

2. **Version A** (a) Proportion defective = 0.05

Let X = no. of defectives in a sample of 40, $X \sim \text{Bin}(x; n = 40, p = 0.05)$

$$\begin{aligned} P(\text{accepting the box}) &= P(X \text{ is no more than } 1) = P(X = 0) + P(X = 1) \\ &= 0.95^{40} + (40)0.95^{39}(0.05) \\ &= 0.1285 + 0.2706 = 0.3991 \end{aligned}$$

(b) Proportion defective = 0.1

Let X = no. of defectives in a sample of 40, $X \sim \text{Bin}(x; n = 40, p = 0.1)$

$$\begin{aligned} P(\text{accepting the box}) &= P(X \text{ is no more than } 1) = P(X = 0) + P(X = 1) \\ &= 0.9^{40} + (40)0.9^{39}(0.1) \\ &= 0.0148 + 0.0657 = 0.0805 \end{aligned}$$

$$P(\text{rejecting the box}) = 1 - P(\text{accepting the box}) = 1 - 0.0805 = 0.9195$$

2. **Version B** (a) Proportion defective = 0.07

Let X = no. of defectives in a sample of 40, $X \sim \text{Bin}(x; n = 40, p = 0.07)$

$$\begin{aligned} P(\text{accepting the box}) &= P(X \text{ is no more than } 1) = P(X = 0) + P(X = 1) \\ &= 0.93^{40} + (40)0.93^{39}(0.07) \\ &= 0.0549 + 0.1652 = 0.2201 \end{aligned}$$

(b) Proportion defective = 0.14

Let X = no. of defectives in a sample of 40, $X \sim \text{Bin}(x; n = 40, p = 0.14)$

$$\begin{aligned} P(\text{accepting the box}) &= P(X \text{ is no more than } 1) = P(X = 0) + P(X = 1) \\ &= 0.86^{40} + (40)0.86^{39}(0.14) \\ &= 0.0024 + 0.0156 = 0.0180 \end{aligned}$$

$$P(\text{rejecting the box}) = 1 - P(\text{accepting the box}) = 1 - 0.0180 = 0.9820$$