

Math 341, Quiz 7, Spring 2009, Name _____
Student # _____

Wednesday, May 6. *Please show the complete solution (with all steps) to the problem to receive full credit.*

A manufacturer of hard safety hats for construction workers is concerned about the mean and variation of the forces its helmets transmit to wearers when subjected to a standard external force. The manufacturer desires the mean force transmitted by helmets to be 800 pounds (or less), well under the legal 1000-pound limit, and desires σ to be less than 40. Tests were run on a random sample of $n = 40$ helmets, and the sample mean and variance were found to be equal to 825 pounds and 2350 pounds², respectively. Do the data provide sufficient evidence to indicate σ exceeds 40? Test at $\alpha = 0.01$ level.

$H_0: \sigma = 40$

$H_a: \sigma > 40$.

$$\chi^2 = [(n-1) s^2] / 40^2 = [39 (2350)] / 1600 = 57.28125.$$

The right tail test critical value is given by $\chi^2_{0.01, \text{d.f.} = 39}$, which is approximately the same as that of $\chi^2_{0.01, \text{d.f.} = 40}$, which from the tables = 63.6907. RR for right tail test is given by $\chi^2 > 63.6907$. Since $57.28125 < 63.6907$, do not reject $H_0: \sigma = 40$.