

Name: _____

Student #: _____

Must show all work to receive full credit!!!

1. How many 5-digit numbers can be formed from the integers 1, 2, ..., 9 if no digit can appear more than twice? (For instance, 41434 is not allowed.) (12 points)
(Self-test problems and exercises #10, page 20)

- 1

3. Let X_1 be Gamma with $(\lambda = 7, \alpha = 4)$ and X_2 be Gamma with $(\lambda = 7, \alpha = 5)$. If X_1 and X_2 are independent derive the distribution of $Y = X_1 + X_2$. (12 points)
(Done in class for general case, also on page 254-255)
4. Let $f(x, y) = 24xy$ $0 \leq x \leq 1, 0 \leq y \leq 1, 0 \leq x + y \leq 1$ and let it equal zero otherwise.
- (a) Compute the marginal density of X.
 - (b) Compute the probability $P(X < 2Y)$
 - (c) Is X independent of Y? Why or why not? (18 points)

5. If X_1 and X_2 are independent exponential random variables, each having parameter λ find the joint density function of $Y_1 = X_1 + X_2$ and $Y_2 = e^{X_1}$. (12 points) (page 290, #6.58)

6. Let X and Y have joint density given by

$$f(x, y) = \begin{cases} 2e^{-2x}/x, & 0 \leq x < \infty, 0 \leq y \leq x, \\ 0, & \text{elsewhere.} \end{cases}$$

Compute $E(XY)$, $E(X)$ and $E(Y)$ (10 points) (7.4, page 373 and 7.38, page 375)

7. Suppose that a die is rolled twice. Find the probability mass function associated with the random variable X : minimum value to appear in the two rolls. Compute the variance of X . (14 points) (4.7 and 4.8 (b) page 173)

8. A parallel system functions whenever at least one of its components works. Consider a parallel system of n components, and suppose that each component works independently with probability $1/3$. Find the conditional probability that component 1 works given that the system is functioning. (10points)