL resolver retrieves the tuple from the **Anchors** and stores the text **AnchorTextinAssociatedwith_u** associated with the resolved docID_u of toURLof_u into the short barrels. Thus the text is associated with the link it points to, not the document that contained it. Given that barrels contain docIDs and never URLs, it is the job of the URL resolver to provide docIDs as needed, a result of prior ACTION 2.7.1.

ACTION 2.7.3: Links. As explained in ACTION 2.5.2, the URL resolver read **ANCHORS** and converts a $\langle \text{fromURLof_p}, \text{toURLof_u}, \text{AnchorTextinAssociatedwith_u} \rangle$ into a pair of docIDs that will be stored into **Links**: $\langle \text{docID_p}, \text{docID_u} \rangle$.

ACTION 2.7.4: URLs with no docID. Periodically, the URL resolver merges a list of URLs that have not been assigned a docID with the list of URLs that have been assigned a docID. This latter file is File3 maintained by DOC index.

2.8. Links. It stores pairs of docIDs (not URLs) generated by the URL resolver through ACTION 2.7.3

The motivation behind the data structures used by Google is to reduce disk accesses since all of the information maintained by the Index can not (or could not) be stored into main memory. Whether it is 1990 or 2010, one disc access still takes 8-10msecs i.e. it is slow.

2.9 Lexicon. The lexicon is maintained so that it fits into main memory. Its size is thus kept small by not maintaining rare words in main memory. Google's lexicon in 1998 used to maintain in main memory roughly 14 million words. Rare words are attached to the lexicon and maintained in a separate disk file, not in main memory. The lexicon is organized as a **hash table** of pointers to a list of words separated by nulls (i.e. `\0` in Unix/C parlance). The indexer generates lists of words (or wordIDs) through the lexicon, and the sorter creates a new one list of wordID as a result of the inversion operation. The merging of these two lists is undertaken by the SEARCHER and generates a new lexicon. Moreover, the lexicon for a given wordID maintains the number of ndocs that contain the wordID and a pointer to the barrel(s).

2.9.1 Heaps' Law. This empirical law states that for a corpus containing W words, the number of distinct words t forming its dictionary/vocabulary/lexicon can be approximated by a formula

$$t = kW^\beta$$

wher β varies between 0.4 and 0.6 and a typical value if $\beta = 0.5$, and k is a constant that varies between 10 and 100.

Example. For a text with 16 billion words, $k = 100$, $\beta = 1/2$, and thus $t = 100\sqrt{W}$ we obtain a $t = 14,000,000$.

Google Search Engine Architecture

Indexing Process: Doc Index, PageRank, BigFiles

2.10 DocIndex. The DocIndex contains information about documents (web-pages) in fixed width and length (ISAM for Indexed Sequential Access Method). The information is indexed by **docID**.

File1 in DocIndex. It includes for each document its **docID**, current status information, a pointer to the Repository for the document, a document checksum and other statistics and a pointer to either **File2**, if the document has been crawled, or **File4**, if it has not been crawled.

File2 in DocIndex (for crawled pages). This is also known as **docinfo**. File2 is a variable width file and contains URL and title information for the document of File1 pointing to this location of File2. This is because in File1, for a crawled web-page a pointer to this File2 exists.

File3 in Doc Index. This contains all URL that have been assigned a **docID**. It's a fixed width file: a entry is the URL checksum i.e. URLsum of the URL and the corresponding docID. File3 is sorted by the URLsum. Thus if we have a URL and we want to determine its docID, we first convert the URL into a URLsum and then do a binary search of the URLsum to retrieve and thus determine the docID associated with the URLsum. The URL resolver periodically merges this sorted by URL checksum file with a list of URLs whose docID is to be computed.

File4 in DocIndex (for non-crawled pages). File1 has a pointer to File4 if it relates to a non crawled page. For a non-crawled page there is not title information yet. Thus **File4** is a variable width file and contains URL information only for the document of File1 pointing to this location of File4.

2.13 PageRank. It computes the PageRank number for every docID stored in the Links using the Links information. It will provide this information to the Searcher for the set of documents submitted by the Searcher to PageRank.

BigFiles. It is virtual files spanning multiple disks and filesystems that store Google index-related information (web-pages, indexes, barrels, etc). They use 64-bit addressing.

2.14 Searcher. It is the query engine of Google. It performs a variety of tasks that includes the following ones.

2.14.a Query satisfaction. It uses the Lexicon and the inverted index (stored in the Barrels) to answer queries. Moreover it uses the Lexicon to offer alternatives if it realizes that a search term might have been misspelled.

It is worth noting that the short barrels (fancy hits) are searched before the long barrels (plain hits).

2.14.b Rank results. It uses and retrieves PageRank information to rank results of queries. Given that Barrels store docIDs, the ranks are retrieved through the PageRank interface. (Be reminded that Links store link information of docIDs as well.)

2.14.c Context Information. For the average user, a docID means nothing. The Searcher uses DocIndex to convert a docID back into a URL (File1 and File2 of DOC index), and then using this information from DOC Index (File1), it retrieves the compressed file from the Repository to display readable result information such as the URL not docID, title information of the document (File2 of DOC Index), context information i.e. the text that includes the word occurrence appearing as a search term in the query.

2.14.d ACTION 2.14.1 below. The Searcher performs the merging of information that merges the sorted list of word/wordIDs generated by the Sorter and a list of word/wordID available in the current Lexicon. Even if the merging takes place by the Searcher, it will be the Indexer and NOT the Searcher that will create a new Lexicon from this merged list.

ACTION 2.14.1 : DumpLexicon. The list of wordID/words generated by the Sorter (ACTION 2.12.2) and the current list of wordIDs maintained in the Lexicon by the Indexer are being merged to generate a new Lexicon that is up-to-date. This merging is performed by the Searcher by the new Lexicon is generated by the Indexer.

Google Search Engine Architecture

Search Process: Google Query Evaluation

Google Query Evaluation Steps

1. Parse the query.
2. Convert words into wordIDs.
3. Seek to the start of the doclist in the short barrel
for every word.
 Short Barrel: Title and Anchor text of web-pages
 DocList : For every wordID list of docIDs containing.
4. Scan through the doclists until there is a document
that matches all the search terms.
5. Compute the rank of that document for the query.
6. If we are in the short barrels and at the end of any doclist,
seek to the start of the doclist in the full barrel for every
word and go to step 4.
 Full Barrel : All of the page is indexed
 (10x larger than Short Barrel in 1998).
7. If we are not at the end of any doclist go to step 4.
8. Sort the documents that have matched by rank,
and return the top k.

Source:<http://www-db.stanford.edu/~backrub/google.html>

Figure 3: Google Query Evaluation Process

An example of an information retrieval system is that used by Google. Figure 3 describes the steps undertaken by a Google search engine in answering a query. Although it represents how Google worked in 1998, it is still relevant today. Several steps may have been enhanced and highly optimized since then, but the fundamental underlying operations have little changed.

So far we have given an outline of what web-searching entails and is about. One might ask the following question. If web-searching through a search engine is an information retrieval problem, that has been studied for more than 30 years, what is left to be told about it? Is it an obvious problem or is there something that still needs to be told about it?

For every query q and document d_j Google establishes an information retrieval based valuation that depends on five or so factors that includes title, anchor, URL, large-font and small-font occurrence of a word in the query in the document. Each such factor is assigned a weight (say a number between 0 and 1) and that weight is then multiplied by a count that shows how often the word of the query appears in the document as factored. This determines the information-retrieval based value/rank of the document relative to the query. This becomes in Google parlance the **relevance score** or the similarity $s(q, d_j)$ measure. For the document in hand, its PageRank is also determined let us call it $r(d_j)$. The sum of the two scores/ranks determines the final rank of the document d_j relative to query q and is used to order the results in the form that will be presented to the user: $R(q, d_j) = s(q, d_j) + r(d_j)$.

To be, or not to be, that is the question:
Whether 'tis Nobler in the mind to suffer
The Slings and Arrows of outrageous Fortune

Exercise 1 *Read the paper introduction the Google search engine also available from the following URL.*

<http://www-db.stanford.edu/~backrub/google.html> *Try to answer after reading the paper the following questions whose answers are in the paper or may need to be further searched upon. (a) What was the size of google's dictionary/vocabulary around 1998? Justify your answer. (b) What is the number of bits used for docID? You might need information beyond the paper for that. (c) On the same one page you used for (a), (b) describe the data structures used by google for indexing. (d) Does google (circa 1998) use a hash table for the dictionary? What do they use? Why? What does Google call the dictionary?*