A corporate website contains errors on 100 of its 1000 pages. If 40 pages are sampled randomly, without replacement, approximate the probability that at most 2 of the pages has errors in the sample. (10 pts)

Let $X$: the number of pages with error out of $n = 40$.

Note that $p = 100/1000 = 0.10$.

Therefore, $\mu = (40)(0.10) = 4$ and $\sigma^2 = 4(0.90) = 3.6$, $\sigma = 1.897366596$.

$P(X \leq 2) = P(X \leq 2.5) = P(Z \leq (2.5-4)/1.897366596) = P(Z \leq -0.79) = 0.214767 \approx 22\%$.

Using Binomial model:

$P(X \leq 2) = f(0) + f(1) + f(2) = (0.90)^{40} + (40)(0.10)(0.90)^{39} + \binom{40}{2}(0.10)^2(0.90)^{38}$

$= (0.90)^{38}(0.81 + 3.6 + 7.8) = (0.90)^{38}(12.21) = 0.222808124 = 22.28\%$