

**CS 341, Fall 2011**  
**Solutions for Quiz 1, Day Section**

1. (a)  $aa, ab, aaa, aab, baa, bab$
- (b)  $A$  is closed under concatenation. To prove this, let  $w_1$  and  $w_2$  be arbitrary strings in  $A$ . Then  $|w_1| \geq 2$ ,  $|w_2| \geq 2$ , and the second-to-last symbol of both strings is  $a$ . Then the concatenation  $w_1w_2$  satisfies  $|w_1w_2| \geq 4 > 2$  and the second-to-last symbol of the concatenation is the same as the second-to-last symbol of  $w_2$ , which is  $a$ . Thus,  $w_1w_2 \in A$ , so  $A$  is closed under concatenation.
- (c) A DFA for  $A$  is below:

