PHYS 122-Lecture 5: Electric Potential Energy

- Gravitational Potential Energy vs. Gravitational Potential
- Electric Potential Energy vs. Electric Potential

Electric potential energy in a uniform field

- The behavior of a point charge in a uniform electric field is analogous to the motion of a baseball in a uniform gravitational field.
- Figures 23.1 and 23.2 below illustrate this point.



A positive charge moving in a uniform field

If the positive charge moves in the direction of the field, the potential energy decreases, but if the charge moves opposite the field, the potential energy increases.

 $f = q_0 E$

Figure 23.3 below illustrates this point.



A negative charge moving in a uniform field

- If the negative charge moves in the direction of the field, the potential energy *increases*, but if the charge moves opposite the field, the potential energy *decreases*.
- Figure 23.4 below illustrates this point.



Electric potential energy of two point charges

- Follow the discussion of the motion of a test charge q_0 in the text.
- The electric potential is the same whether q_0 moves in a radial line (left figure) or along an arbitrary path (right figure).





Electric potential

- *Potential* is *potential energy per unit charge*.
- We can think of the potential difference between points *a* and *b* in either of two ways. The potential of *a* with respect to $b (V_{ab} = V_a V_b)$ equals:
 - ✓ the work done by the electric force when a *unit* charge moves from a to b.
 - ✓ the work that must be done to move a *unit* charge slowly from *b* to *a* against the electric force.
- Follow the discussion in the text of how to calculate electric potential.

Finding electric potential from the electric field

- If you move in the direction of the electric field, the electric potential *decreases*, but if you move opposite the field, the potential *increases*. (See Figure 23.12 at the right.)
- Follow the discussion in the text.
- Follow Example 23.3.

(a) A positive point charge



$$if \quad F = \frac{1}{4\pi\epsilon_{o}} \frac{|\ell||_{20}}{r^{2}}$$

$$W = \int_{a}^{b} F \cdot d\ell = \int_{a}^{b} \frac{1}{4\pi\epsilon_{o}} \frac{|\ell||_{20}}{r^{2}} \frac{a_{s}\phi d\ell}{dr} = \frac{|\ell||_{20}}{4\pi\epsilon_{o}} \left(\frac{1}{\epsilon_{o}} - \frac{1}{\epsilon_{b}}\right)$$

$$if \quad \Gamma_{b} = \infty$$

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$$U_{T} = \frac{1}{4\pi\epsilon_{o}} \frac{|\ell||_{20}}{r} = \frac{1}{4\pi\epsilon_{o}} \frac{2}{r}$$

$$U_{T} = \frac{1}{2}U;$$

$$if \quad \Gamma_{b} = \infty$$

$$\frac{1}{|\ell_{0}|} = \frac{1}{4\pi\epsilon_{o}} \frac{|\ell_{1}|}{r} \equiv V = \frac{1}{4\pi\epsilon_{o}} \frac{2}{r}$$

$$Note: No Vectors!$$

V= 1 - 2 - F V= EV: = Etito E: = (the de Because W= SF.Jl = StoF.Jl = $\frac{W}{q_0} = \left(V = \int E \cos \phi \, d\ell \right)$ Have E -> get V this is backwards to "real life" Ê=-VV

Potential due to two point charges

- Follow Example 23.4 using Figure 23.13 at the right.
- Follow Example 23.5.



Potential due to two point charges

- Follow Example 23.4 using Figure 23.13 at the right.
- Follow Example 23.5.



a)
$$V_{q} = V_{1} + V_{2}$$

 $= \frac{1}{4\pi\epsilon_{0}} \frac{q_{1}}{r_{1}} + \frac{1}{4\pi\epsilon_{0}} \frac{q_{2}}{r_{2}}$
 $= -900[V]$
($U_{q} = q V_{q} = -3.6.10^{-6} (J]$)
 $= NO Vectors$

Finding potential by integration

• Example 23.6 shows how to find the potential by integration. Follow this example using Figure 23.14 at the right.



Finding potential by integration



An infinite line charge or conducting cylinder

• Follow Example 23.10 using Figure 23.19 below.



An infinite line charge or conducting cylinder

Follow Example 23.10 using Figure 23.19 below.





Equipotential surfaces and field lines

- An *equipotential surface* is a surface on which the electric potential is the same at every point.
- Figure 23.23 below shows the equipotential surfaces and electric field lines for assemblies of point charges.
- Field lines and equipotential surfaces are always mutually perpendicular.



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Equipotentials and conductors

- When all charges are at rest:
 - \checkmark the surface of a conductor is always an equipotential surface.
 - the electric field just outside a conductor is always perpendicular to the surface (see figures below).
 - the entire solid volume of a conductor is at the same potential.



An impossible electric field If the electric field just outside a conductor had a tangential component E_{\parallel} , a charge could move in a loop with net work done.

