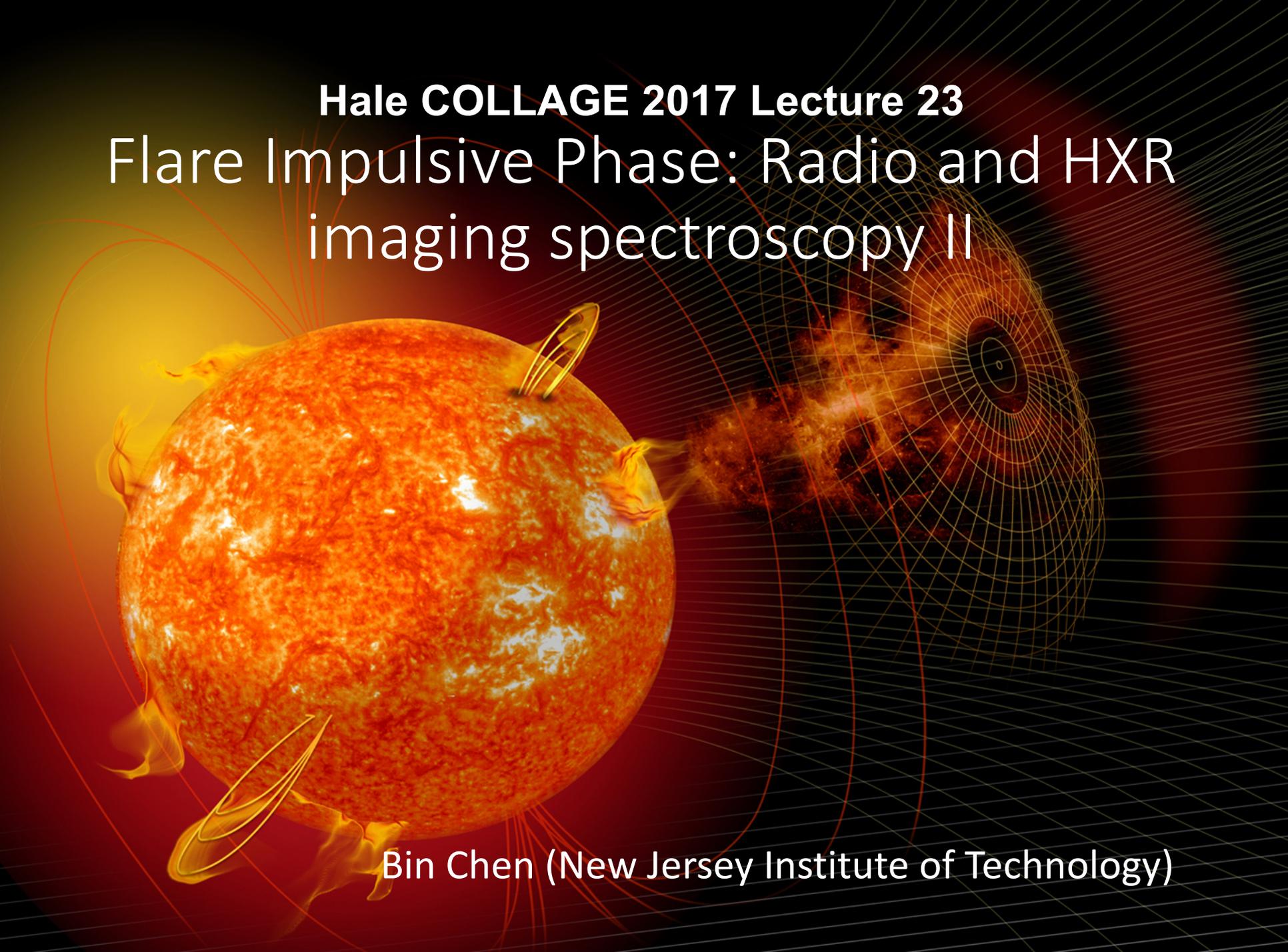


**Hale COLLAGE 2017 Lecture 23**  
**Flare Impulsive Phase: Radio and HXR**  
**imaging spectroscopy II**

**Bin Chen (New Jersey Institute of Technology)**



# Outline

- Radiation from energetic particles
  - Bremsstrahlung → Lecture 20
  - Gyromagnetic radiation (“magnetobremsstrahlung”) → Lecture 21
  - Other radiative processes → Lecture 22
    - Inverse Compton, coherent radiation
- Diagnosing flare energetic particles using hard X-ray and radio spectroscopy and imaging
  - **Where?** → previous lecture
  - **What?** → this lecture
- Suggested reading: Ch. 13 of Aschwanden’s book for hard X-rays and Ch. 15 for radio

# Diagnosing energetic electrons

- Each mechanism provides a method to probe the thermal plasma and/or energetic electrons
  - **Acceleration: Where? When? What?**
- HXR:
  - Thermal bremsstrahlung →  $n_e, T_e$
  - Nonthermal thin-target and thick-target bremsstrahlung →  $f(E)$
  - Inverse Compton → mostly corrections to  $f(E)$
- Radio:
  - Thermal bremsstrahlung →  $n_e, T_e$
  - Gyrosynchrotron →  $f(E), n_e, T_e, B, \theta$
  - Coherent radiation →  $n_e$  (possibly  $f(E), B$ , model dependent)

# A note on electron energies

- For an electron
  - Total energy  $\varepsilon_{total} = \gamma m_e c^2$
  - kinetic energy  $\varepsilon = (\gamma - 1) m_e c^2$ , where  $\gamma = 1/\sqrt{1 - \beta^2}$
- **Thermal electron** in the corona:  $T \sim 1$  MK,  $\beta \sim 0.018$ , or  $\varepsilon \approx 0.086$  keV  $\rightarrow$  nonrelativistic
- **Type-III-burst-emitting electron**  $\beta \approx 0.1-0.3$  or  $\varepsilon \approx 5-50$  keV  $\rightarrow 5\sim 20$  x thermal speed  $\rightarrow$  bump-on-tail instability  $\rightarrow$  nonrelativistic to mildly relativistic
- **HXR-emitting electron**  $\varepsilon \approx 20-200$  keV  $\rightarrow \beta \approx 0.2-0.5 \rightarrow$  mildly relativistic
- **Gyrosynchrotron-emitting electron**  $\gamma \approx 2 - 6 \rightarrow \beta \approx 0.6-0.9$  or  $\varepsilon \approx 0.5-3$  MeV  $\rightarrow$  (upper-end of) mildly relativistic

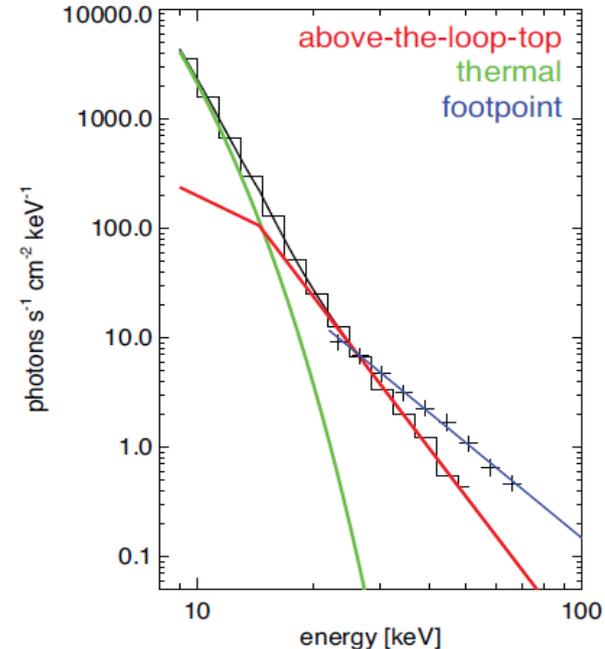
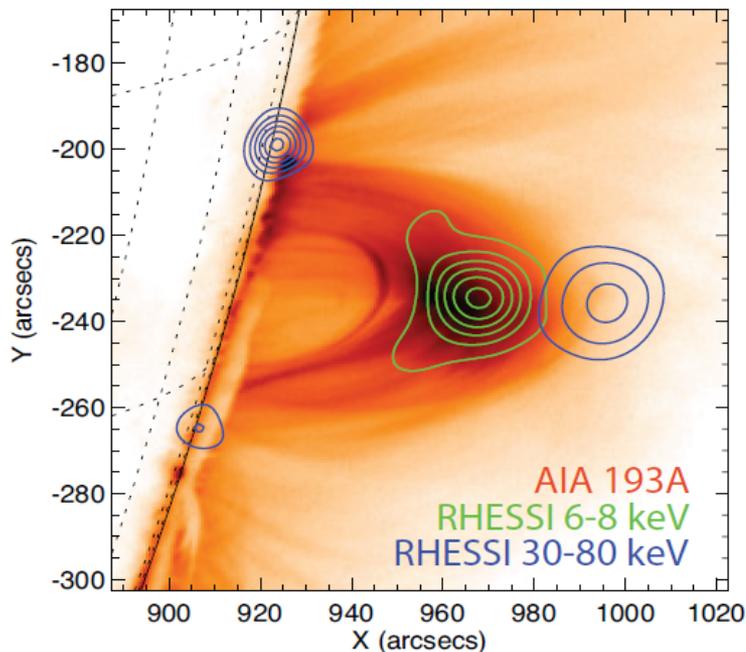
Each emission probes a different part of the electron energy spectrum!

# HXR spectral analysis

- Currently the most straightforward method to derive the distribution function of the accelerated electrons  $f_{nt}(E)$ . Also capable of obtaining  $f_{nt}(E)$  of  $>\sim 20$  MK flare plasma
- Number density ratio  $n_{nt}/n_{th}$  (previous lecture)
- Energy density ratio  $\varepsilon_{nt}/\varepsilon_{th}$
- Details of  $f_{nt}(E)$  and its spatiotemporal evolution provide diagnostics for acceleration and transport processes

# From HXR spectra to electron distribution

- Forward fitting with parameterized model(s): Thermal + power-law? Thermal + superhot? Thermal + kappa? Thin-target? Thick-target? ...
- Regularized inversion



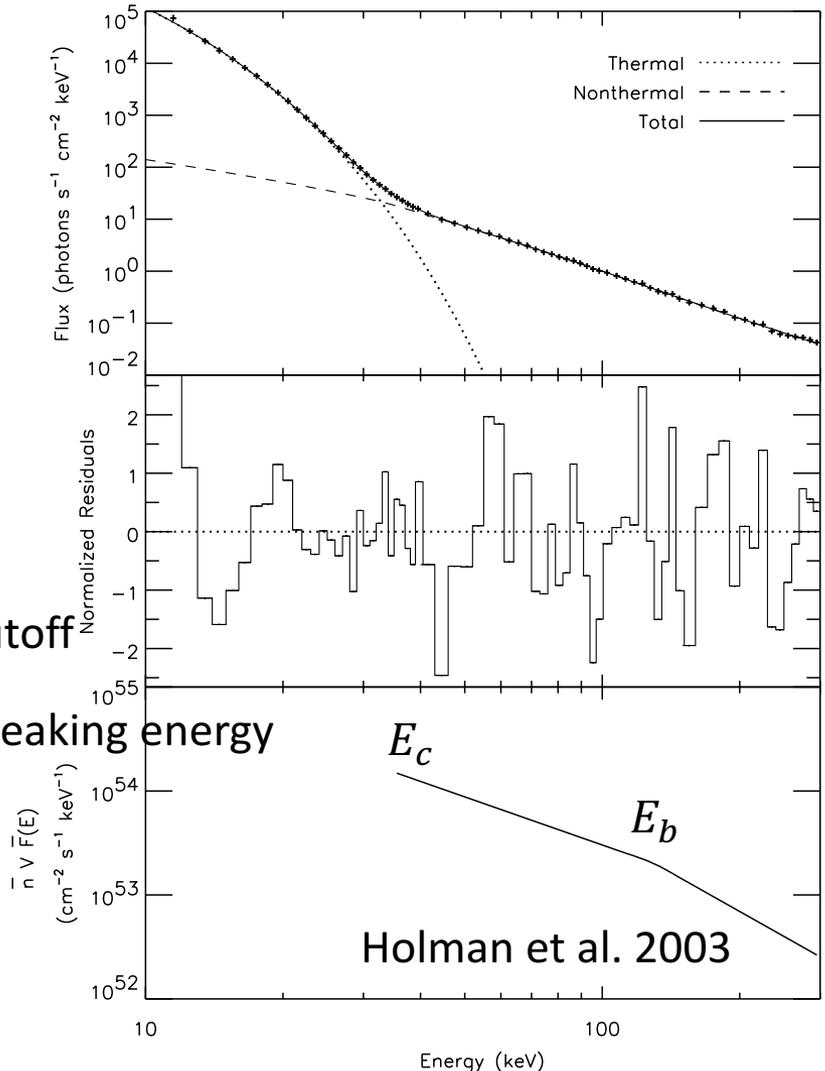
# Forward fitting HXR spectra

- People often use a **two-component** model electron energy spectrum to fit the HXR spectrum
- Isothermal Maxwellian
- Broken power-law with low-energy cutoff

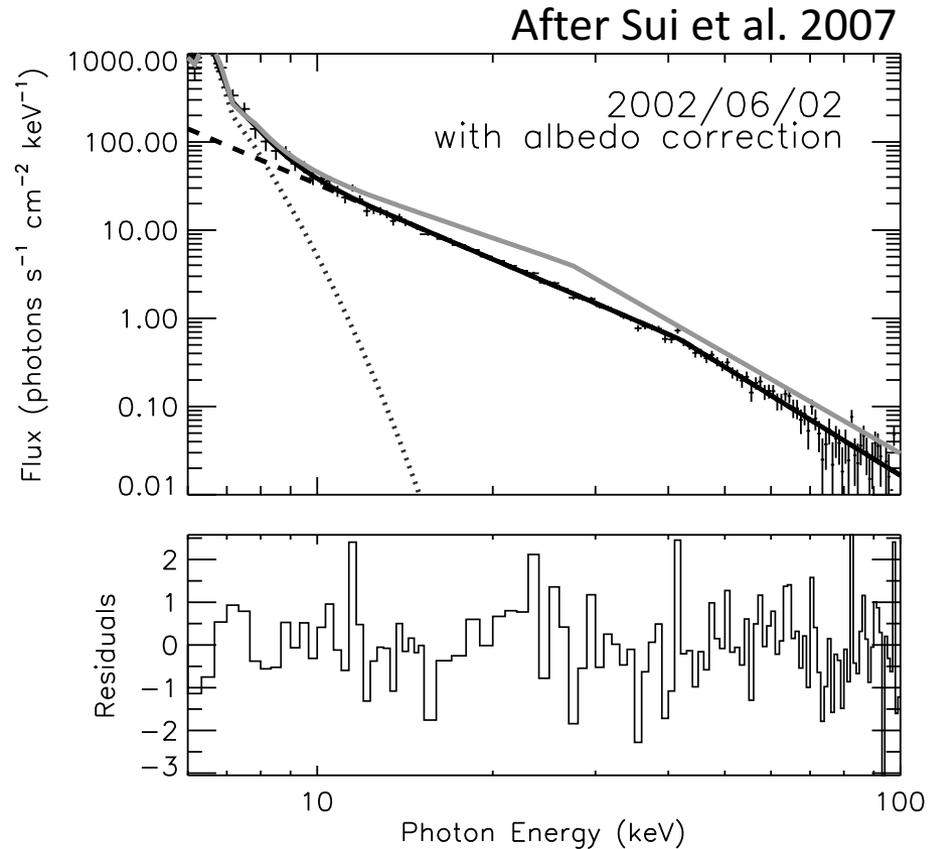
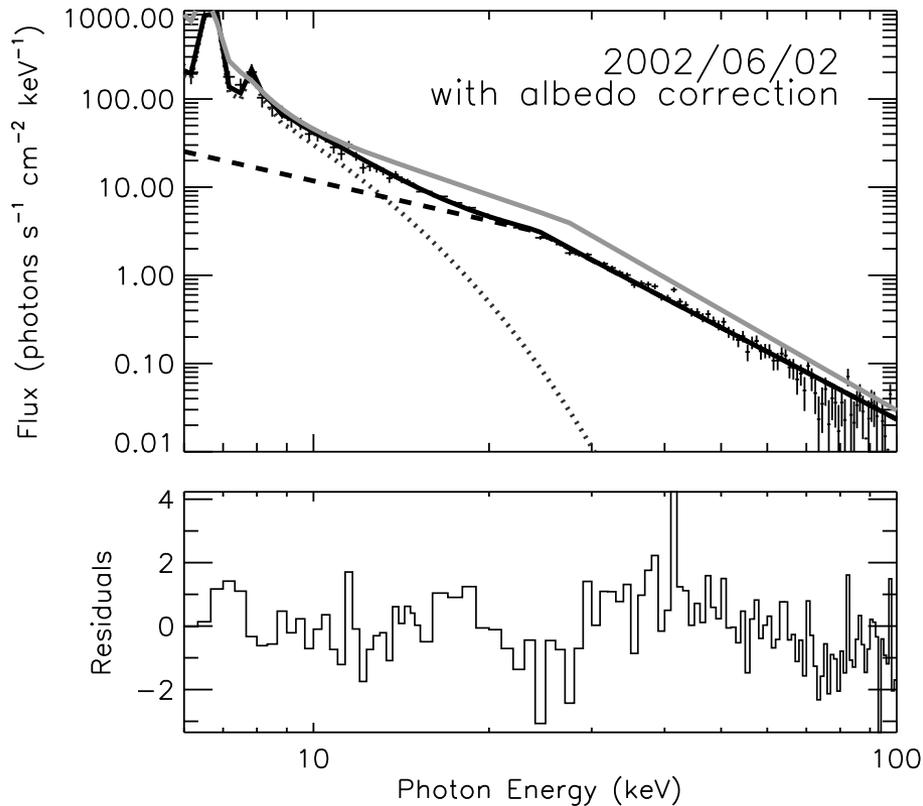
$$\bar{F}(E) = \begin{cases} 0; & E < E_c \\ AE^{-\delta_1}; & E_c < E < E_b \\ AE_b^{\delta_2 - \delta_1} E^{-\delta_2}; & E_b < E \end{cases}$$

Low-energy cutoff
Breaking energy

Mean electron flux (electrons  $\text{cm}^{-2} \text{s}^{-1} \text{keV}^{-1}$ , different from  $f(E)$  -- c.f. Lecture 17)



# Spot the difference...



What is the difference in the model? Which forward fit result is better?

# Low-energy cutoff plays a key role

- Let's assuming a single power-law with a low-energy cutoff:  $\bar{F}(E) = AE^{-\delta}$  ( $E > E_c$ )

- Nonthermal electron flux (electrons  $\text{cm}^{-2} \text{s}^{-1}$ ):

$$\int_{E_c}^{\infty} AE^{-\delta} dE = \frac{A}{\delta-1} E_c^{-\delta+1} \text{ (if } \delta > 1 \text{)}$$

- Nonthermal electron energy flux ( $\text{erg cm}^{-2} \text{s}^{-1}$ ):

$$\int_{E_c}^{\infty} AE^{-\delta+1} dE = \frac{A}{\delta-2} E_c^{-\delta+2} \text{ (if } \delta > 2 \text{)}$$

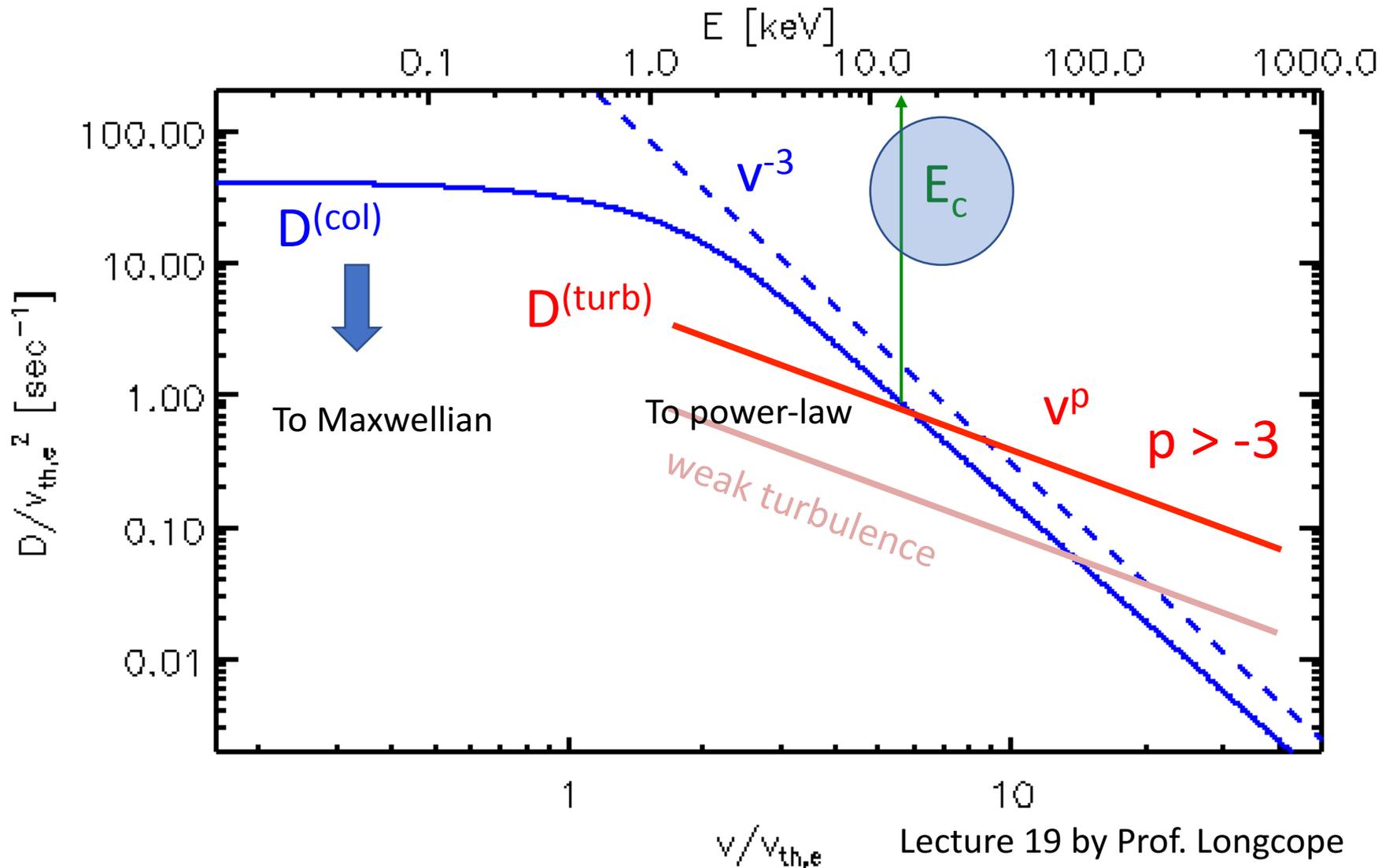
- Both are very sensitive to  $E_c$

- e.g., for  $\delta = 4$  ("typical" in a flare peak), a factor of 2 error in  $E_c$  means a factor of 4 error in energy flux!

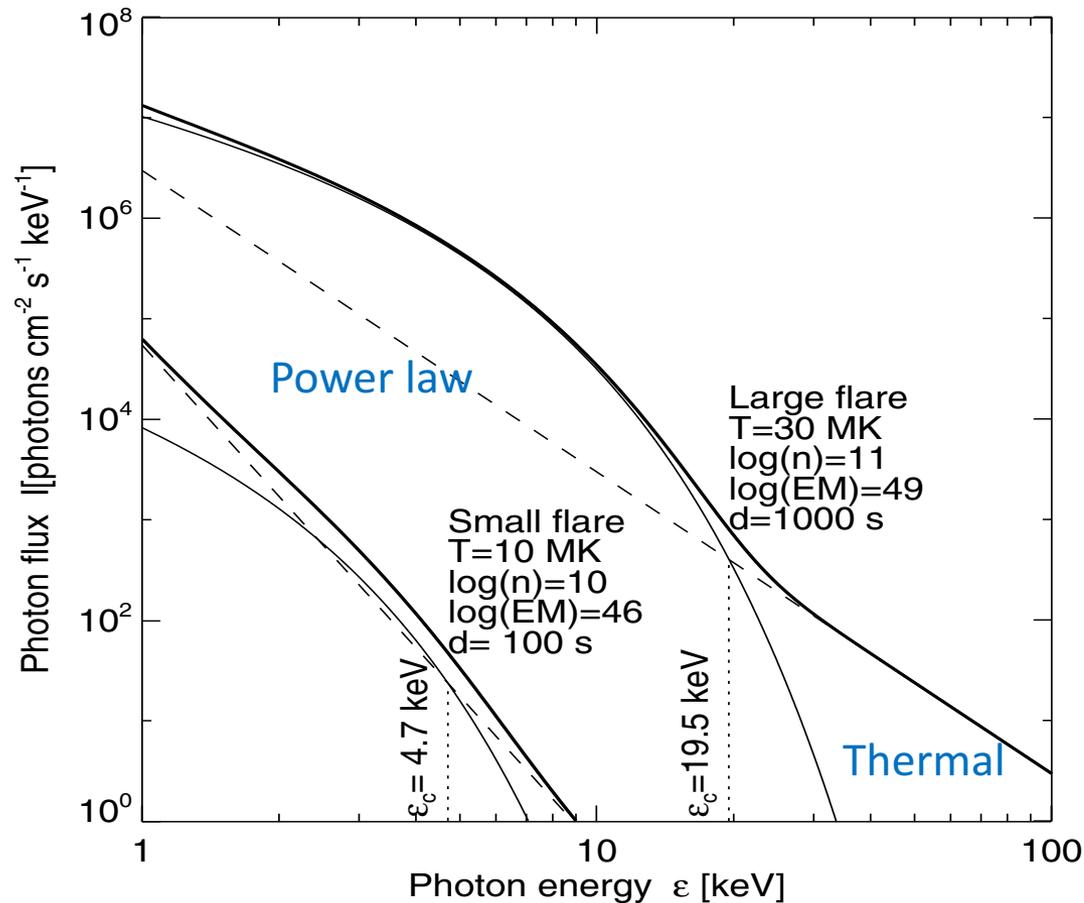
- Both are very important observables to examine particle acceleration mechanisms

- e.g., a smaller low-energy cutoff would require a much more efficient acceleration mechanism

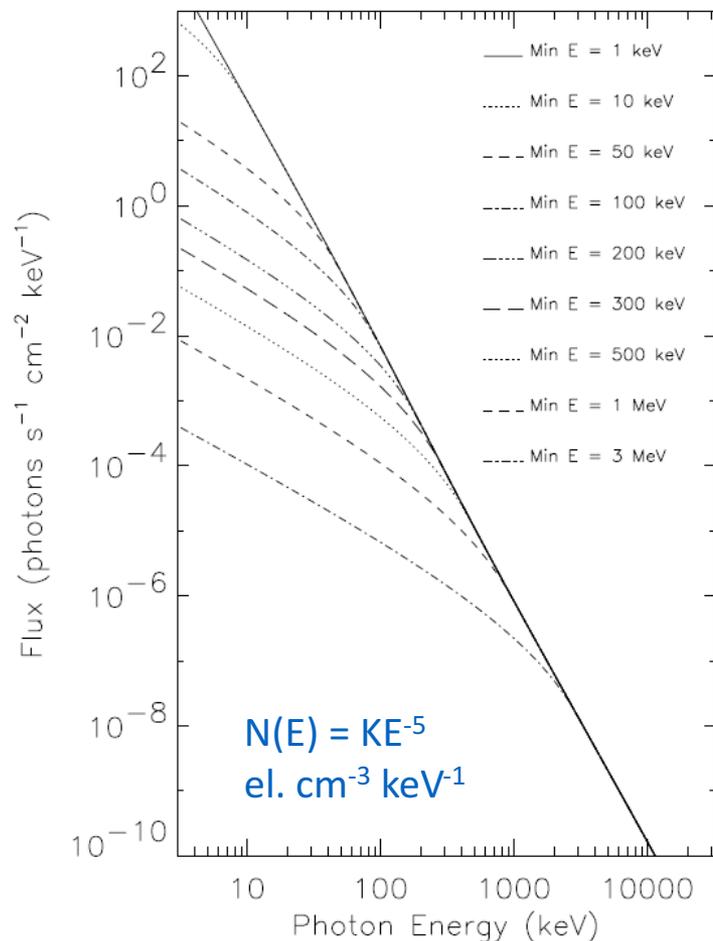
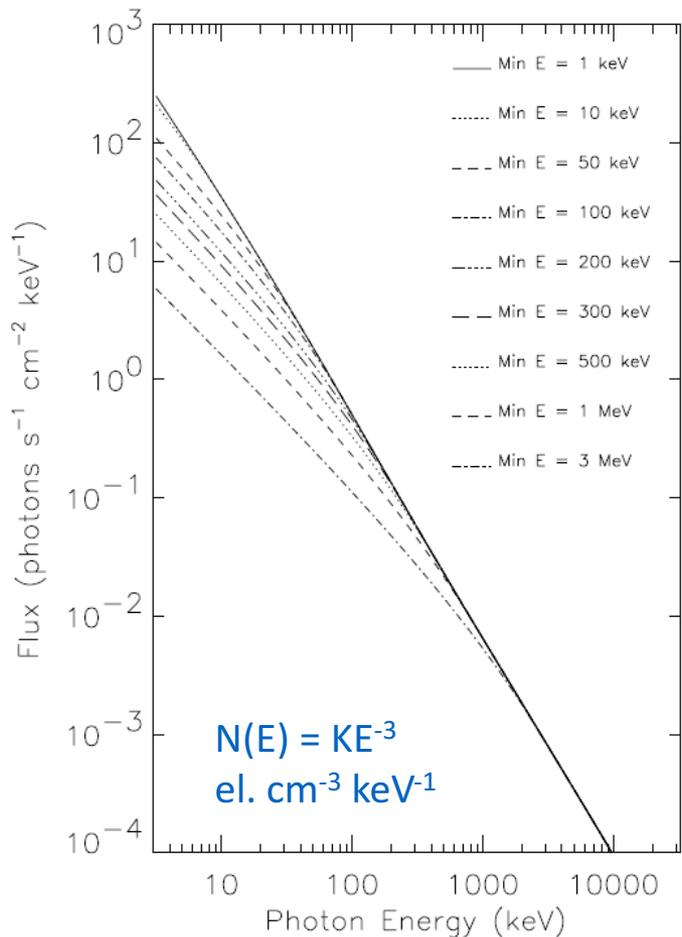
# Low energy cutoff plays a key role



# Low-energy cutoff: Can we determine it from HXR spectral analysis?



# HXR spectra: low-energy cutoffs

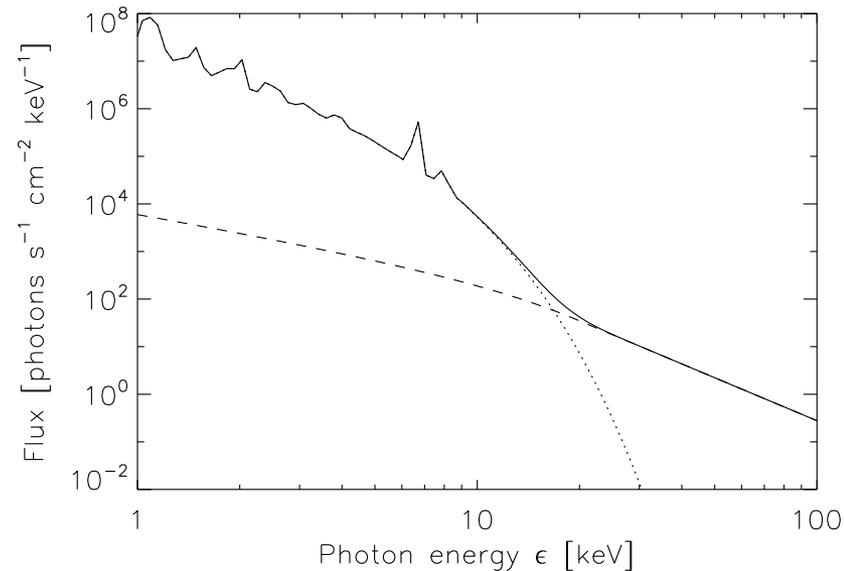


Holman 2003

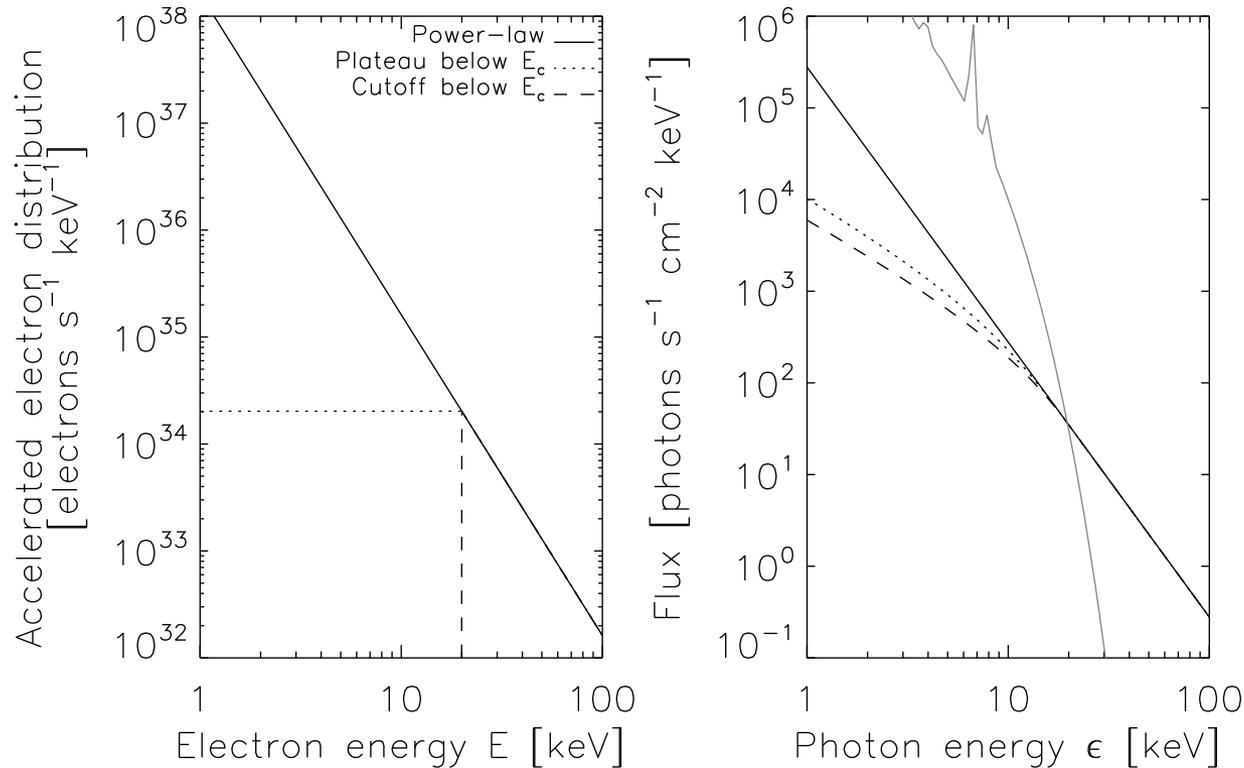
Low energy cutoff *flattens* the HXR spectra at lower energies

# Low-energy cutoff

- Results in a flattening of HXR spectrum below  $E_c$
- But usually masked by the thermal component!
- For a typical flare with distinctive thermal + nonthermal component:
  - Well constrained at the high-energy side
  - Poorly constrained at the low-energy side
- Low-energy cutoff is usually really the “*highest value* of  $E_c$  that still fits the data”, which gives a *lower limit* of the total nonthermal energy

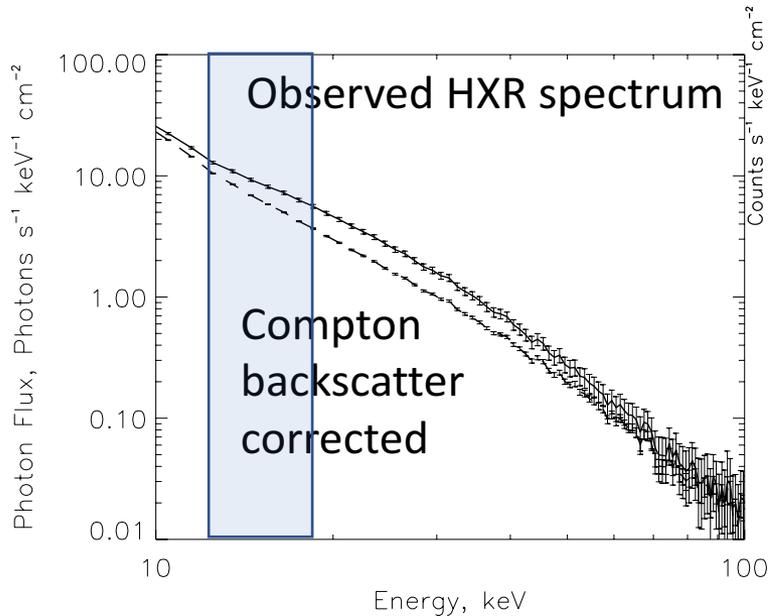


# Different forms of low-energy cutoff

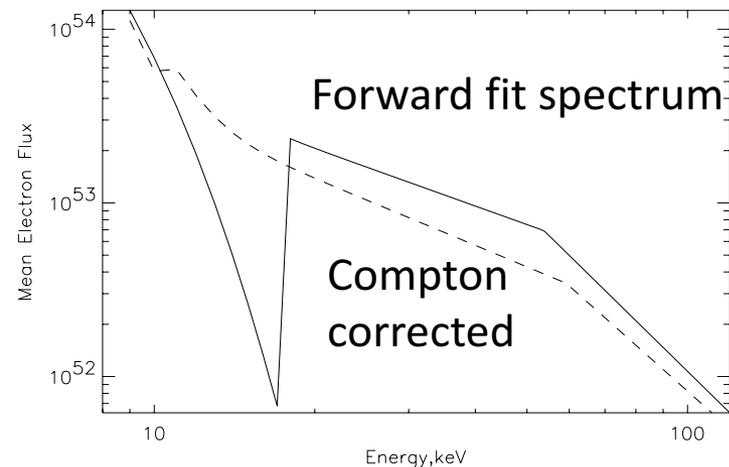
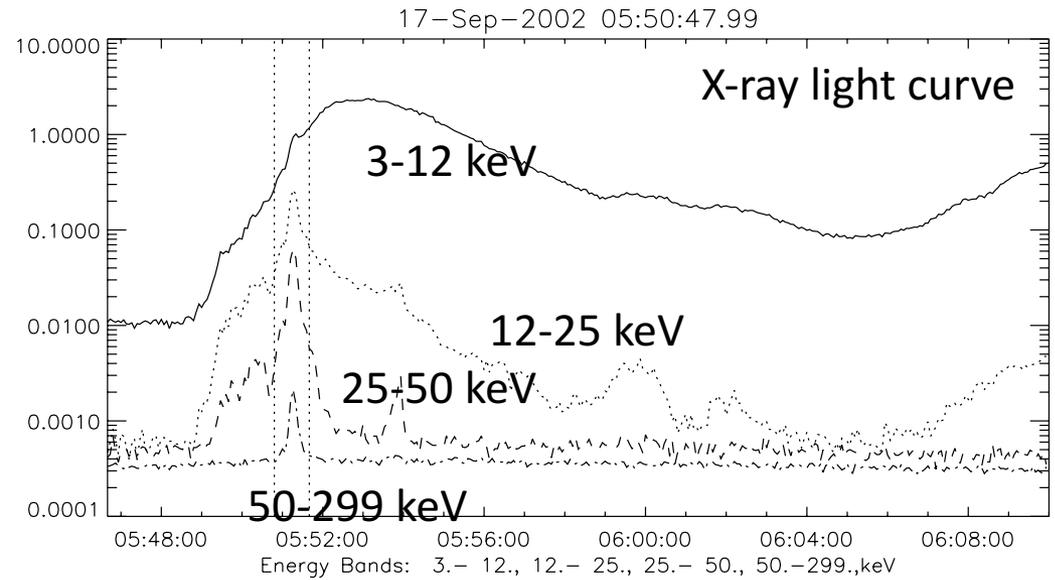


- Different forms of low-energy cutoff lead to **subtle difference** in the observed X-ray spectra  $\rightarrow$  difficult to determine
- Luckily, the exact shape of low-energy cutoff is not dramatically important in terms of energetics

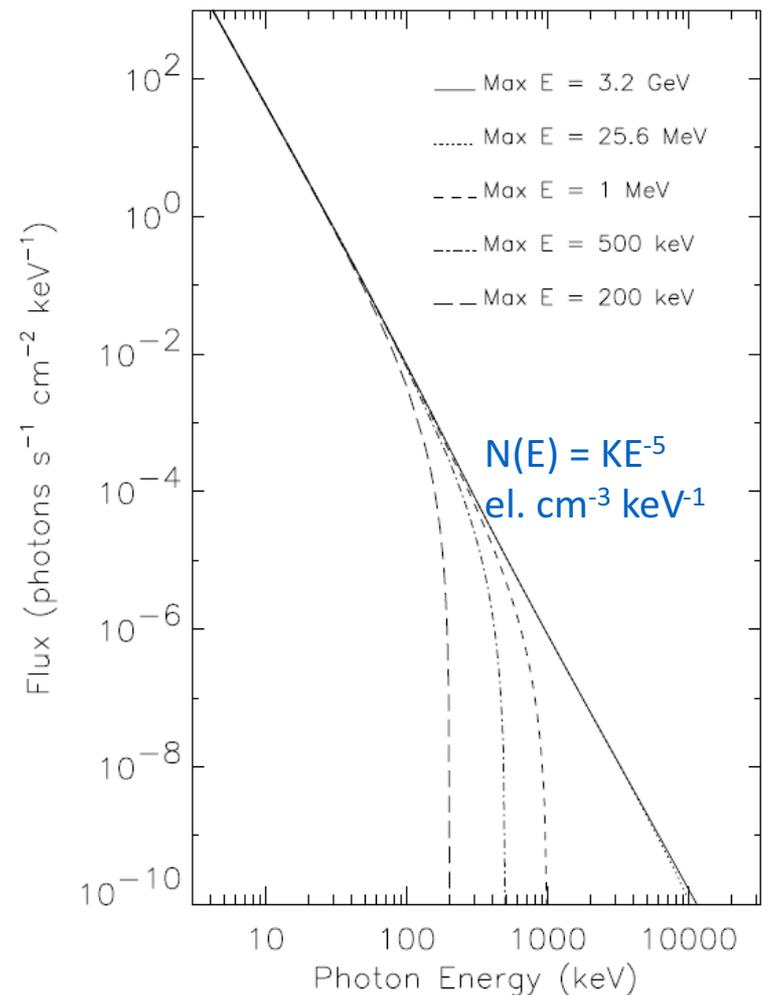
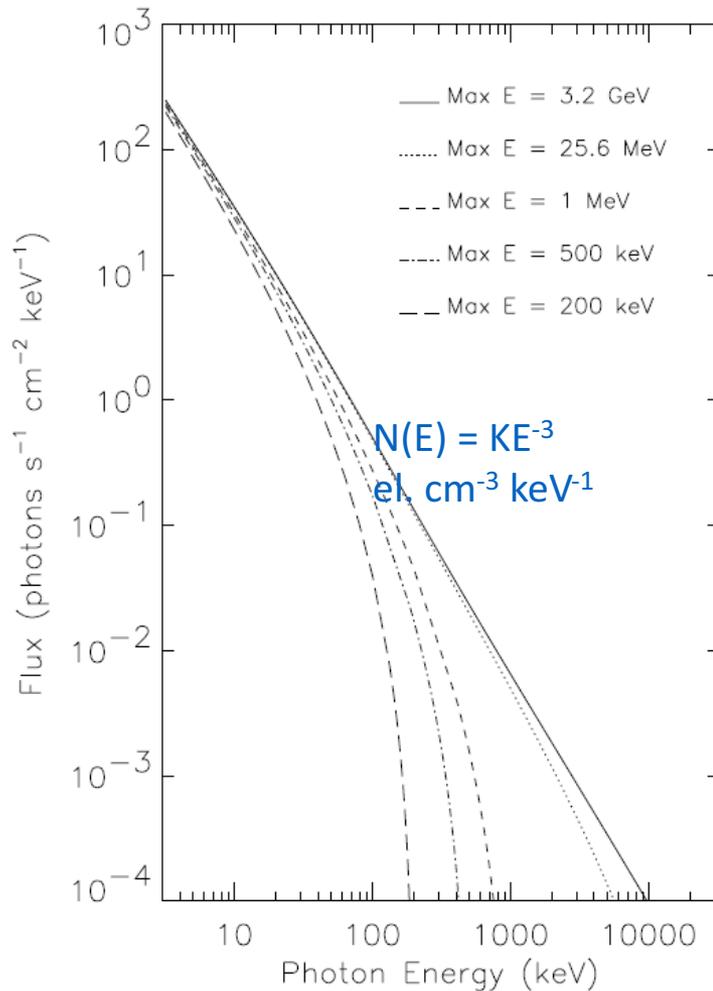
# Low-energy cutoff: An example



Can you identify the possible location of  $E_c$  and  $E_b$ ?



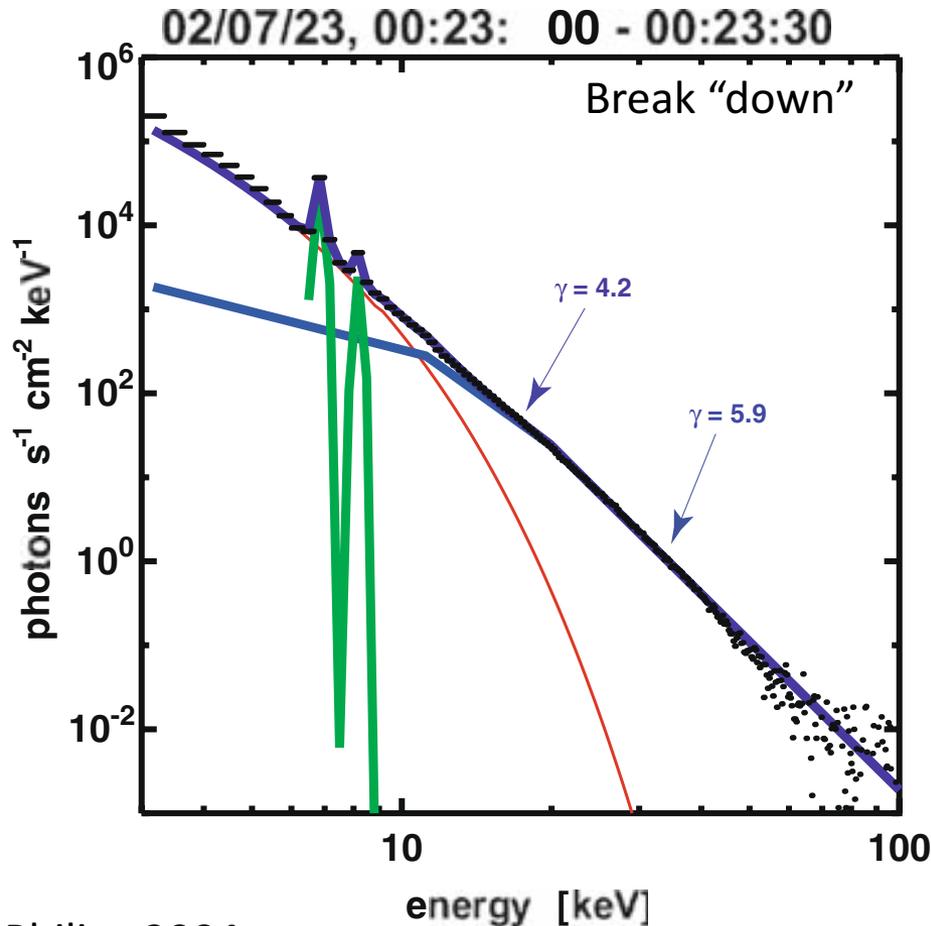
# HXR spectra: high-energy cutoffs



Holman 2003

High energy cutoff leads to a *steepening* of the HXR spectra at high energies

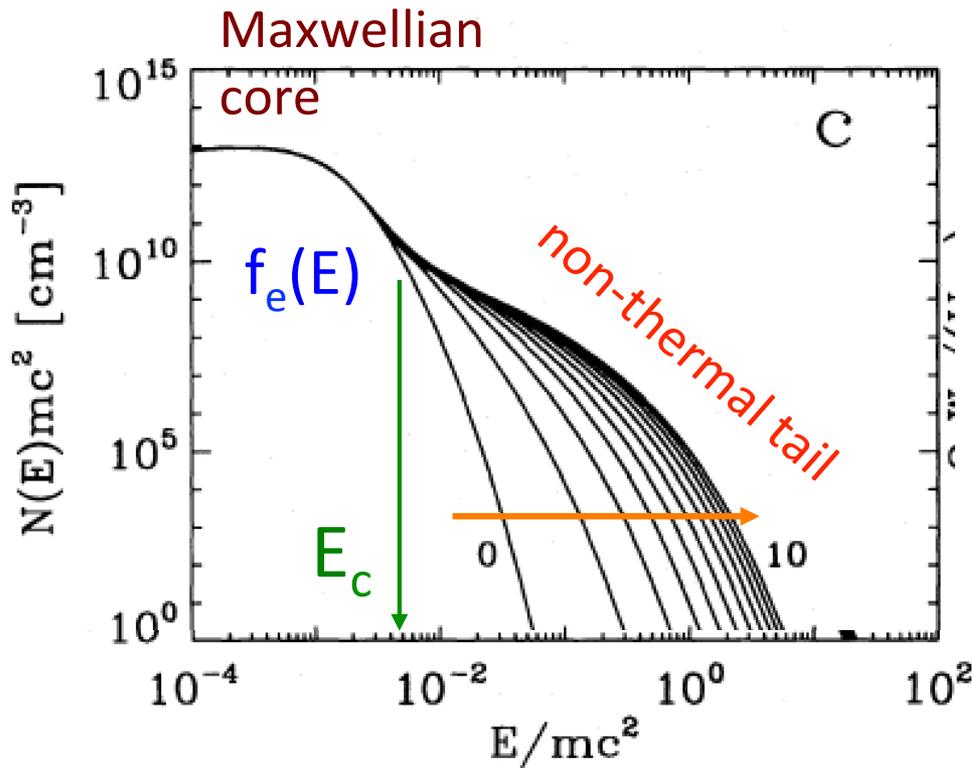
# HXR Spectral breaks



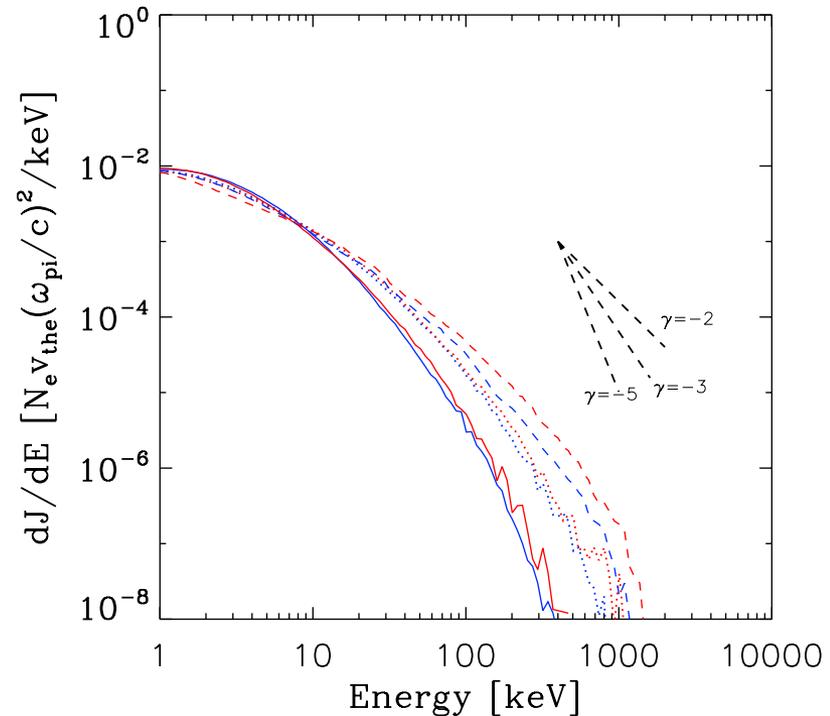
Philips 2004

- HXR spectral fit results usually show a spectral break at  $\sim 30$ - $60$  keV
- **Flatter** at lower energies, and **steeper** at higher energies

# Possibility 1: less $e^-$ at higher energies



Stochastic acceleration (Miller et al. 1996, see also Lecture 19 by Prof. Longcope)



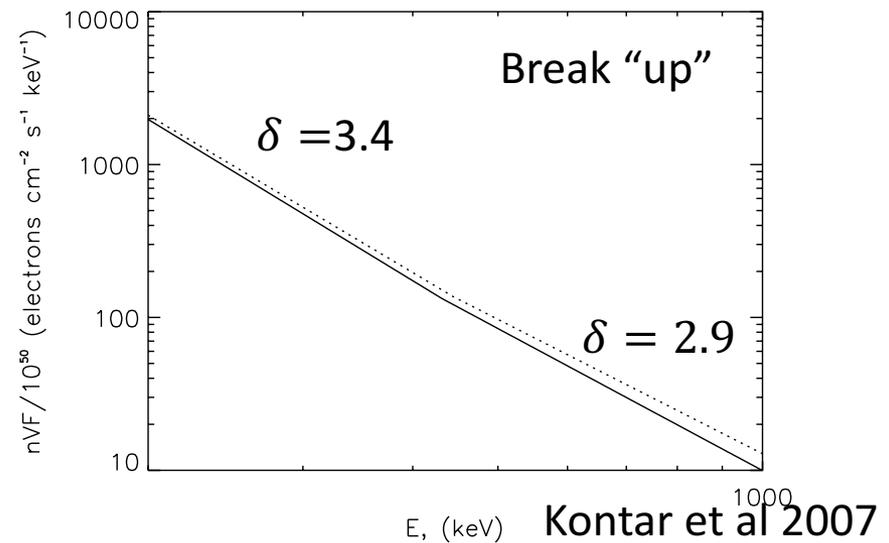
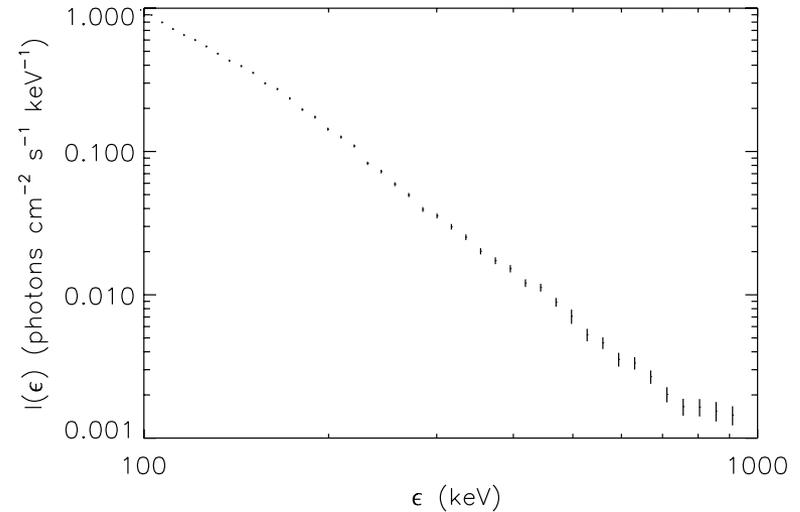
Acceleration by termination shock (Guo & Giacalone 2012)

# Possibility 2: loss of low energy $e^-$

- **Return current:** large number of electrons precipitating to the footpoint → “returning” ambient electrons to re-establish neutral charge → self-induced “return current”
- Return current generates an electric field (Ohm’s law) along the loop
- Lower energy electrons lose a larger *fraction* of energy than their higher energy counterparts → flattening of the HXR spectrum at lower energies

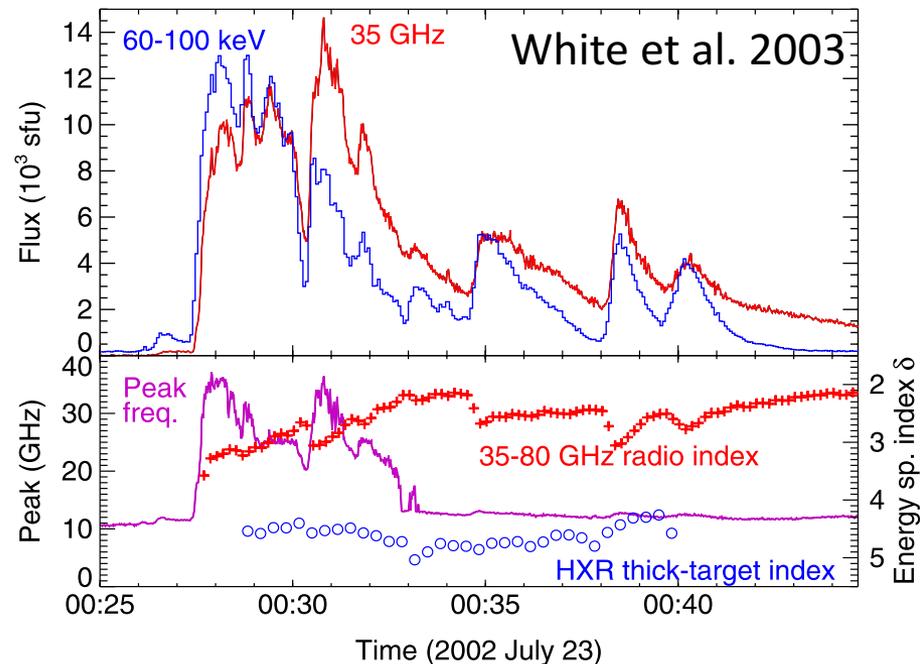
# Spectral breaks at higher energy

- At higher energies, the HXR/ $\gamma$ -ray spectrum break “up” again
- Contribution from the e-e bremsstrahlung
- Acceleration mechanism?



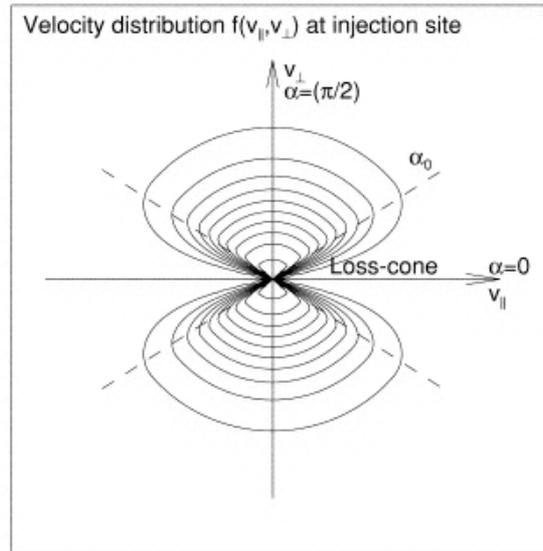
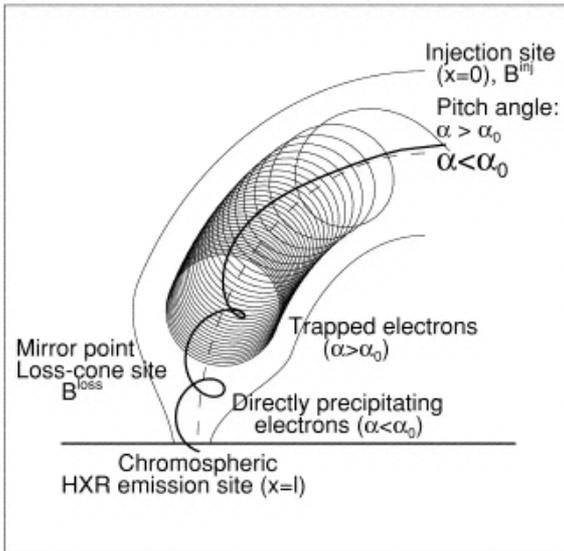
# Microwave gyrosynchrotron spectra

- HXR photons with energy  $\varepsilon$  come from electrons with  $\sim\varepsilon$  via bremsstrahlung  $\rightarrow$  10s to 100s keV
- Microwave gyrosynchrotron probes electrons with higher energies (>300 keV)
- Can one electron distribution fits all?



Large discrepancy usually found between HXR and microwave!

# HXR and microwave discrepancy: What's wrong?

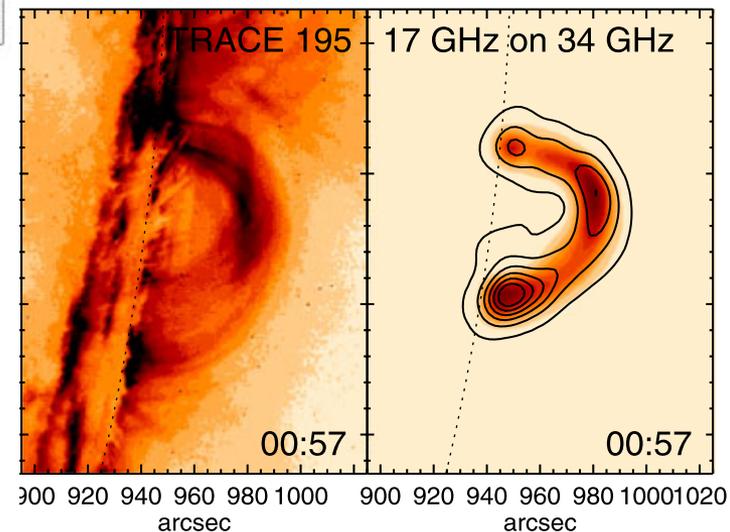


- HXR emission is dominated by the *precipitated* electrons at the chromosphere

- Gyrosynchrotron emission is mainly from the *trapped* electrons in the flare loop
- Trapping may result in hardening
- Anisotropy* of electron distribution also contributes to spectral hardening. **How?**

The HXR/microwave discrepancy is still largely unexplained

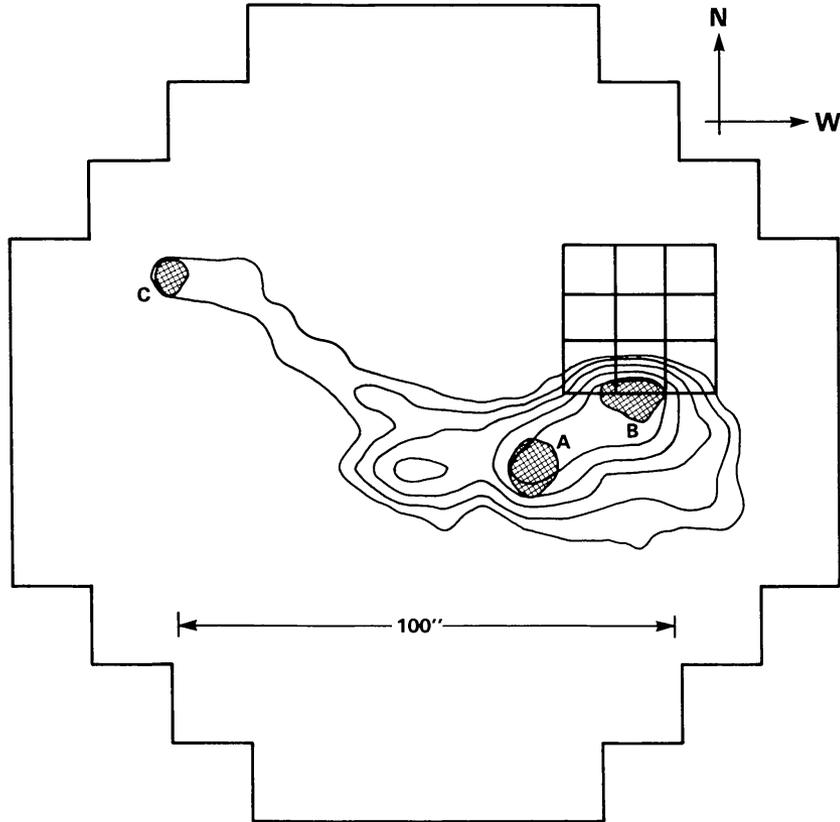
White et al. 2011



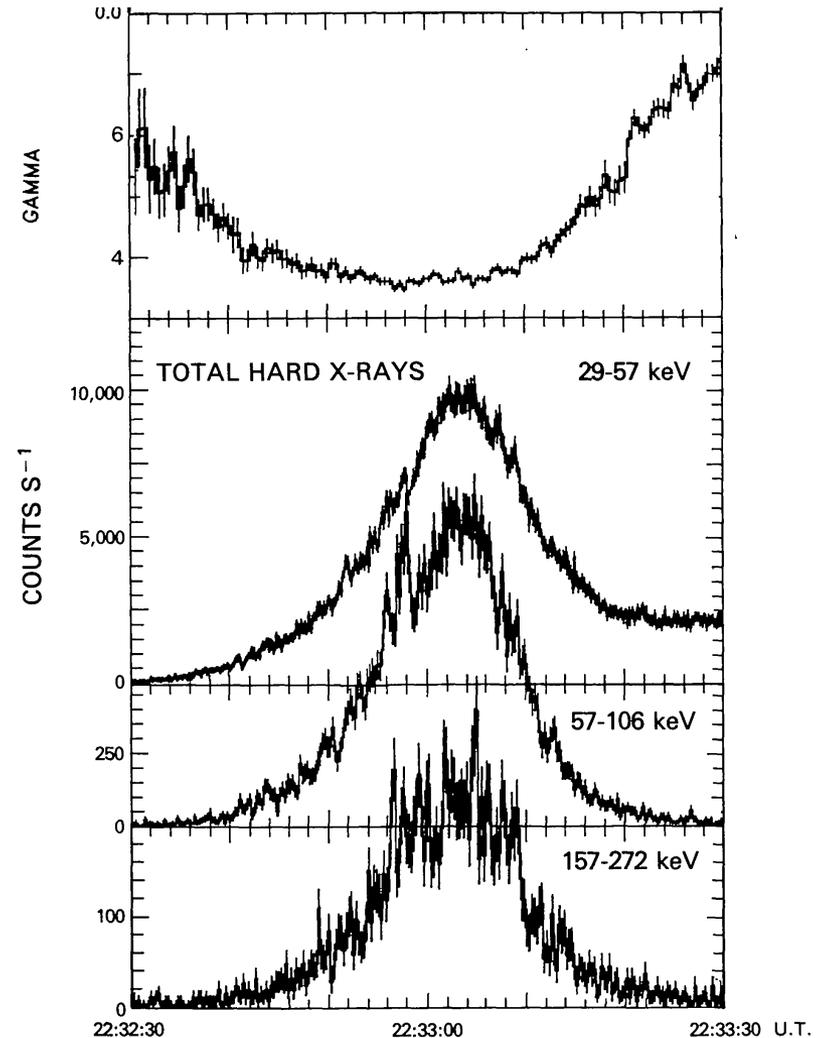
# HXR/microwave spectra evolution

- Events showing **impulsive** HXR/microwave peaks usually have a **harder** spectral index during the peaks, and **softer** both in the rise and decay phase, known as a ***soft-hard-soft (SHS)*** spectral evolution
- In some events, the spectra stay **hard** or even gets **harder**, known as a ***soft-hard-harder (SHH)*** spectral evolution

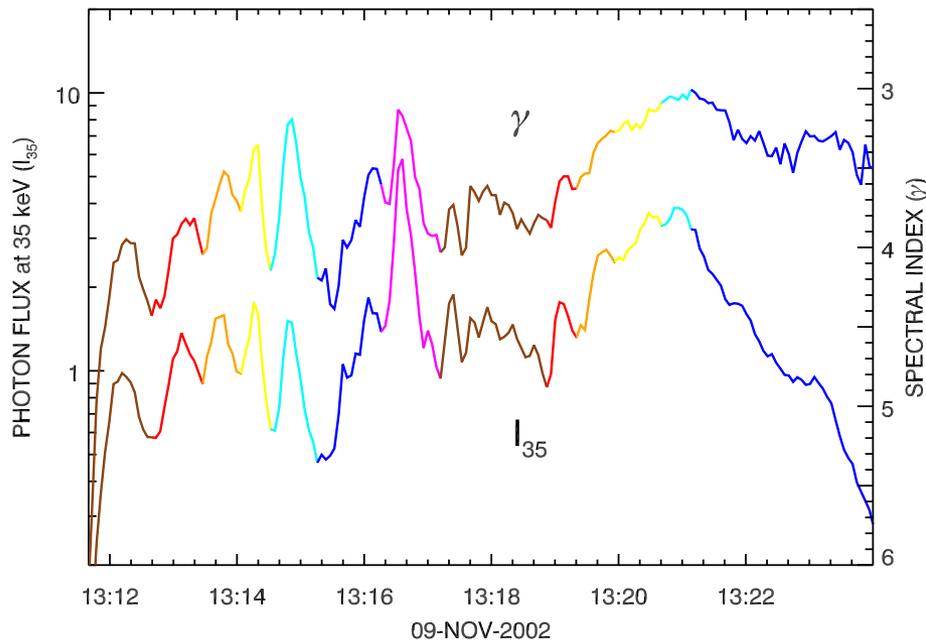
# SHS HXR spectral evolution



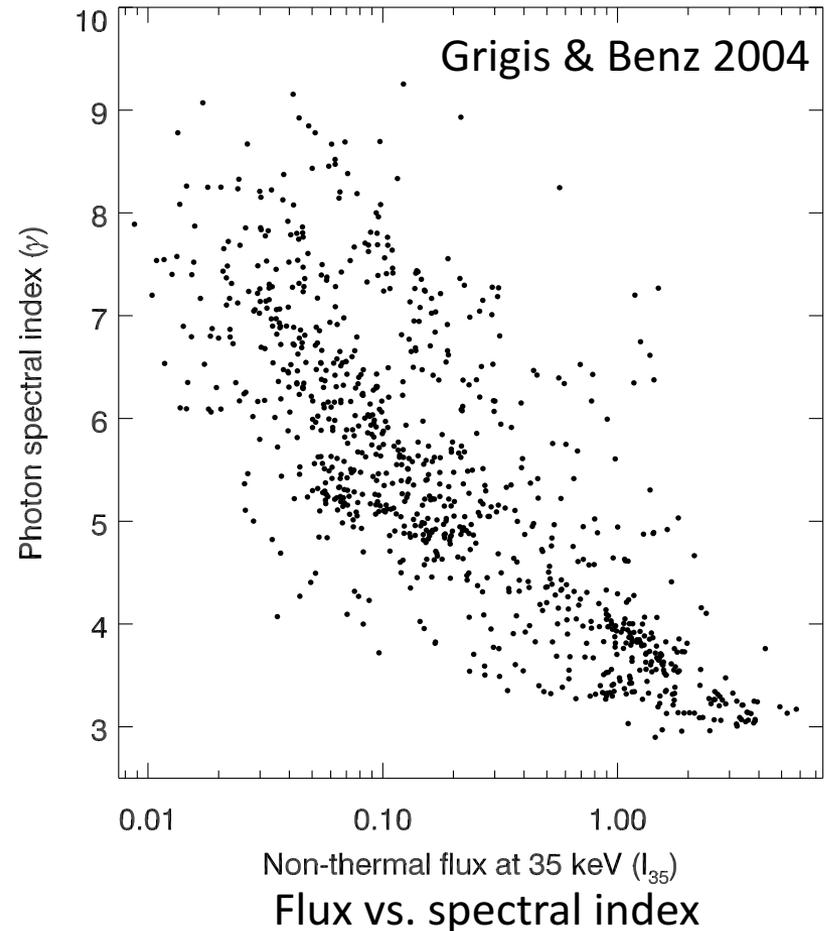
Dennis 1985



# SHS feature at every HXR peak

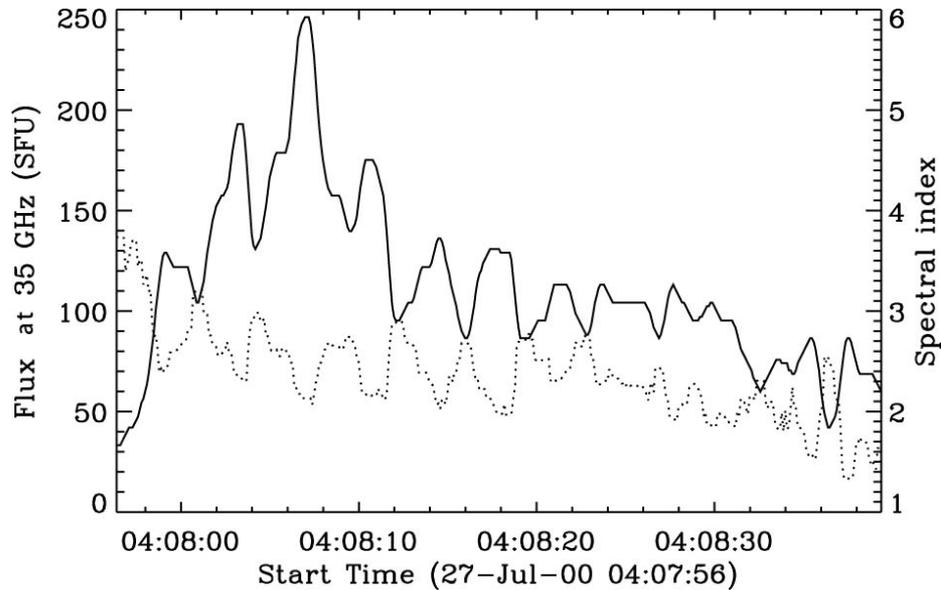


Flux and spectral index evolution

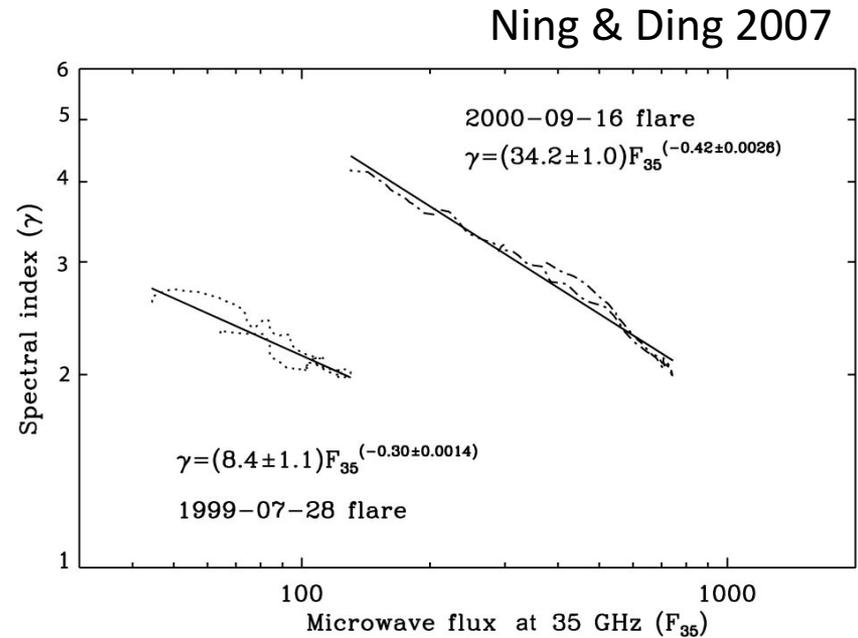


Flux vs. spectral index

# SHS spectral evolution in microwave

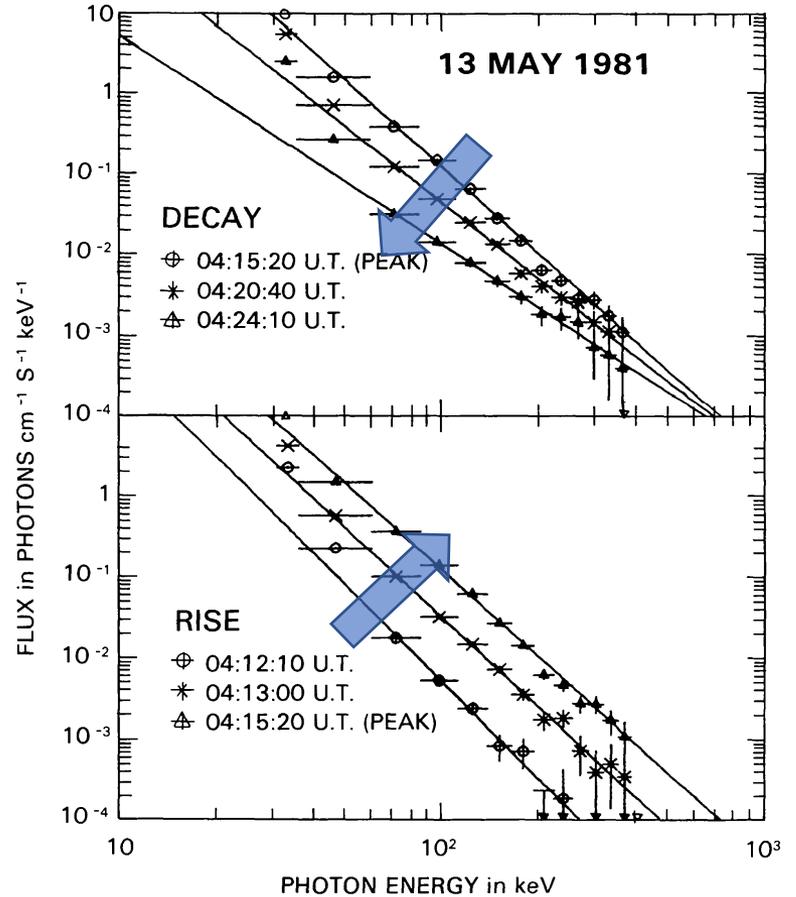
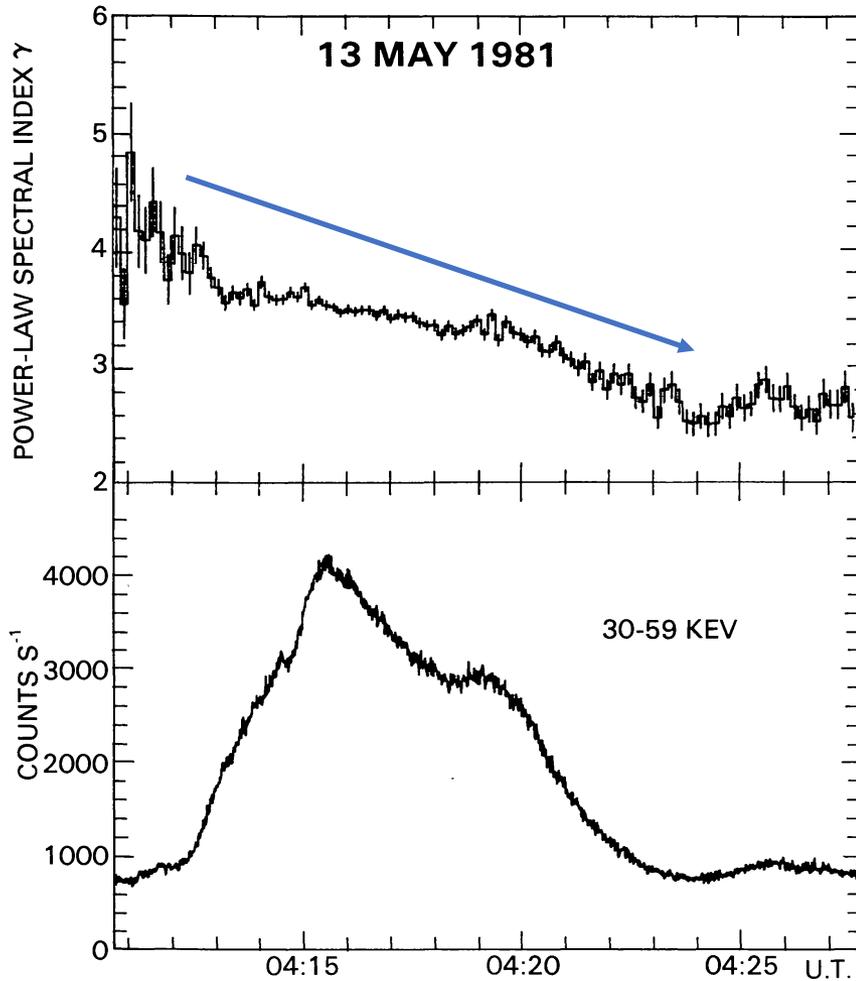


Flux and spectral index evolution



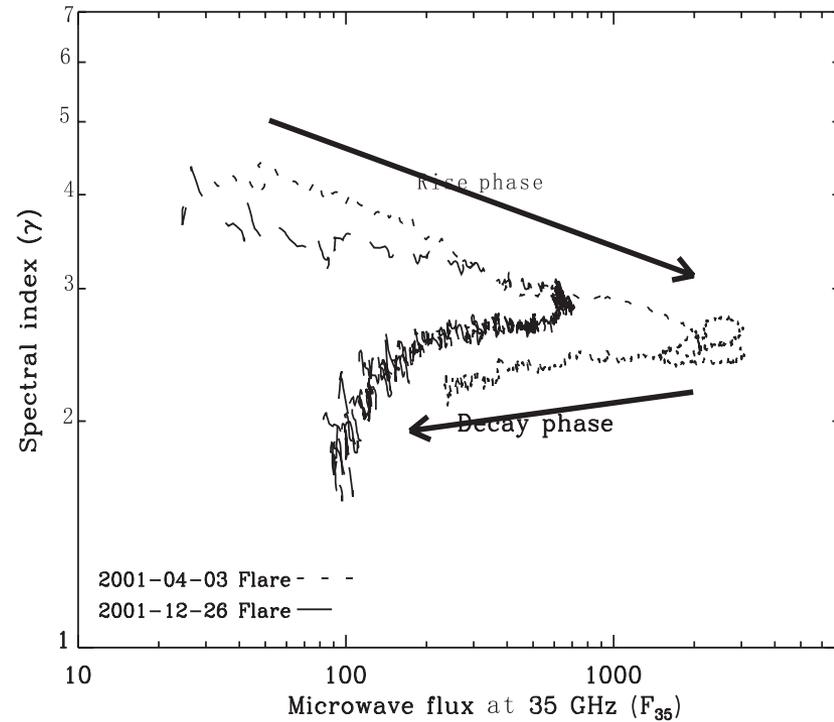
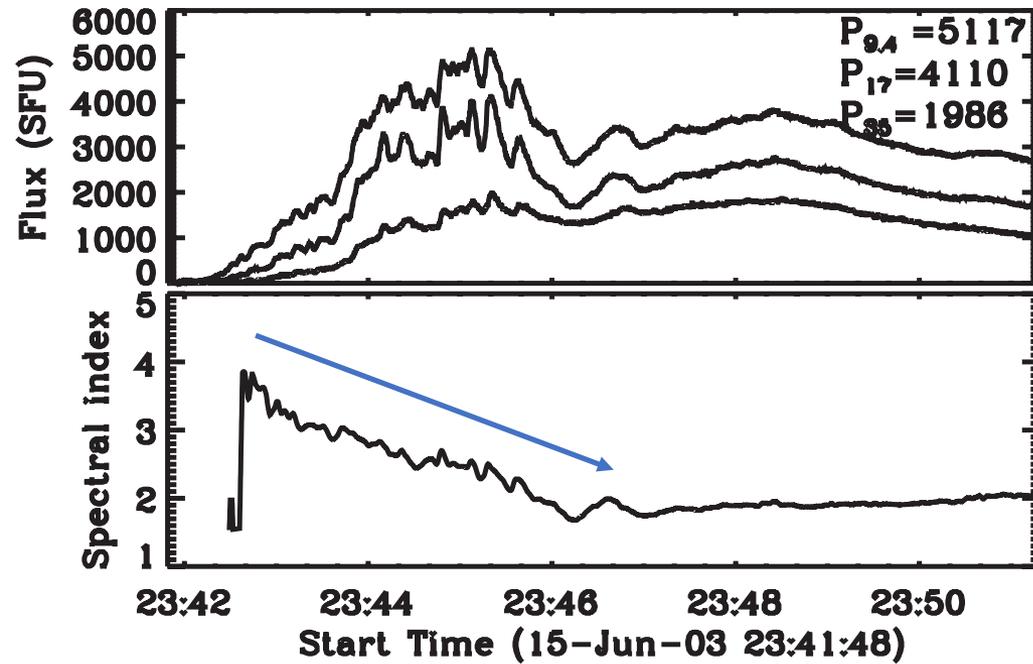
Flux vs. spectral index

# SHH HXR spectral evolution



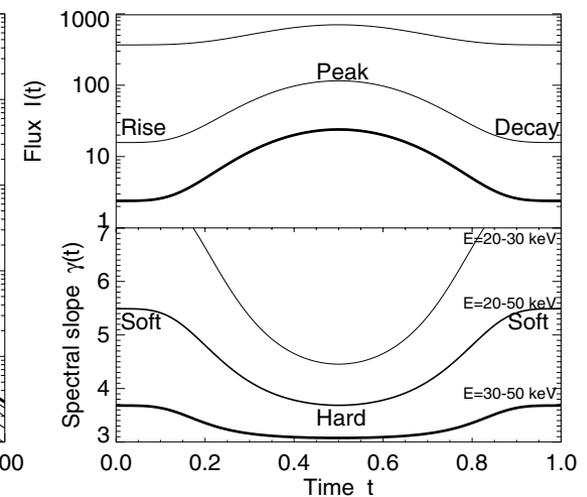
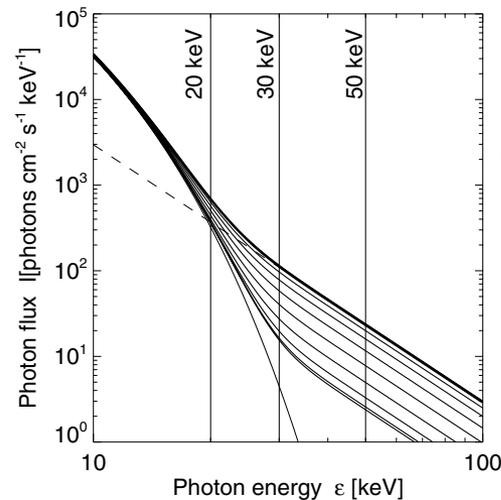
Dennis 1985

# SHH microwave spectral evolution



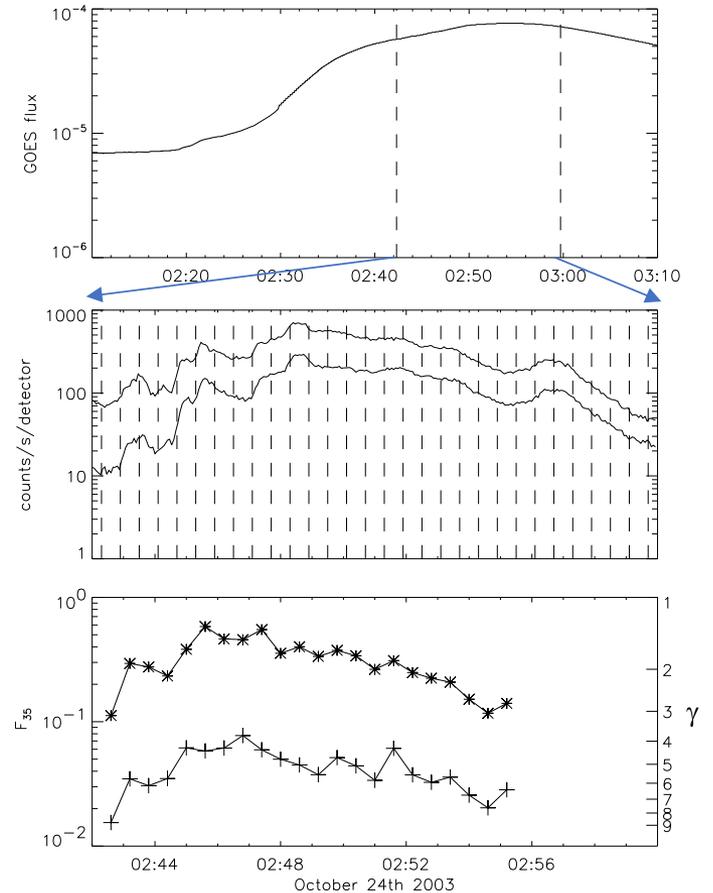
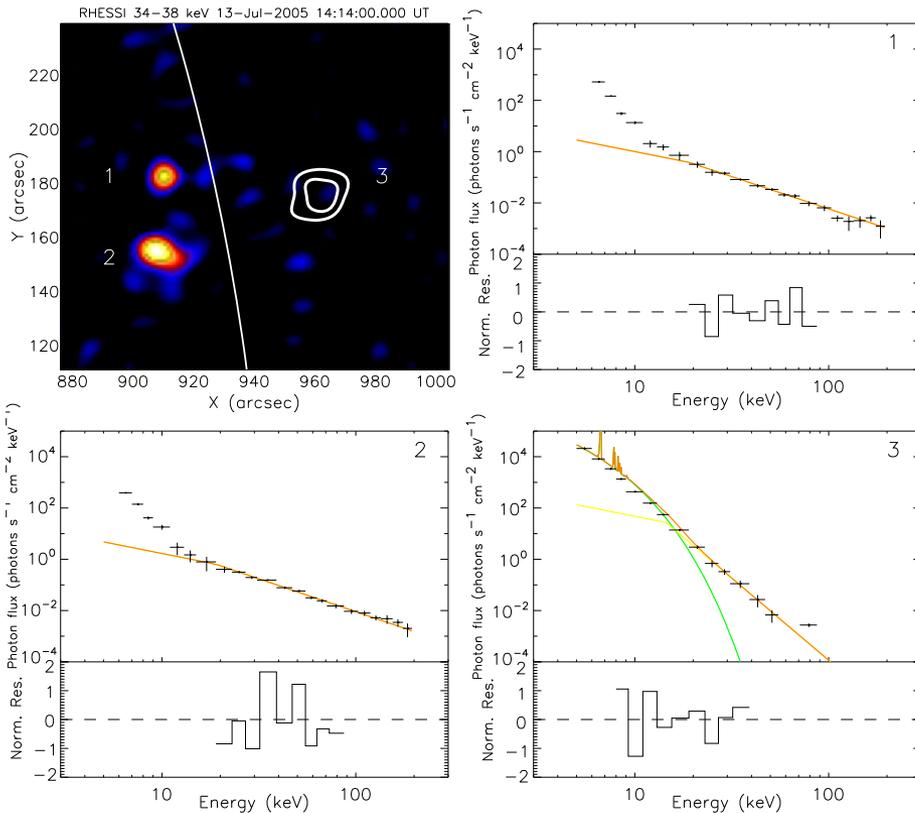
# HXR spectral evolution: Why?

- Variation of thermal and non-thermal contribution in the X-ray energy range where spectral index is obtained
- Transport: Longer transport time  $\rightarrow$  more loss in low-energy electrons  $\rightarrow$  harder spectrum
- Particle acceleration mechanism itself



# SHS also in coronal HXR sources

- Coronal HXR sources are at least closer to the acceleration site  $\rightarrow$  probably from the acceleration mechanism?



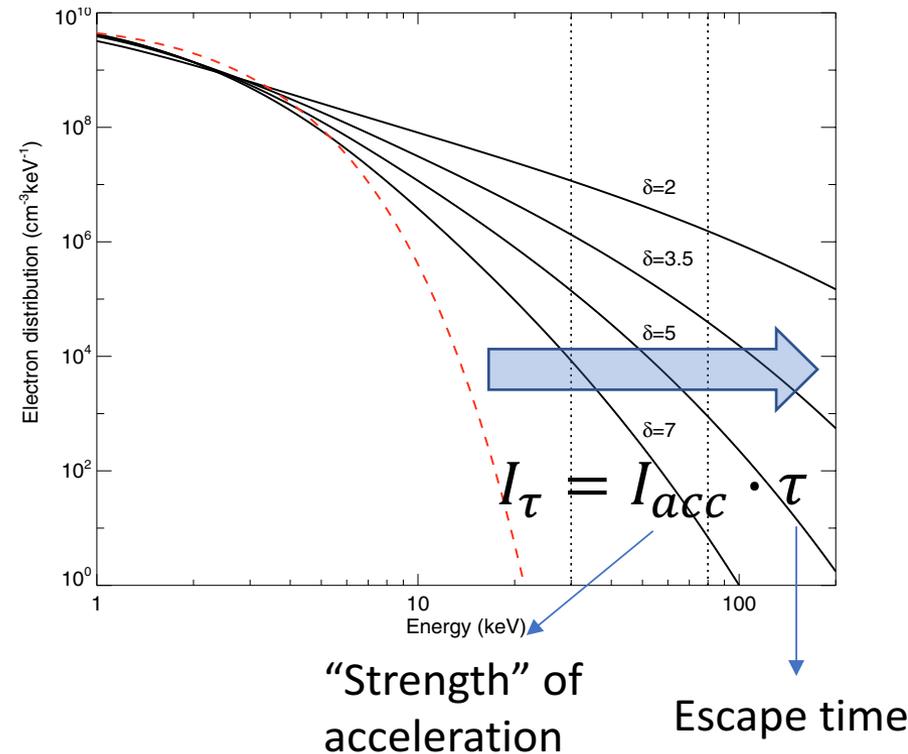
# What causes HXR spectral hardening?

- Stochastic acceleration model by turbulent fast-mode waves (c.f. Lecture 19 by Prof. Longcope)

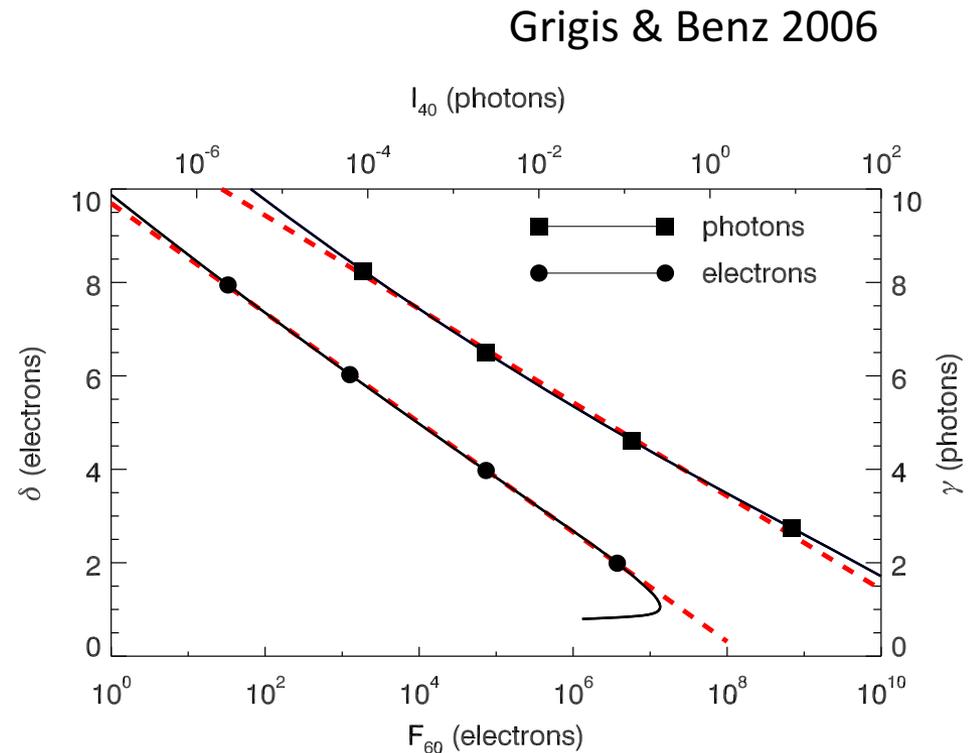
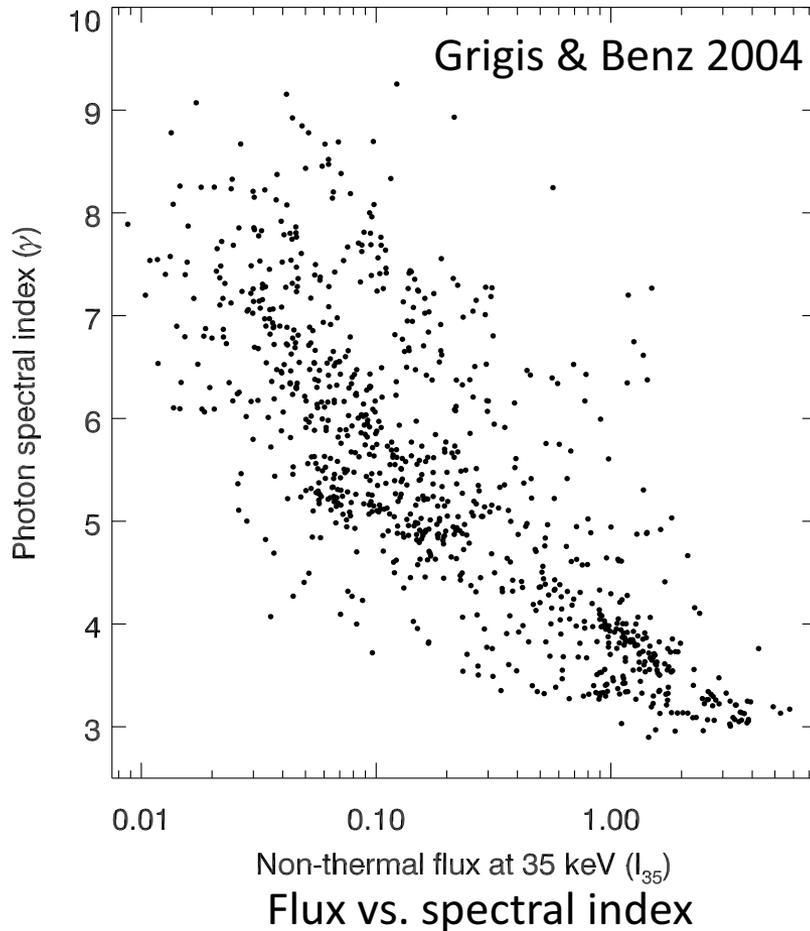
$$f(\mathbf{v}) \propto |\mathbf{v}|^{-\xi} \quad \xi = \frac{e^2 n \Lambda \bar{k}}{\pi \varepsilon_{\text{turb}}}$$

- Stronger turbulence  $\rightarrow$  harder spectrum
- Longer trapping time  $\tau \rightarrow$  harder spectrum

Grigis & Benz 2006

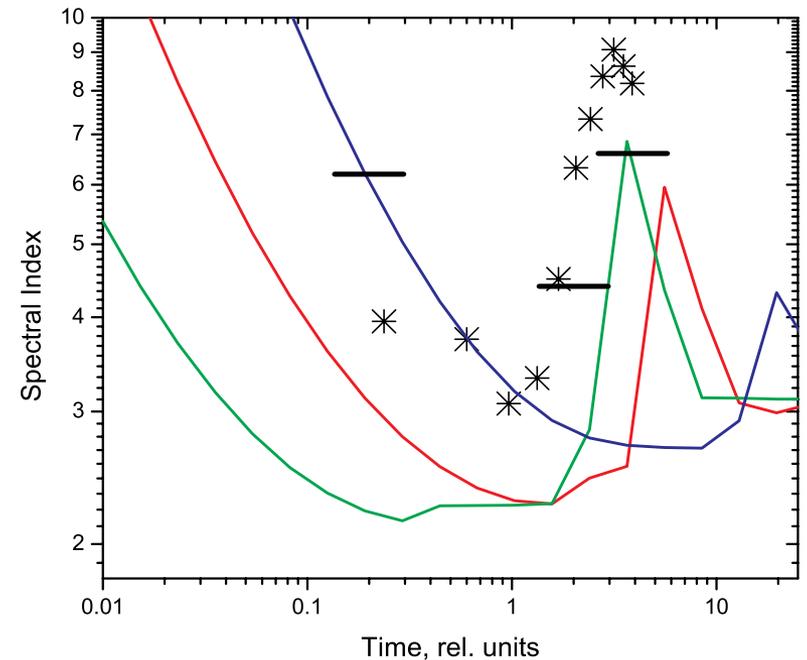


# Modeling HXR flux vs. spectral index



# So what causes the SHS behavior?

- Stochastic acceleration  
example: variation of the level of turbulence during the particle acceleration process
  - Energy release  $\rightarrow$  strong turbulence
  - Efficient particle acceleration  $\rightarrow$  harder spectrum
  - Turbulence exhausted
  - Less efficient particle acceleration  $\rightarrow$  softer spectrum
- Shock? DC electric field?
- How about SHH?



Bykov & Fleishman 2009

# Summary

- HXR and microwave observations provide critical diagnostics for particle acceleration mechanisms
  - Low-energy cutoff → number, energetics
  - Spectral breaks
  - Spectral evolution
- Some success in interpreting the observed phenomena
- But more are unexplained
- What can be improved?
  - More advanced instrumentation: HXR/microwave imaging spectroscopy with high spatial, spectral, and temporal resolution
  - Data-driven, self-consistent particle acceleration modeling