Lecture 13

Momentum Conservation And Collisions

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Physics 105 Fall 2009

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Linear Momentum

New fundamental quantity (like force, energy,..)

Particle:

$$\vec{p} = m\vec{v}$$

System of Particles:

$$\vec{P}$$
 =m₁ \vec{v}_1 +m₂ \vec{v}_2 +...

Extended objects:

$$ec{P} = M ec{v}_{
m com}$$

Relation to Force: $\vec{F}_{tot} = m\vec{a}$

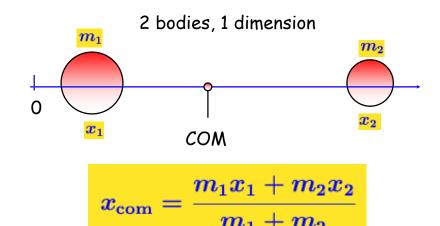
$$ec{F}_{
m net} = rac{dec{p}}{dt}$$

$$ec{F}_{
m net} = rac{dec{P}}{dt}$$

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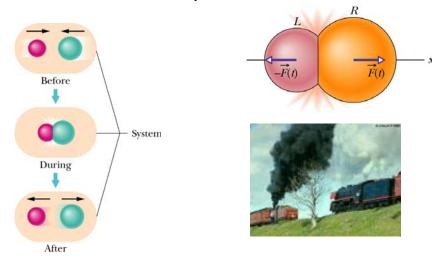
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Center of Mass for a system of particles



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Collision of two particle-like bodies



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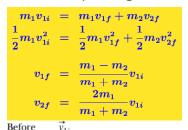
Elastic Collisions in 1D

change, but the total kinetic energy of the system does not change

Stationary Target

Projectile Target

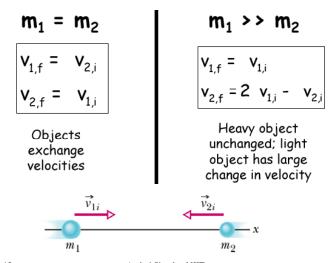
After



Moving Target

In an elastic collision, the kinetic energy of each colliding body may

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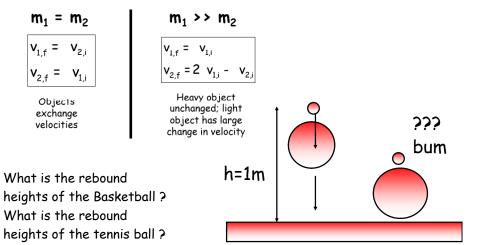


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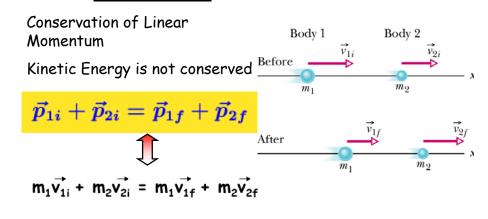
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Inelastic Collisions in 1D



Cannot solve based only on the information about the state before the collision

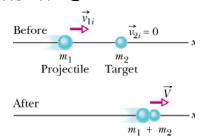
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Completely Inelastic Collision Collisions in 1D

Conservation of Linear Momentum works!

$$ec{p}_{1i} + ec{p}_{2i} = ec{p}_{1f} + ec{p}_{2f}$$

$$egin{array}{lcl} m_1 v_{1i} &=& (m_1 + m_2) V \ V &=& rac{m_1}{m_1 + m_2} v_{1i} \end{array}$$



Example: Two equal objects, one initially at rest

$$mv_i = 2mv_f \longrightarrow v_f = v_i/2$$

Final Kinetic Energy =
$$\frac{1}{2}(2m)(v_i/2)^2$$
 Half the original Kinetic Energy

Lecture 13 = $\frac{1}{4}m(v_i)^2$

Who wins?







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How can we reach another star?



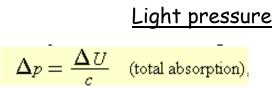




Combination of

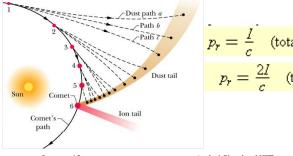
- >Regular rocket
- >Ion-drive engine
- >And Solar sail







$$\Delta p = \frac{2\Delta U}{c}$$
 (total reflection back along path)



 $p_r = \frac{I}{c}$ (total absorption)

 $p_r = \frac{2I}{c}$ (total reflection back along path)

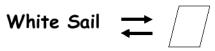
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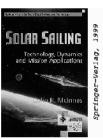


Photons bounce off

Black Sail



Photons adsorbed



What color/material is the best for the Light Sail?

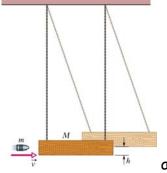
A) Black; B) Mirror-type; C) Blue; D) any

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Sample Problem

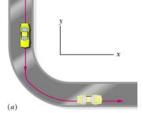


Ballistic Pendulum. A bullet is fired into the block (M = 5 kg, m = 10 g). The block/bullet is then swinging upward, their center of mass rising h = 6 cm. What is the speed of the bullet just prior to the collision?

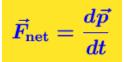
- a) Linear Momentum is conserved at the collision
- b) After collision the Energy is conserved

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QZ#13 Linear Momentum



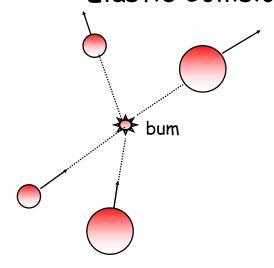




The figure shows a **2.0 kg** toy car before and after taking a turn on a track. Its speed is **0.30 km/s** before the turn and **0.40 km/s** after the turn. The turn takes **0.33** seconds.

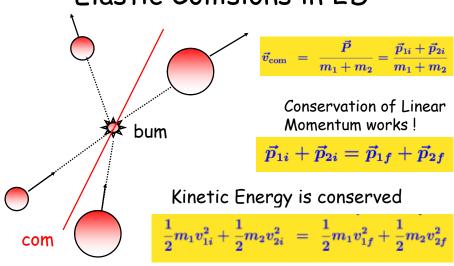
- (a) What is the change ΔP in the linear momentum of the car due to the turn?
- (b) What is the **average force** of friction between the car and the road during the turn?

Elastic Collisions in 2D



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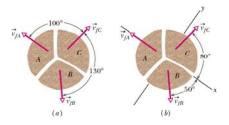
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Conservation of Linear Momentum

$$\vec{P} = {
m const.} \quad \Rightarrow \quad \vec{P_i} = \vec{P_f}$$



A firecracker placed inside a coconut of mass M, initially at rest on a frictionless floor, blows the coconut into three pieces that slide across the floor. An overhead view is shown. Piece C, with mass 0.30 M, has final speed $v_{fC} = 5.0 m/s$.

- (a) What is the speed of piece B, with mass 0.2 M?
- (b) (b) What is the speed of piece A?

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