

## ECE 642 - Midterm Spring 2014

*Please justify all your responses (responses without justifications will not be considered). Please label your axes and plot with care.*

**1. (4 points)** Consider the signal  $x(t) = \sum_{n=-\infty}^{\infty} s(t - 2n)$ , where  $s(t)$  is a rectangle of unit height spanning the interval  $[-1/2, 1/2]$ .

- a. Plot  $x(t)$ .
- b. Calculate and plot the Fourier transform  $X(f)$ .
- c. Consider a bandpass filter  $H_c(f)$  with unit gain, central frequency equal to  $3/2$  Hz and bandwidth equal to 1 Hz. Calculate the output  $y(t)$  (in the time domain) of this filter when the input is  $x(t)$ .
- d. Evaluate the frequency response of the equivalent baseband filter  $H_z(f)$ .

**2. (5 points)** We are given the complex baseband signal  $x_z(t) = \text{sinc}(t - 1) + j2\text{sinc}(t)$ .

- a. Calculate the real part and the imaginary parts of the Fourier transform  $X_z(f)$  (to express the transforms, please use the function  $\text{rect}(t)$ , which is defined as a rectangle of unit height and spanning the interval  $[-1/2, 1/2]$ ).
- b. Plot the real and imaginary parts of  $X_z(f)$ . Comment on the symmetry or lack thereof of these plots.
- c. Plot the real part of the Fourier transform of the bandpass signal obtained by upconverting  $x_z(t)$  to the carrier frequency 10 Hz.
- d. Plot the imaginary part of the Fourier transform of the bandpass signal of the previous point.
- e. Choose a sampling frequency for the bandpass signal at the previous points.

**3. (2 points)** Consider the baseband message  $m(t) = \text{rect}(t)$  (the function  $\text{rect}(t)$  is defined at the previous problem). The message is modulated using DSB-AM with  $A = 1$  and is received through a channel with phase  $\phi_P = \pi$ .

- a. Draw the baseband equivalent block diagram of the DSB-AM system including the explicit equations for all the involved signal ( $x_z(t)$ ,  $r_z(t)$ , etc.).
- b. Assume that the baseband demodulator uses the wrong phase  $\theta_P = \pi/2$ , instead of  $\phi_P = \pi$ . What is the demodulated message  $\hat{M}(t)$  (you can neglect the noise)?