

# Packet-Pair Sizing for Controlling Packet Dispersion on Wired Heterogeneous Networks

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**Abstract**—The packet-pair structure is a widely used probing technique for measuring link capacity over network paths. In packet-pair probing, the probe-gap value at the link of interest (e.g., the link with the smallest capacity or any link along a path) is determined for link-capacity measurement, which can be affected if dispersion (i.e., separation) of the packet pair is created by the heterogeneous link capacities and cross traffic over an end-to-end path. In this paper, we present an analytical model concerning the effect of heterogeneous link capacities and cross traffic on the packet-pair structure over a multiple-hop path, and define the constraints on the packet sizing for accurate end-link (i.e., the link connected to the destination node of an end-to-end path) capacity measurement. We test the model through numerical evaluations and experimentally, on end-to-end paths with heterogeneous links and different cross traffic loads. The experiments are performed on a testbed and in the Internet.

**Index Terms**—Active probing, packet pair, packet sizing, link capacity, analytical model.

## I. INTRODUCTION

Packet-pair structure is a widely used probing technique for measuring link capacity of network paths [1]–[6]. In packet-pair probing, two packets are sent from the source node to the destination node of an end-to-end path to measure the probe gap of the packet pair at the link of interest (e.g., the narrow link, the smallest link capacity, or any link along the path) for capacity measurement. The accuracy of link-capacity measurement based on the probe gap can be affected if additional dispersion (i.e., separation) in the packet-pair structure is created by the heterogeneous link capacities and cross traffic of the path [4].

The sizes of probing packets in the packet-pair structure is an important parameter for link-capacity measurement, and the effect of link heterogeneity and cross traffic on the measurement accuracy can be reduced if suitable packet sizes are used over a path [2]–[4]. In this paper, we present an analytical model concerning the effect of heterogeneous link capacities and cross traffic on the packet-pair structure as it travels over a multiple-hop path and define the constraints on the packet sizing for accurate end-link (i.e., the link connected to the destination node of an end-to-end path) capacity measurement.

The remainder of the paper is organized as follows: In Section II, we discuss existing link-capacity measurement schemes. In Section III, we present a packet-pair structure. In Section IV, we present an analytical model for sizing the probing packets in the packet-pair structure and verify the model through numerical evaluations. In Section V, we show experimental results of end-link capacity measurement over testbed and Internet paths. In Section VI, we conclude the discussion.

## II. RELATED WORK

A plethora of packet-pair based schemes to measure link capacity have been proposed [1]–[6]. Because we aim to estimate the end-link capacity of a path in this paper, we limit the discussion to two prominent per-hop measurement schemes, which measures the capacities of all links along a path, that may be applicable to that case.

Nettimer is an early per-hop scheme to measure link capacities of an end-to-end path based on tailgating technique, where a small packet tailgating a large packet is sent back-to-back from the source node to the destination node [2]. The one way delay (OWD) of the small packet in the packet pair is used for capacity estimation. In the tailgating technique, the large packet is dropped right before reaching the link of interest and the small packet is left to continue toward the destination node to identify the contribution to OWD of the link of interest. Although the probe gap of the packet-pair structure is not considered in Nettimer, this scheme requires that the packet pair hold a zero-dispersion gap before arriving at the link of interest to avoid measurement error due to link heterogeneity and cross traffic over the path. However, it is unclear whether a packet pair could keep a zero-dispersion gap throughout the path as no analytical model was presented. The reported implementation of Nettimer shows around 50% measurement accuracy [2].

Different from the traditional per-hop scheme approach, Cartouche probing measures the capacities of target links in a segment of a path under interest [5]. This scheme sends a train of probing packets in pairs, where each pair consists of a large packet tailgated by a small packet, similar to the single packet pair in Nettimer. All the packets in the probing train are dropped before reaching the link of interest while the small packets of the first and last packet pairs reach the destination node. The scheme measures the gap between the small packets at the destination node for capacity estimation. The accuracy of the scheme depends on the size of the probing train (i.e., number of packet pairs), which depends on the ratios of the link capacities along the path. It is reported that the scheme has been tested under low cross-traffic loads [5].

## III. COMPOUND PROBE

Figure 1 shows a packet-pair structure comprising two probing packets: a heading packet ( $P_h$ ) followed by a trailing packet ( $P_t$ ) [2], and we call this a compound probe [7], [8]. The sizes of  $P_h$  and  $P_t$  are denoted as  $s_h$  and  $s_t$ , respectively. The gap in between the last bit of  $P_h$  and the last bit of

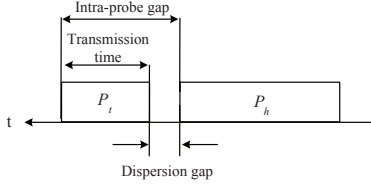


Fig. 1. Compound-probe structure.

$P_t$  is called the *intra-probe gap*,  $G(s_t)$ , which includes the transmission time of  $P_t$ .

The two probing packets in the compound probe are used to identify the beginning and the end of  $P_t$  (i.e., the transmission time of the trailing packet) as the time-stamping process records the arrival time at which a packet has been received successfully. To determine the transmission time of  $P_t$  on the end link of a path from  $G(s_t)$ , the dispersion gap between  $P_h$  and  $P_t$  (i.e., the separation between the last bit of  $P_h$  and the first bit of  $P_t$ ) is required to be zero at the time of arrival in the destination node.

In a compound probe, gap dispersion (i.e., the increment of the dispersion gap) can occur if one or two of the following events occur: 1) if the packet-size ratio of the compound probe,  $\alpha = \frac{s_h}{s_t}$ , is smaller than the link-capacity ratio of the input and output links of a network node  $i$ ,  $lr_i = \frac{l_{i+1}}{l_i}$ , or 2) one or more cross-traffic packets are enclosed between  $P_h$  and  $P_t$ . Because event 2 is out of our reach, we mainly focus on event 1. According to event 1, if the transmission time of  $P_h$  at the output link is smaller than the transmission of  $P_t$  at the input link of a network node, the compound probe experiences dispersion [2], [5]. Therefore, at the network node  $i$ , the packet-size ratio  $\alpha$  between  $P_h$  and  $P_t$  to avoid gap dispersion must follow

$$\alpha \geq \frac{l_{i+1}}{l_i}. \quad (1)$$

For end-link capacity measurement, a zero-dispersion gap is required at the end link of the followed path. This requirement can be achieved even if a dispersion gap is created along the path but it becomes zero before reaching the end link (e.g., due to a link-capacity ratio smaller than 1). To avoid uncertainty, a model to ensure the above requirement considering the link heterogeneity and cross traffic of the path is required.

#### IV. SIZING OF PROBING PACKETS

In this section, we present an analytical model for sizing  $P_h$  and  $P_t$  to ensure a zero-dispersion gap on the end link of a path considering the effects of link heterogeneity and cross traffic on intermediate links. Different from [2], our model considers cross traffic and an end-to-end path.

##### A. Sizing of Probing Packets and Link Heterogeneity

Consider that the link capacities between node 0 (*src*) and node  $n$  (*dst*) along a  $n$ -hop path are  $l_1, \dots, l_n$ , as shown in Figure 2. To keep a zero-dispersion gap between  $P_h$  and  $P_t$  at *dst*, the following equation applies:

$$\left(\frac{s_h}{l_n} - \frac{s_h}{\alpha l_{n-1}}\right) + \left(\frac{s_h}{l_{n-1}} - \frac{s_h}{\alpha l_{n-2}}\right) + \dots + \left(\frac{s_h}{l_{z+1}} - \frac{s_h}{\alpha l_z}\right) = 0 \quad (2)$$

where  $\frac{s_h}{\alpha} = s_t$ , and  $l_z$  is the capacity of a link connected to a node  $z$ , such that  $lr_z = \frac{l_{z+1}}{l_z}$  is the largest link-capacity ratio along the path, located after the narrow link (in the direction from *src* to *dst*) and that  $l_z$  also is the link closest to *dst* (e.g., if two nodes following the narrow link closest to *dst* of the path have the largest link-capacity ratio, the node located the closest to *dst* is selected). Therefore, the index  $z$  is such that  $1 \leq z \leq (n-1)$ . Equation (2) is valid as long as the narrow link is not the end link of the path.

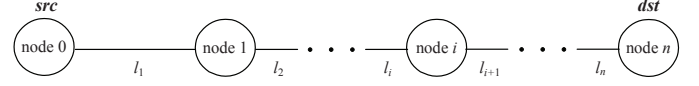


Fig. 2.  $n$ -hop end-to-end path.

The largest size of  $P_t$  is calculated from (2) as:

$$s_t = s_h \frac{\sum_{j=z+1}^n \frac{1}{l_j}}{\sum_{j=z}^{n-1} \frac{1}{l_j}} \quad (3)$$

When the end-link capacity  $l_n$  is the path's narrow link, the required condition to achieve a zero-dispersion gap is:

$$\frac{s_h}{l_n} - \frac{s_h}{\alpha l_{n-1}} = 0 \quad (4)$$

and the largest size of  $P_t$  is calculated as:

$$s_t = \frac{s_h}{l_n} l_{n-1} \quad (5)$$

The rationale behind (2) and (4) is that a compound probe may experience the largest dispersion at a network node over a path where the link-capacity ratio is the largest and the packet-size ratio is smaller than the largest link-capacity ratio. Therefore,  $s_t$  is determined with respect to  $s_h$  by finding a suitable packet-size ratio so that the dispersion gap reduces to zero upon arriving at node  $n$ .

##### B. Sizing of Probing Packet and Cross-Traffic Effect

Figure 3 shows an example of a compound probe forwarded from the input link to the output link by node  $i$  when two cross-traffic packets, denoted by  $D_h$  and  $D_t$ , intrude the compound probe. The capacity of the input and output links are  $l_i$  and  $l_{i+1}$ , respectively, where  $l_i < l_{i+1}$  in this example. Here,  $P_h$  and  $P_t$  arrive at node  $i$  with a zero-dispersion gap. However, the compound probe experiences dispersion at the output link, as shown by the dispersion gap in the figure.

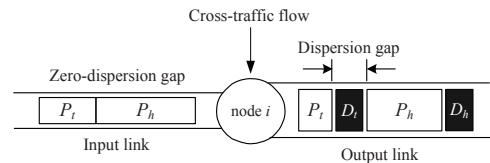


Fig. 3. Forwarding of a compound probe by node  $i$  from its input link to its output link.

The intra-probe gap of the compound probe at the output link of node  $i$  is defined as:

$$G(s_t)_{i+1} = \frac{s_t}{l_{i+1}} + \delta_{i+1}, \quad (6)$$

where the dispersion gap at the output link,  $\delta_{i+1}$ , is:

$$\delta_{i+1} = \begin{cases} \delta_i - \Delta tr(h, t)_i & \text{if } \delta_i - \Delta tr(h, t)_i > Qt_i \\ Qt_i & \text{else} \end{cases} \quad (7)$$

In the above equation,  $\delta_i$  is the dispersion gap at the input link of node  $i$ ,  $\Delta tr(h, t)_i$  is the difference between the transmission time of  $P_h$  plus the queuing delay ( $Qh_i$ ) caused by the cross-traffic packet(s) backlogged ahead of  $P_h$  at the output link and the transmission time of  $P_t$  at the input link of node  $i$ .  $Qt_i$  is the increment of the dispersion gap caused by the cross-traffic packet(s) inserted between  $P_h$  and  $P_t$  at node  $i$ . These terms are estimated as:

$$\Delta tr(h, t)_i = \frac{s_h}{l_{i+1}} + Qh_i - \frac{s_t}{l_i} \quad (8)$$

$$Qh_i = \sum_u \frac{\zeta_{u(i)}}{l_{i+1}}; \quad u \geq 0 \quad (9)$$

$$Qt_i = \sum_v \frac{\zeta_{v(i)}}{l_{i+1}}; \quad v \geq 0 \quad (10)$$

Here,  $\zeta_{u(i)}$  and  $\zeta_{v(i)}$  denote the sizes of the cross-traffic packets  $u$  and  $v$  ahead of  $P_h$  and  $P_t$  for  $Qh_i$  and  $Qt_i$ , respectively, at node  $i$ .

When node  $n$  of Figure 2 measures the intra-probe gap of the compound probe upon receiving it at the application layer, the measured intra-probe gap includes the interframe gap (IFG) [9] of the end link and it follows (6):

$$G(s_t)_n = \frac{s_t}{l_n} + \delta_n + IFG \quad (11)$$

### C. Numerical Evaluations of Packet-Sizing Model

We calculated the upper bounds of  $\alpha$  (i.e., the largest possible values of  $s_t$  against  $s_h$ ) needed to keep the dispersion gap at zero using (3) or (5) over a four-hop end-to-end path, considering different configurations for the link capacities, as shown in Table I. The four different configurations, each denoted as  $Cc$ - $R$  where  $c$  is the identification index for each of the four considered configurations and  $R$  is the capacity of the end link of configuration  $c$ , are C1-10, C2-100, C3-100, and C4-100. These configurations provide diversity of the link capacity assignments and the location of narrow link in each configuration is also different.

TABLE I  
TESTBED PATH CONFIGURATIONS AND ESTIMATED PACKET-SIZE RATIOS

| Path   | Link capacity ( $l_i$ )<br>(Mb/s) |       |       |       | Link-capacity ratio<br>( $lr_i = \frac{l_{i+1}}{l_i}$ ) |        |        | Packet-size ratio<br>( $\alpha = \frac{s_h}{s_t}$ ) |           |
|--------|-----------------------------------|-------|-------|-------|---------------------------------------------------------|--------|--------|-----------------------------------------------------|-----------|
|        | $l_1$                             | $l_2$ | $l_3$ | $l_4$ | $lr_1$                                                  | $lr_2$ | $lr_3$ | Calculated                                          | Evaluated |
| C1-10  | 100                               | 155   | 100   | 10    | 1.55                                                    | 0.645  | 0.1    | 1                                                   | 1         |
| C2-100 | 10                                | 155   | 10    | 100   | 15.5                                                    | 0.064  | 10     | 10                                                  | 10        |
| C3-100 | 100                               | 10    | 155   | 100   | 0.1                                                     | 15.5   | 0.645  | 6.49                                                | 6.67      |
| C4-100 | 10                                | 10    | 155   | 100   | 1                                                       | 15.5   | 0.645  | 6.49                                                | 6.67      |

To verify the calculated values, we evaluated the values of  $\alpha$  using the dispersion-gap model in Section IV-B, considering  $Qt_i$  and  $Qh_i$  equal to zero in (7) and (8). To evaluate with different  $\alpha$ s, the initial value of  $s_t$  is set to 50 bytes and it

is gradually increased by 25 bytes until the length of  $s_h = 1500$  bytes is reached. The last two columns of Table I show the lower bounds of both the calculated and evaluated values of  $\alpha$  for each configuration. Here, both the calculated and evaluated values were obtained by using a single compound-probe over each path configuration. According to Table I, the evaluated values are very close to the calculated ones; the calculated values of  $\alpha$  over C1-10 to C4-100 are 1 ( $s_t = 1500$  bytes), 10 ( $s_t = 150$  bytes), 6.49 ( $s_t = 232$  bytes), and 6.49 ( $s_t = 232$  bytes), respectively. The evaluated values of  $\alpha$  are 1 ( $s_t = 1500$  bytes), 10 ( $s_t = 150$  bytes), 6.67 ( $s_t = 225$  bytes), and 6.67 ( $s_t = 225$  bytes) over C1-10, C2-100, C3-100, and C4-100, respectively. The small over estimation in the evaluated values for C3-100 and C4-100 are produced by the 25-byte step increase of  $s_t$ , as stated above.

Figures 4(a)-4(d) show detailed information about the estimated end-link capacities over each path configuration using different values of  $\alpha$ , after considering  $IFG = 0$  in (11). The acceptable packet-size ratios are those representing the actual end-link capacity, as indicated by the arrows in the figures (where the zero-dispersion gap can be kept).

### D. Impact of Cross Traffic on Packet-Size Ratio

The impact of cross traffic in the measurement of end-link capacity was evaluated considering a symmetric cross-traffic load over the second and third links of each path configurations. In this evaluation, we considered the same values of  $\alpha$ , as used in Section IV-C, along with three different values for  $u$  and  $v$ , i.e., 1, 5, and 10 packets, each packet is 64 bytes, in (9) and (10). Figures 4(e)-4(h) show the estimated end-link capacities over C1-10 to C4-100, respectively. The estimated end-link capacities show that the cross-traffic interference increases the upper bounds of  $\alpha$  for accurate link-capacity measurement except over C1-10, where the end link is the narrow link of the path. For example, when  $P_h$  and  $P_t$  of the compound probe is interfered by a single cross-traffic packet (i.e., when  $u = 1$  and  $v = 1$ ), the upper bound of  $\alpha$  increases from 10 to 20 (i.e.,  $s_t$  decreases to 75 bytes) over C2-100, and from 6.67 to 8.57 (i.e.,  $s_t$  decreases to 175 bytes) over both C3-100 and C4-100, according to Figures 4(f)-4(h), respectively. Here, we can see that if the narrow link is other than the end link, cross traffic produces dispersion. Another observation is that a large  $\alpha$  simplifies the selection of the sizes of  $P_h$  and  $P_t$ . In this case, the largest value of  $\alpha$  achievable on Ethernet is sufficient to achieve a zero-dispersion gap in the considered path configurations.

## V. EXPERIMENTAL RESULTS

We tested the above analytical model to measure end-link capacity over testbed and Internet paths. We used Linux based commodity workstations as  $src$  and  $dst$  in the experimental paths. The specification of the workstation at  $dst$  is shown in Table II.

### A. Experimental Measurement on a Controlled Testbed

In the testbed experiment, we considered the first two path configurations, C1-10 and C2-100, of Table I because they have the smallest and the largest upper-bound values of  $\alpha$ , respectively, among the four listed path configurations. We

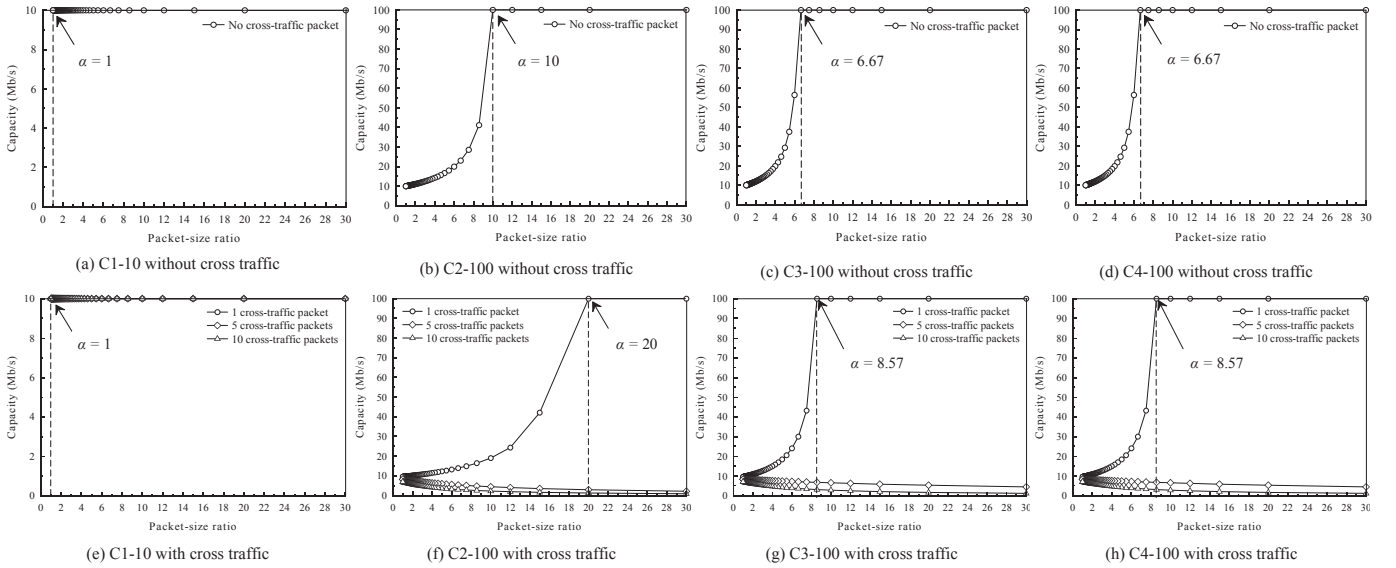


Fig. 4. Evaluation of packet-size ratio ( $\alpha$ ) to measure the end-link capacity ( $l_4$ ) of four different path configurations: (a) C1-10, (b) C2-100, (c) C3-100, and (d) C4-100 without cross-traffic load. (e) C1-10, (f) C2-100, (g) C3-100, and (h) C4-100 with cross-traffic load.

TABLE II  
SPECIFICATIONS OF THE WORKSTATION AT  $dst$

| Dell Inspiron 531S     |                                    |
|------------------------|------------------------------------|
| Name                   | 1531S                              |
| Processor (CPU speed)  | AMD Athlon 64 X2 Dual Core (1 GHz) |
| RAM size               | 1024 MB                            |
| RAM speed (data width) | 667 MHz (64 bits)                  |
| PCI bus speed          | 133 MB/s                           |
| Interface speed        | 10/100 Mb/s                        |
| Linux kernel version   | 2.6.18                             |

implemented these two paths on a testbed consisting of three Cisco routers, as intermediate nodes, and two Linux workstations, as  $src$  and  $dst$  (see Table II for the specifications). We also implemented a compound-probe based probing tool as an application on Linux system, which provides a clock with  $1\text{-}\mu\text{s}$  resolution for time stamping (based on the pcap library [10]). For end-link capacity measurement, we used two compound probes over each path having a common  $s_h$  and two different  $s_t$ s to test our analytical model. The value of  $s_h$  was determined by the maximum transmission unit (MTU) over each path: 1448 bytes of user datagram protocol (UDP) payload plus 54 bytes of Ethernet encapsulation at the end link (Ethernet encapsulation includes a 12-byte preamble, start of frame delimiter, SFD, and frame check sequence, FCS, fields). The values of  $s_t$  used in the two compound probes are 87 bytes and 112 bytes, respectively, since these values provide two large packet-size ratios (e.g.,  $\alpha_1 = \frac{1502 \text{ bytes}}{87 \text{ bytes}} = 17.26$  and  $\alpha_2 = \frac{1502 \text{ bytes}}{112 \text{ bytes}} = 13.41$ ) which ensure a zero-dispersion gap at  $dst$  over each testbed path configuration. Moreover, these values are within the upper bounds of the packet-size ratios of both C1-10 and C2-100. We sent 500 compound-probes using each  $s_t$  size to measure the end-link capacity. The time stamps of each compound probe at  $dst$  were obtained using Wireshark [11].

1) *Measured Intra-Probe Gaps at  $dst$ .* Figure 5 shows the distributions of the intra-probe gaps measured by  $dst$  over each testbed path when there was no cross-traffic load. The

theoretical values of the intra-probe gaps on the end link, i.e., the value of  $G(s_t)_n$  when  $\delta_n = 0$  in (11), for the 87- and 112-byte trailing packets over C1-10 are 80 and 100  $\mu\text{s}$ , respectively, considering  $IFG = 9.6 \mu\text{s}$  for  $l_4 = 10 \text{ Mb/s}$  [9]. The theoretical intra-probe gap values for the same packet sizes over C2-100 are 8 and 10  $\mu\text{s}$ , respectively, considering  $IFG = 0.96 \mu\text{s}$  for  $l_4 = 100 \text{ Mb/s}$  [9]. According to Figure 5(a), the intra-probe gaps measured over C1-10 for the 87- and 112-byte packets are tightly clustered around 79 and 99  $\mu\text{s}$ , respectively. Over C2-100, the measured intra-probe gaps are clustered around 7 and 9  $\mu\text{s}$  for the respective packet sizes, as shown by Figure 5(b). The solid and a dashed vertical-lines indicate the theoretical values and  $G_{peak}$  indicates the most frequent intra-probe gap for the 87- and 112-byte packets, respectively, in both graphs. In each graph, the measured intra-probe gaps smaller than the theoretical values are due to the  $1\text{-}\mu\text{s}$  clock resolution in the Linux system [12], [13]. However, the measured intra-probe gaps show that the compound probes did not experience dispersion over the paths since the used packet-size ratios avoid the effect of link heterogeneity.

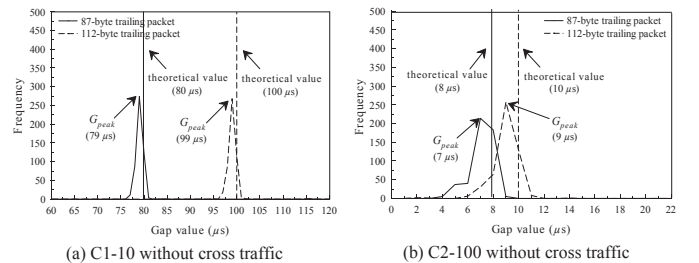


Fig. 5. Distributions of intra-probe gaps measured at  $dst$  over (a) C1-10 and (b) C2-100 without cross-traffic load.

2) *Effect of Cross Traffic on Intra-probe Gap Measurement.* Figure 6 shows the measured intra-probe gaps over C1-10 and C2-100 with 60% cross-traffic load, which consists of two symmetric cross-traffic flows at the second and third links,

respectively, of each four-hop path. We used small packet sizes, between 64 and 128 bytes, and the constant-bit-rate (CBR) traffic model in each flow to create a demanding environment on the testbed paths. In Figure 6, the distributions of the intra-probe gaps are similar to those in Figure 5 and the majority of the compound probe arrives at *dst* with a zero-dispersion gap for both trailing packet sizes. However, Figure 6(b) has some outlier values (i.e., large intra-probe gaps) at the right-hand side of the graph for both packet sizes, as compared to Figure 5(b). These gaps are affected by cross traffic which corresponds to the scenario when  $\delta_n > 0$  in (11).

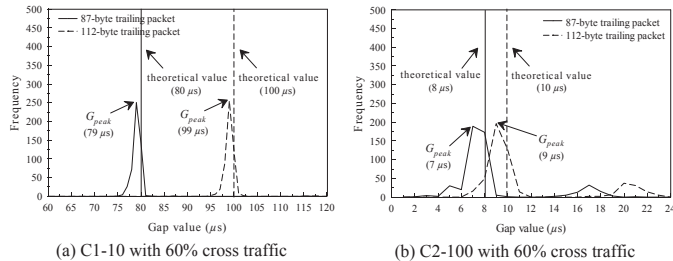


Fig. 6. Distributions of intra-probe gaps measured at *dst* over (a) C1-10 and (b) C2-100 with 60% cross-traffic load.

### B. Experimental Measurements in the Internet

We tested our analytical model over two Internet paths, an inter-state path in the U.S. and an international path between Taiwan and the U.S., between December 2010 and January 2011. The inter-state path was set between New York Institute of Technology (NYIT), New York, New York and New Jersey Institute of Technology (NJIT), Newark, New Jersey. This path is labeled as NYNJ and comprises 19 hops. The international path was set between Chaoyang University of Technology (CYUT), Taichung, Taiwan, and NJIT. This path is labeled as TWNJ and comprises 21 hops. We configured the workstations at NYIT and CYUT as *src* and the workstation (I531S) at NJIT as *dst*. These workstations were connected to either 10-Mb/s or 100-Mb/s links, but the capacities of the intermediate links along the paths are unknown. As for measuring the end link, the same  $s_t$  values used on the testbed paths, 87 and 112 bytes, were considered. However,  $s_h = 1512$  bytes was used instead of 1502 bytes considering the maximum payload size in an IP packet. We also used 500 compound-probes of each  $s_t$  size over each path, as in the testbed experiment. Figures 7(a) and 7(b) show the distributions of the intra-probe gaps measured by *dst* connected to 10-Mb/s and 100-Mb/s links, respectively, over the TWNJ path, which is the longest of the two Internet paths. Here, the gap distributions are similar to those measured on the testbed. The intra-probe gap distributions on the NYNJ path are also similar to those measured on the testbed paths. These results, therefore, show that the compound probe arrive at *dst* over the Internet paths with a zero-dispersion gap and can measure the end-link capacities with similar accuracy to that achieved on the testbed paths.

## VI. CONCLUSIONS

We presented an analytical model to determine the packet sizes in the packet-pair structure for the measurement of end-

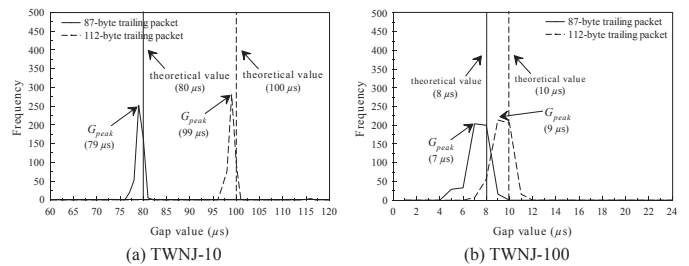


Fig. 7. Distributions of intra-probe gaps measured at *dst* over the TWNJ path with (a) 10-Mb/s and (b) 100-Mb/s end links.

link capacity over a network path. The model is derived by considering the heterogeneous link capacities and cross-traffic load of the path to ensure a zero-dispersion gap in the packet pair for accurate end-link capacity measurement. We numerically evaluated the model using different path configurations and cross-traffic loads. We also presented experimental results of end-link capacity measurements on a controlled testbed and in the Internet. The outcomes of the numerical evaluations verify the analytical model. The experiment results show that high measurement accuracy can be achieved, irrespective of link heterogeneity and cross-traffic load of a path, when suitable packet sizes are used in the packet-pair structure. Our experiments also show that the proposed model is practical.

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