

# WEEK 1

Engineering Calculations –  
Processes – Process Variables

# 2.1 Units and Dimensions

- Units and dimensions are important in science and engineering
- A measured quantity has a numerical value and a unit (ex: 25°C)
- Dimension: Length, time, mass or temperature - These are properties that can be measured or obtained by multiplying other dimensions (ex: velocity = Length/time; volume = Length<sup>3</sup>)

Note: If the units are the same, they can be added or subtracted (ex: 3 cm- 1 cm). If they are different, conversion is required in order to obtain the same units.

# 2.2 Unit Conversion

- Measured quantity  $\rightarrow$  Unit having appropriate dimension.

Ex: Volume  $\rightarrow$  3 cm<sup>3</sup>  $\rightarrow$  Length<sup>3</sup>

Measure quantity  $\rightarrow$  numerical value, proper unit  $\rightarrow$  proper dimension

Note: The numerical value depends on the unit.

(Inside cover of the book)

- To convert from one unit to another, we multiply by a “conversion factor”

Ex: 36 mg (1g/1000 mg) = 0.036 g

36 mg (0.001g/1 mg) = 0.036 g

Note: The old units should cancel out. All we have left is the desired unit.

- We also deal with compound units (Ex: miles/h). These units are formed by combining different dimensions (Ex: **to do in class**: 1 cm/s<sup>2</sup> in km/yr<sup>2</sup>)

# 2.3 Systems of Units (SI, American Engineering System)

- Base units are units for mass, length, time, temperature, electrical current and light intensity (Page 11 in the textbook).

Ex1: Quantity: temperature, Base unit: Kelvin (SI), symbol: K.

Ex2: Quantity: time, Base unit: second, symbol: s.

- Multiple units: multiple or fraction of base units such as hours, milliseconds, year etc... Multiple unit prefixes are: Mega (M) =  $10^6$ , Kilo (k) =  $10^3$ , Centi (c):  $10^{-2}$ , Milli (m) =  $10^{-3}$ , Micro ( $\mu$ ) =  $10^{-6}$ , Nano (n) =  $10^{-9}$ .

Note: There are quantities which require derived units. It is imperative that we recognize units associated with quantities.

Ex: volume  $\rightarrow$  liter  $\rightarrow$  l or L

Force  $\rightarrow$  Newton (SI), dyne (CGS)  $\rightarrow$  N

Pressure  $\rightarrow$  pascal (SI)  $\rightarrow$  Pa

Energy, work  $\rightarrow$  joule (SI)  $\rightarrow$  J

Power  $\rightarrow$  watt  $\rightarrow$  W

Conversion:  $W = 1 \text{ J/s} = 1 \text{ kg}\cdot\text{m}^2/\text{s}^3$  ;  $1 \text{ N} = 1 \text{ kg}\cdot\text{m}/\text{s}^2$

Example: Conversion between systems of units:  $23 \text{ lbf}\cdot\text{ft}/\text{min}^2$  in  $\text{kg}\cdot\text{cm}/\text{s}^2$

# 2.4 Force and Weight

- For now, we are interested in force and weight in the context of units and unit conversion

- Force is proportional to mass X acceleration

SI:  $\text{kg}\cdot\text{m}/\text{s}^2$

CGS:  $\text{g}\cdot\text{cm}/\text{s}^2$

American engineering:  $\text{lbm}\cdot\text{ft}/\text{s}^2$

1 Newton (N) = 1  $\text{kg}\cdot\text{m}/\text{s}^2$  (SI)

1 dyne = 1  $\text{g}\cdot\text{cm}/\text{s}^2$  (CGS)

1 lbf = 32.174  $\text{lbm}\cdot\text{ft}/\text{s}^2$  (American engineering)

(acceleration of gravity at sea level and 45° latitude)

Conversion factors: 1  $\text{kg}\cdot(\text{m}/\text{s}^2)/\text{N}$ , 1  $\text{g}\cdot(\text{cm}/\text{s}^2)/\text{dyne}$ , 32.174  $\text{lbm}\cdot(\text{ft}/\text{s}^2)/\text{lbf}$

- Weight is force exerted on an object by gravitational acceleration

$$W = m g$$

$$g = 9.8066 \text{ m}/\text{s}^2 = 980 \text{ cm}/\text{s}^2 = 32.174 \text{ ft}/\text{s}^2$$

- There is a distinction between weight and mass (**Go over example 2.4-1 on page 13 in class**)

# 2.5 Numerical Calculations and Estimations

- Scientific notation, significant figures, and precision:  $a \times 10^b$  (b is a negative or positive integer)  
Ex:  $123,000,000 = 1.23 \times 10^8$ ;  $0.000028 = 2.8 \times 10^{-5}$

Significant figures:

a) **There is a decimal point:** 0.000028 (2 significant figures)

First nonzero digit on the left to the last digit (zero or nonzero) on the right

b) **There is no decimal point:** 123000000 (3 significant figures)

First nonzero digit on the left to the last nonzero digit of the number

More examples: 2300 : 2; 2300. : 4; 2300.0 : 5; 23040 : 4; 0.035 : 2; 0.03500 : 4.

When using scientific notations, make sure that the significant digits are shown.

$2.3 \times 10^3$ ;  $2.300 \times 10^3$ ;  $2.3000 \times 10^3$ ;  $2.304 \times 10^4$ ;  $3.5 \times 10^{-2}$ ;  $3.500 \times 10^{-2}$ .

Note: high precision: close to each other

High accuracy: very near the target

Significant figures have to do with precision of a reported (or measured) quantity.

Ex1: 3 significant figures: the value of the third of the figures may be off by as much as one half.

Ex2: 8.3 g lies between 8.25 g and 8.35 g

Ex3: 8.300 g lies between 8.2995 g and 8.3005 g

# 2.5 Numerical Calculations and Estimations

- When doing multiplication or division, keep the lowest number of significant figures of any of the multiplicands or divisors.

$$\text{Ex1: } \underset{(3)}{3.57} \times \underset{(4)}{4.286} = 15.30102 = \underset{(3)}{15.3}$$

$$\text{Ex2: } \underset{(2)}{(5.2 \times 10^{-4})} \underset{(4)}{(0.1635 \times 10^7)} / \underset{(3)}{2.67} =$$
$$\underset{(9)}{318.426966} = \underset{(2)}{3.2 \times 10^2} = 320$$

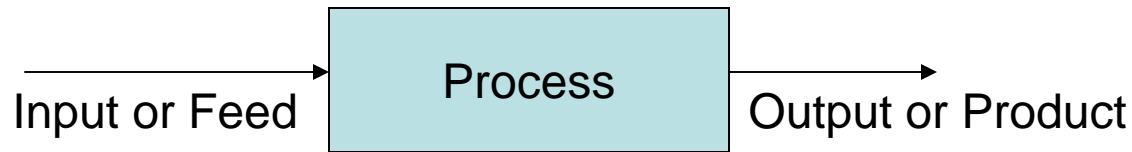
- Addition and subtraction: the number of decimal places in the answer = the number of decimal places in the *quantity with the smallest number of decimal places*

$$\text{Ex: } \underset{(3)}{(2.75 \times 10^6)} + \underset{(4)}{(3.400 \times 10^4)} = \underset{(3)}{2.78 \times 10^6}$$

Note: Equations must be dimensionally homogeneous (End of Chapter 2)

# Chapter 3

- Processes and process variables
- “Process”: any operation or series of operations that causes a physical or chemical change in a substance or a mixture of substances



- “Process Unit”: apparatus in which one of the operations that constitutes of a process is carried out

Examples of “process units” reactors, distillation columns, heat exchanger

We need to introduce definitions and measurement techniques to help understand and design process units



# Chapter 3

- Density: mass/volume of substance ( $\text{kg}/\text{m}^3$ ,  $\text{g}/\text{cm}^3$ ,  $\text{lbm}/\text{ft}^3$ )
- Specific volume of a substance: volume of substance/mass ( $\text{m}^3/\text{kg}$ ,  $\text{cm}^3/\text{g}$ ,  $\text{ft}^3/\text{lbm}$ )

Density of solid and liquid are weak functions of temperature and pressure.

Ex1: density of carbon tetrachloride:  $1.595 \text{ g}/\text{cm}^3$

Ex2: mass of  $20.0 \text{ cm}^3$  of carbon tetrachloride?  
 $20.0 \text{ cm}^3 \times 1.595 \text{ g}/\text{cm}^3 = 31.9 \text{ g}$

Ex3: volume of  $6.20 \text{ lbm}$  of tetrachloride:  $6.20 \text{ lbm} \times (454\text{g}/1\text{lbm}) \times (1\text{cm}^3/1.595 \text{ g}) = 1760 \text{ cm}^3$

# Chapter 3

- “Specific gravity” of a substance:  $SG = \rho/\rho_{ref}$ .  $\rho_{ref}(H_2O, 4^\circ C) = 1.000 \text{ g/cm}^3 = 1000 \text{ kg/m}^3 = 62.43 \text{ lbm/ft}^3$ .  $SG = 0.6 \text{ } 20^\circ/4^\circ$  (**Example 3.1-1 in class**)

- 3.2 Flow rate: Mass and volumetric flow rate

-Flow rate of a material = rate at which a material is transported through a process line. Mass flow rate (mass/time); volumetric flow rate (volume/time)

- How do we measure flow rate? (**Page 46: rotameter - float and orifice meter – pressure drop**).

- 3.3 Chemical composition

Moles and molecular weights. Atomic weight of an element = mass of an atom. Molecular weight of a compound = sum of the atomic weights of all the atoms that make up the molecule of the compound

Ex: atomic weight (O): 16; Molecular weight of  $O_2$  is about 32.

Unit: 1 gram-mole (g-mole or mole in SI) = amount of that species (# moles) that is numerically equal to its molecular weight. Instead of g-mole, we may write moles (ex: 2 g-moles = 2 moles)

Ex: Carbon monoxide (CO) = 28 g/mole -> 1 g-mole of CO contains 28 g. Also 1 lb-mole of CO contains 28 lbm

Conversion:  $34 \text{ kg NH}_3 \times (1 \text{ kmol}/17 \text{ kg NH}_3) = 2 \text{ kmol NH}_3$   
 $4 \text{ lb-mole NH}_3 \times (17 \text{ lbm}/1 \text{ lb-mole NH}_3) = 68 \text{ lbm NH}_3$

**In class Page 48 Example 3.3-1**

# Chapter 3

- Notes: Avogadro's number:  $6.02 \times 10^{23}$  molecules/mole
  - Molecular formula:  $C_xO_y$  means x mole of C and y mole of O. But we have 1 mole of  $C_x$  and 1 mole of  $O_y$ . Also: 1 mole of  $C_xO_y$ .

## Mass, mole fractions and average molecular weight

Mass fraction =  $X_A$  = mass of A/total mass

Mole fraction =  $Y_A$  = mole of A/total moles

### **Example 3.3.2 to do in class**

In this example, we use conversion of mass and mole fractions.

You are giving mass %. 1) Use 100 (g, kg, lbm) basis, 2) Obtain the mass, 3) Convert mass to moles using molecular weight.

When giving mole %, the procedure is similar.

# Chapter 3

- Average molecular weight (or mean molecular weight) of a mixture:  $\bar{M}$  (kg/Kmol or lbm/lbmol).

$$\bar{M} = y_1M_1 + y_2M_2 + \dots = \sum y_iM_i$$

- $M_i$ : molecular weight of compound  $i$ ;  $y_i$ : mole fraction of compound  $i$ .

$$\frac{1}{\bar{M}} = \frac{x_1}{M_1} + \frac{x_2}{M_2} + \dots = \sum \frac{x_i}{M_i}$$

$x_i$ : mass fraction of  $i$

- **Example 3.3-4 page 51 to do in class**

# 3.4 Pressure

- 3.4a Fluid pressure and hydrostatic head:

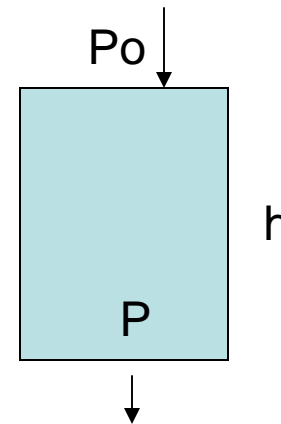
$$P = F/A = \text{N/m}^2; \text{ dynes/cm}^2; \text{ lbf/in}^2$$

$$1 \text{ N/m}^2 = 1 \text{ pascal (Pa)}$$

$$P = P_o + \rho gh$$

$P$  is the hydrostatic pressure of the fluid

“Head” of a particular fluid  $P_{\text{head}} = \rho_{\text{fluid}}gh$



## Example 3.4-1 page 55 to do in class

We need to use  $1 \text{ N} = 1 \text{ kg.m/s}^2$ ;  $1 \text{ dyne} = 1 \text{ g.cm/s}^2$ ;  $1 \text{ lbf} = 32.174 \text{ lbf.ft/s}^2$  to obtain proper units.

- 3.4b Atmospheric pressure, absolute pressure and gauge pressure:  $P_{\text{abs}} = P_{\text{gauge}} + P_{\text{atmospheric}}$
- 3.4c Fluid pressure measurement: Bourdon gauge; Manometer. **Read Page 58 and 59**

# 3.5 Temperature

- $T(\text{K}) = T(^{\circ}\text{C}) + 273.15$
- $T(^{\circ}\text{R}) = T(^{\circ}\text{F}) + 459.67$
- $T(^{\circ}\text{R}) = 1.8 T(\text{K})$
- $T(^{\circ}\text{F}) = 1.8 T(^{\circ}\text{C}) + 32$

**HMK: 2.2, 2.3, 2.8, 2.9, 3.2, 3.3, 3.14**